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EUROPEAN CENTRE FOR THEORETICAL STUDIES  
IN NUCLEAR PHYSICS AND RELATED AREAS  
TRENTO, ITALY

# Status and Prospects of $e^+e^-$ hadronic cross sections at low energy

G. Venanzoni LNF/INFN

**Scattering and annihilation electromagnetic processes**

Trento 18-22 February 2013

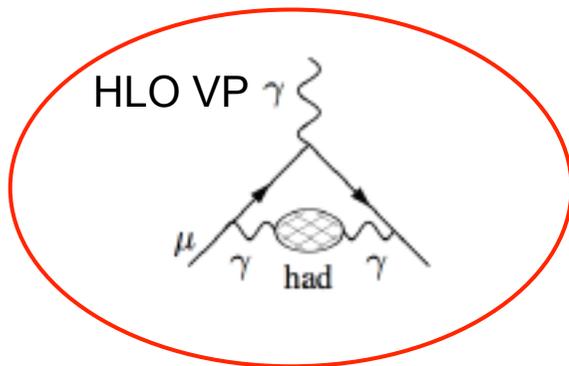
# Importance of precision $R \equiv \frac{\sigma(e^+e^- \rightarrow \text{hadrons})}{\sigma_0(e^+e^- \rightarrow \mu^+\mu^-)}$ measurements

- $(g-2)_\mu$  and  $\alpha_{\text{e.m.}}(M_Z)$
- CVC tests between  $e^+e^-$  and  $\tau$
- QCD sum rules and  $\alpha_S$
- Test of models and input to theory (ChPT, VDM, QCD,...)
- Spectroscopy, search of hybrids and glueballs
- Search for hypothetical light gauge bosons
- ...

# Muon anomaly

$$a_\mu = \frac{(g_\mu - 2)}{2}$$

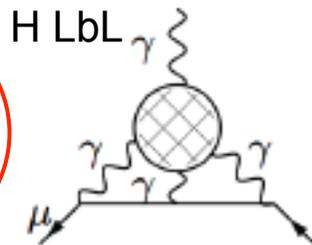
- Long established discrepancy ( $>3\sigma$ ) between SM prediction and BNL E821 exp.
- Theoretical error  $\delta a_\mu^{\text{SM}}$  ( $\sim 6 \times 10^{-10}$ ) dominated by HLO VP ( $4 \div 5 \times 10^{-10}$ ) and HLbL ( $[2.5 \div 4] \times 10^{-10}$ ). A **twofold** improvement on  $\delta a_\mu^{\text{SM}}$  from 2001 (thanks to new  $e^+e^-$  measurements)!
- Experimental error  $\delta a_\mu^{\text{EXP}} \sim 6 \times 10^{-10}$  (E821). Plan to reduce it to  $1.5 \times 10^{-10}$  by the new g-2 experiments at FNAL and J-PARC.



$$a_\mu^{\text{HLO}} = (690.9 \pm 4.4) \cdot 10^{-10}$$

[Eidelman, TAU08]

$$\delta a_\mu^{\text{HLO}} \sim 0.7\%$$



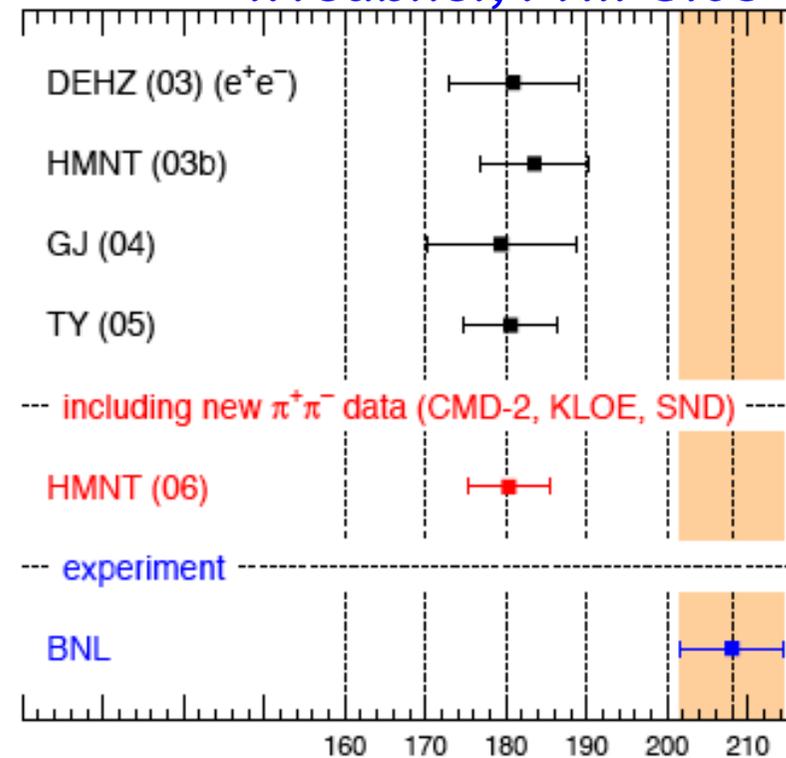
$$a_\mu^{\text{HLbL}} = (10.5 \pm 2.6) \cdot 10^{-10}$$

[Prades, dR&V. 08]  
 $(11 \pm 4) \cdot 10^{-10}$  (Jegerlehner, Nyffler)

$$\delta a_\mu^{\text{HLbL}} \sim 25-40\%$$

$a_\mu^{\text{SM}}$  compared to BNL world av.

*T. Teubner, PHIPSI08*



$$a_\mu^{\text{SM}} \times 10^{10} - 11659000$$

$$a_\mu^{\text{EXP}} - a_\mu^{\text{TH}} = (27.6 \pm 8.1) \cdot 10^{-10}, \sim 3.4\sigma$$

$$\text{In 2001 } a_\mu^{\text{EXP}} - a_\mu^{\text{TH}} = (23 \pm 16) \cdot 10^{-10}$$

# $a_\mu^{\text{HLO}}$

L.O. Hadronic contribution to  $a_\mu$  can be estimated by means of a dispersion integral:



$$a_\mu^{\text{had}} = \left( \frac{\alpha m_\mu}{3\pi} \right)^2 \int_{4m_\pi^2}^{\infty} ds \frac{R(s) \hat{K}(s)}{s^2}$$

$1 / s^2$  makes **low energy contributions** especially important:

$$e^+ e^- \rightarrow \pi^+ \pi^-$$

in the range  $< 1$  GeV contributes to 70% !

$$R(s) = \frac{\sigma_{\text{tot}}(e^+ e^- \rightarrow \gamma^* \rightarrow q \bar{q} \rightarrow \text{hadrons})}{\sigma_{\text{tot}}(e^+ e^- \rightarrow \gamma^* \rightarrow \mu^+ \mu^-)}$$

- $K(s)$  = analytic kernel-function
- above sufficiently high energy value, typically 2...5 GeV, use *pQCD*

Input:

- a) **hadronic electron-positron cross section data** (G.dR 69, E.J.95, A.D.H.'97,....)
- b) **hadronic  $\tau$ - decays**, which can be used with the help of the CVC-theorem and an isospin rotation (plus isospin breaking corrections)

(A., D., H. '97)

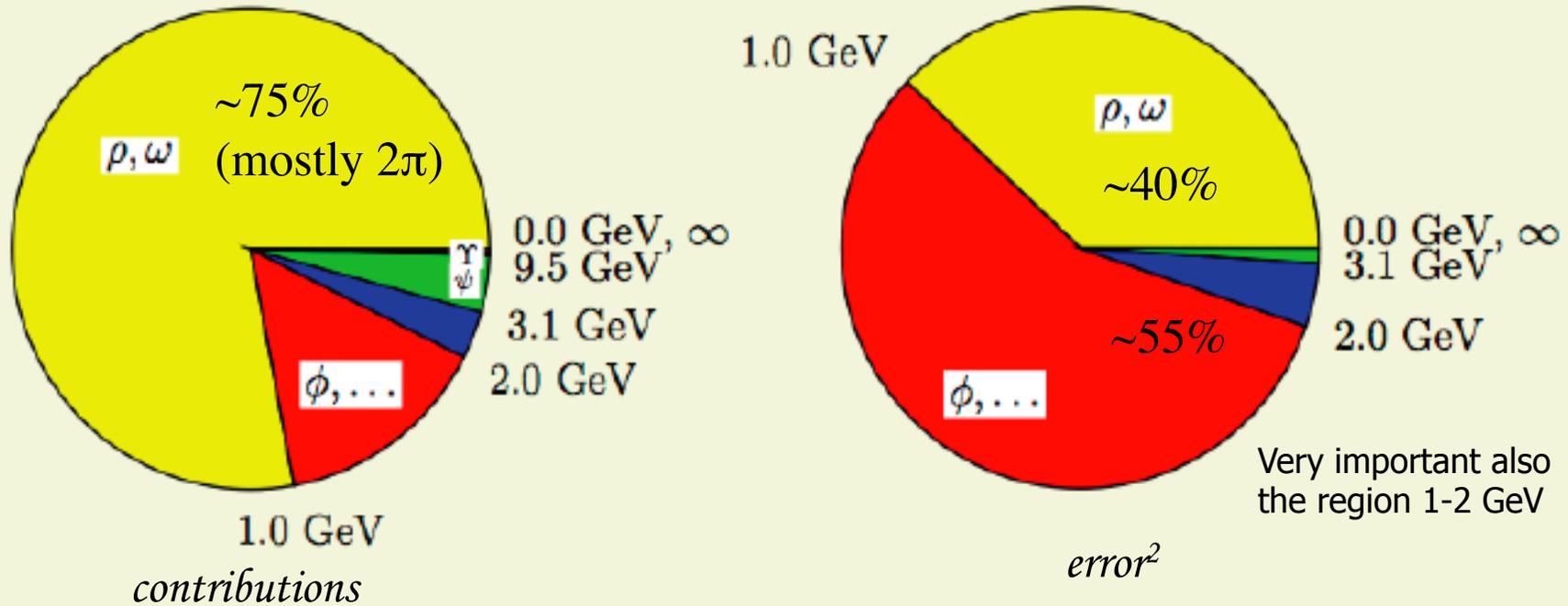
# Dispersion Integral:

$$a_{\mu}^{HLO} = \int_{4m_{\pi}^2}^{\infty} \sigma_{had}(s)K(s)ds$$

$$K(s) \sim 1/s$$

Contribution of different energy regions to the dispersion integral and the error to  $a_{\mu}^{HLO}$

F. Jegerlehner, Talk at PHIPSI08



Experimental errors on  $\sigma^{had}$  translate into theoretical uncertainty of  $a_{\mu}^{had}$ !  
 → Needs precision measurements!

$$\delta a_{\mu}^{exp} \rightarrow 1.5 \cdot 10^{-10} = 0.2\% \text{ on } a_{\mu}^{HLO}$$

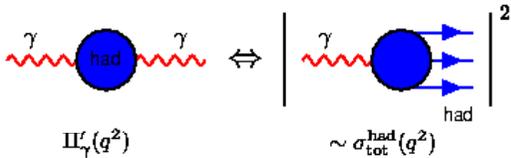
New g-2 exp.

# $\alpha_{em}(M_Z)$ and EW fit of the SM ( $M_{Higgs}$ )

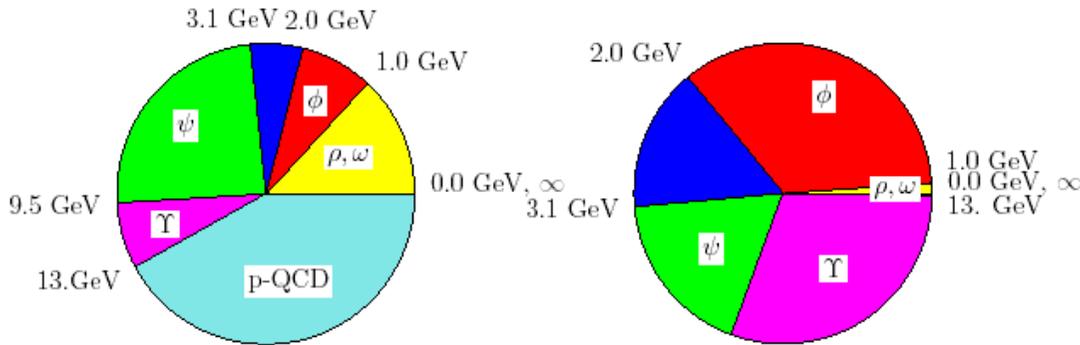
$$\alpha(M_Z) = \frac{\alpha(0)}{1 - \Delta\alpha(M_Z)}$$

$$\Delta\alpha = \Delta\alpha_l + \Delta\alpha_{had}^{(5)} + \Delta\alpha_{top}$$

polarization function  $\Pi_\gamma^L(q^2)$



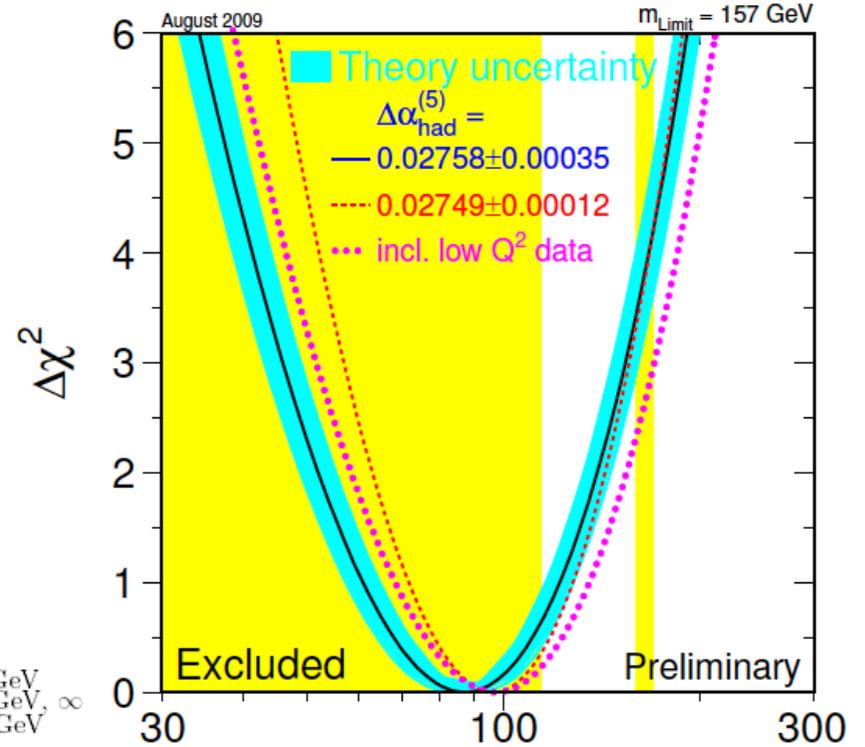
$$\Delta\alpha_{had}^{(5)}(M_Z^2) = -\frac{\alpha M_Z^2}{3\pi} \text{Re} \int_{4m_\pi^2}^{\infty} ds \frac{R(s)}{s(s - M_Z^2 - i\epsilon)}$$



$$\Delta\alpha_{had}^{(5)}(M_Z^2)$$

$$\delta^2 \Delta\alpha_{had}^{(5)}(M_Z^2)$$

$$\delta\alpha(M_Z)/\alpha(M_Z) \sim 2 \times 10^{-4} \rightarrow 5 \times 10^{-5}$$



$$\Delta\alpha_{had}^{(5)}(M_Z^2) = 0.027607 \pm 0.000225$$

$$\alpha^{-1}(M_Z^2) = 128.947 \pm 0.035$$

$$\alpha^{-1}(0) = 137.0359895 \pm 0.0000061$$

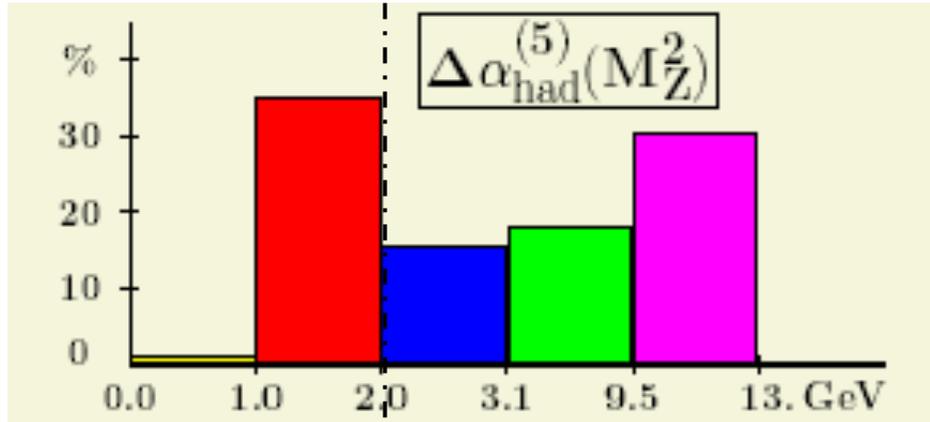
FJ08

Requirement from ILC (6x improvement)

# Comparison of error profiles for $\alpha_{em}(M_Z)$

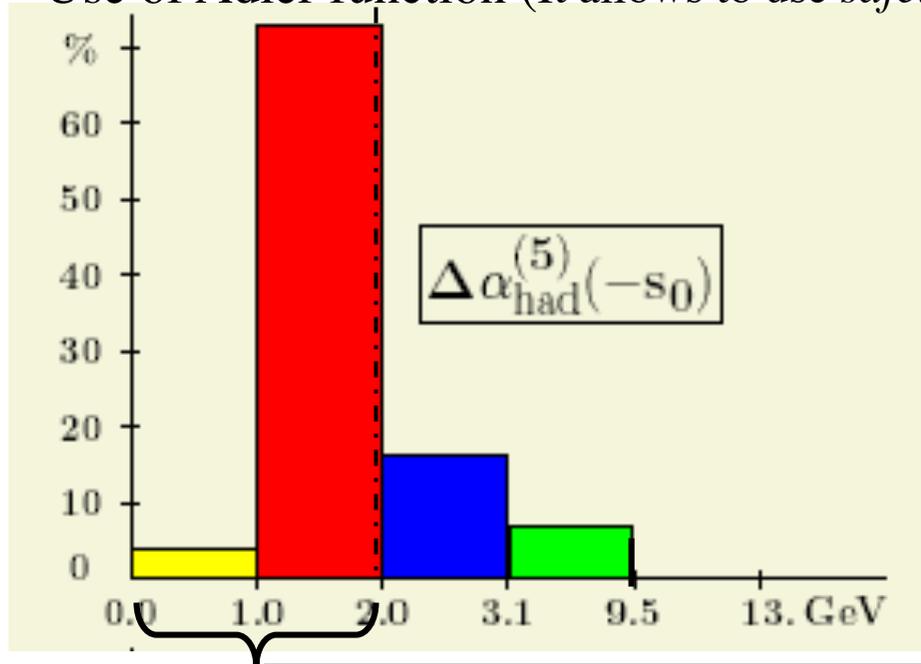
Direct integration of energy points

*F. Jegerlehner, Nucl. Phys. B  
181-182 (2008) 135*



→  $\delta\sigma$  at 1% in the region  $\sqrt{s} < 10$  GeV  
 ⇒ improvement of  $\sim 3$  in  $\delta\alpha(M_Z)$

Use of Adler function (It allows to use *safely* pQCD down to 2.5 GeV)



→ 1% in the region  $1 < \sqrt{s} < 2.5$  GeV  
 ⇒ improvement of  $\sim 5$  on  $\delta\alpha(M_Z)$

$2m_\pi < \sqrt{s} < 2$  GeV

**Extremely important:**

- 80% of  $\delta\Delta\alpha_{had}^{(5)}$  (using Adler function)
- 95% of  $\delta a_\mu$

# Cross section data:

Two approaches:

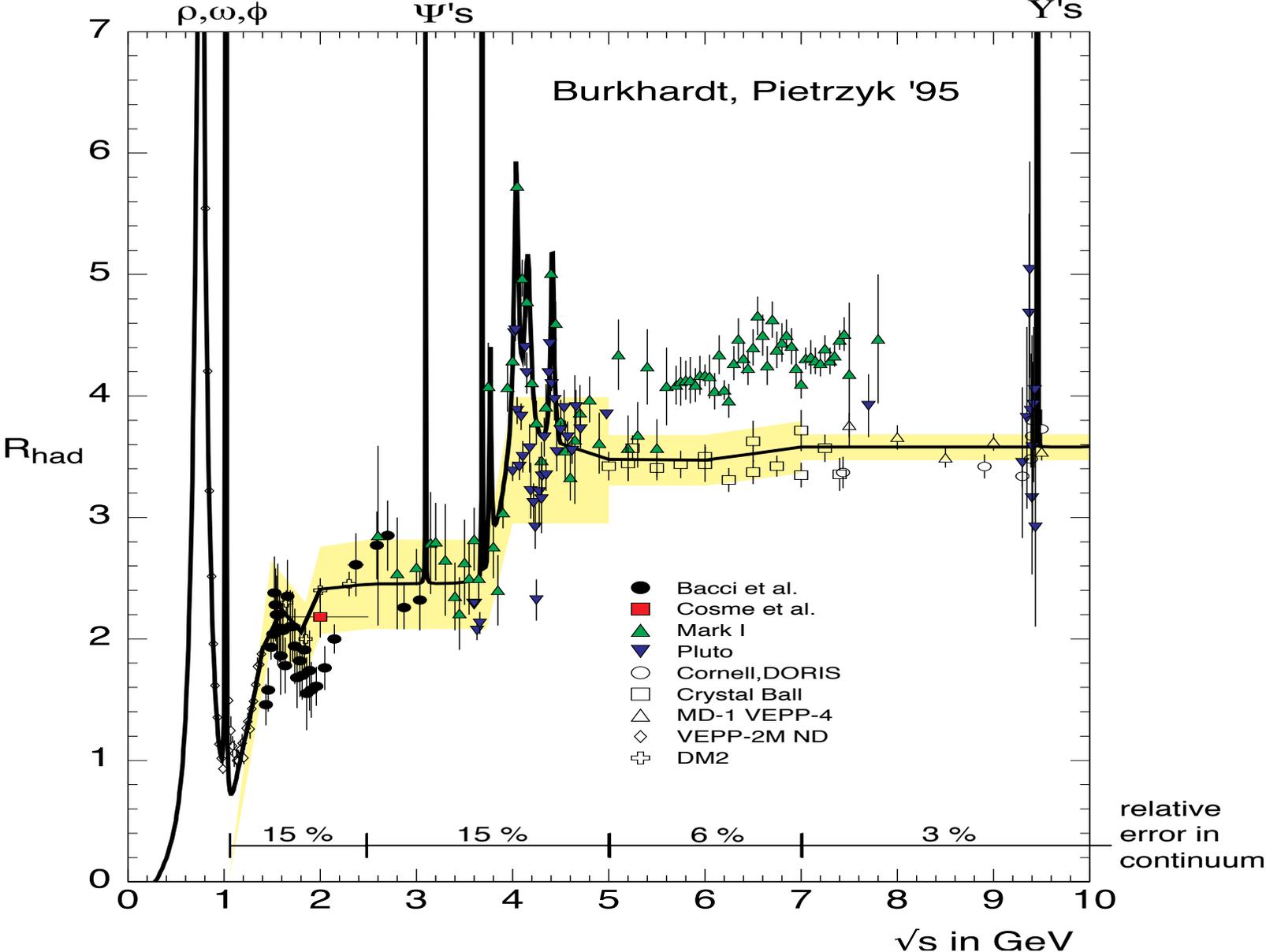
Energy scan (CMD2, SND, BES, CLEO):

- energy of colliding beams is changed to the desired value
- “direct” measurement of cross sections
- needs dedicated accelerator/physics program
- needs to measure luminosity and beam energy for every data point

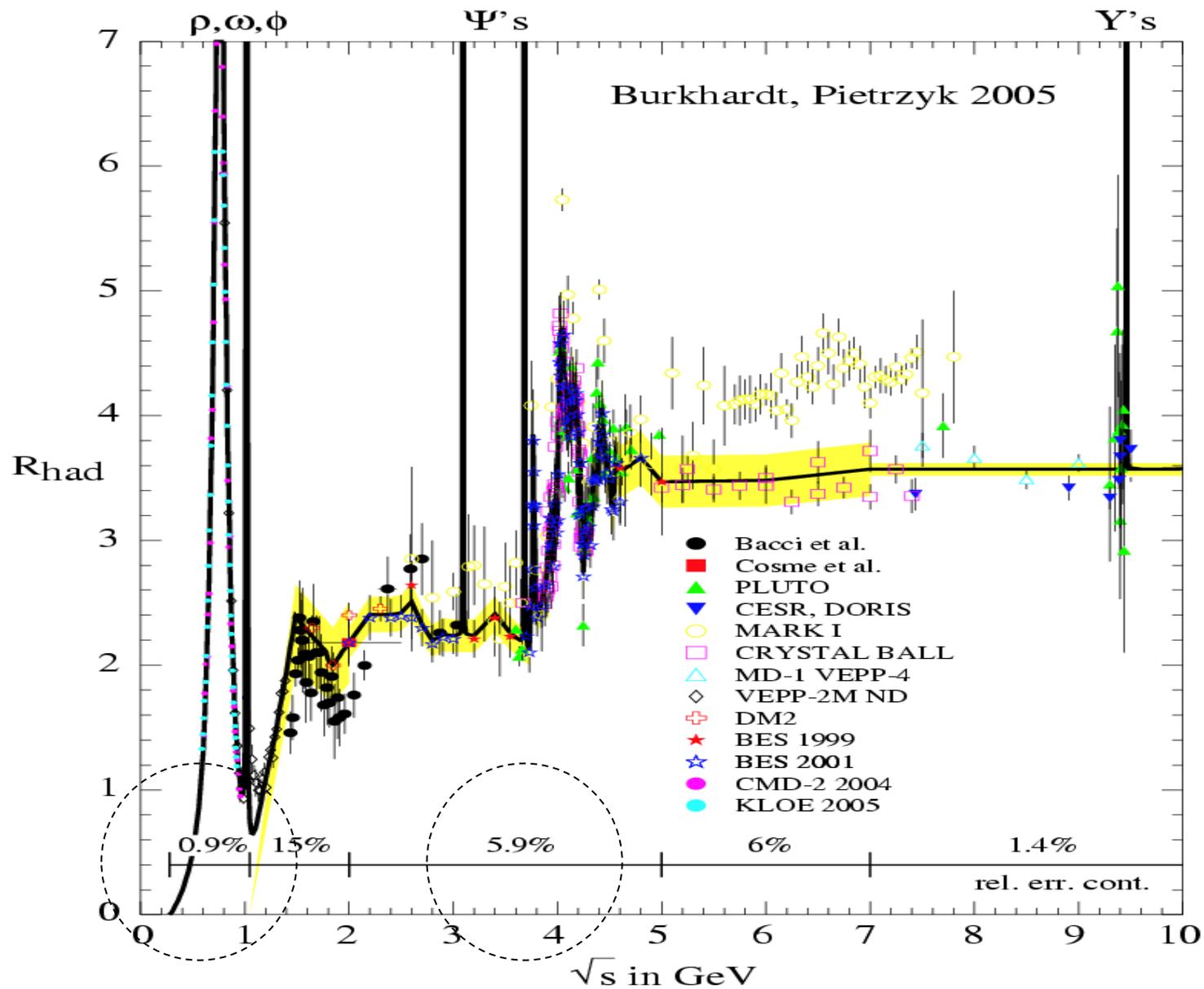
Radiative return (KLOE, BABAR, BELLE, BESIII?):

- runs at **fixed-energy machines** (meson factories)
- use **initial state radiation** process to access lower lying energies or resonances
- data come as by-product of standard physics program
- requires precise theoretical calculation of the **radiator function**
- luminosity and beam energy enter only once for all energy points
- needs larger integrated luminosity

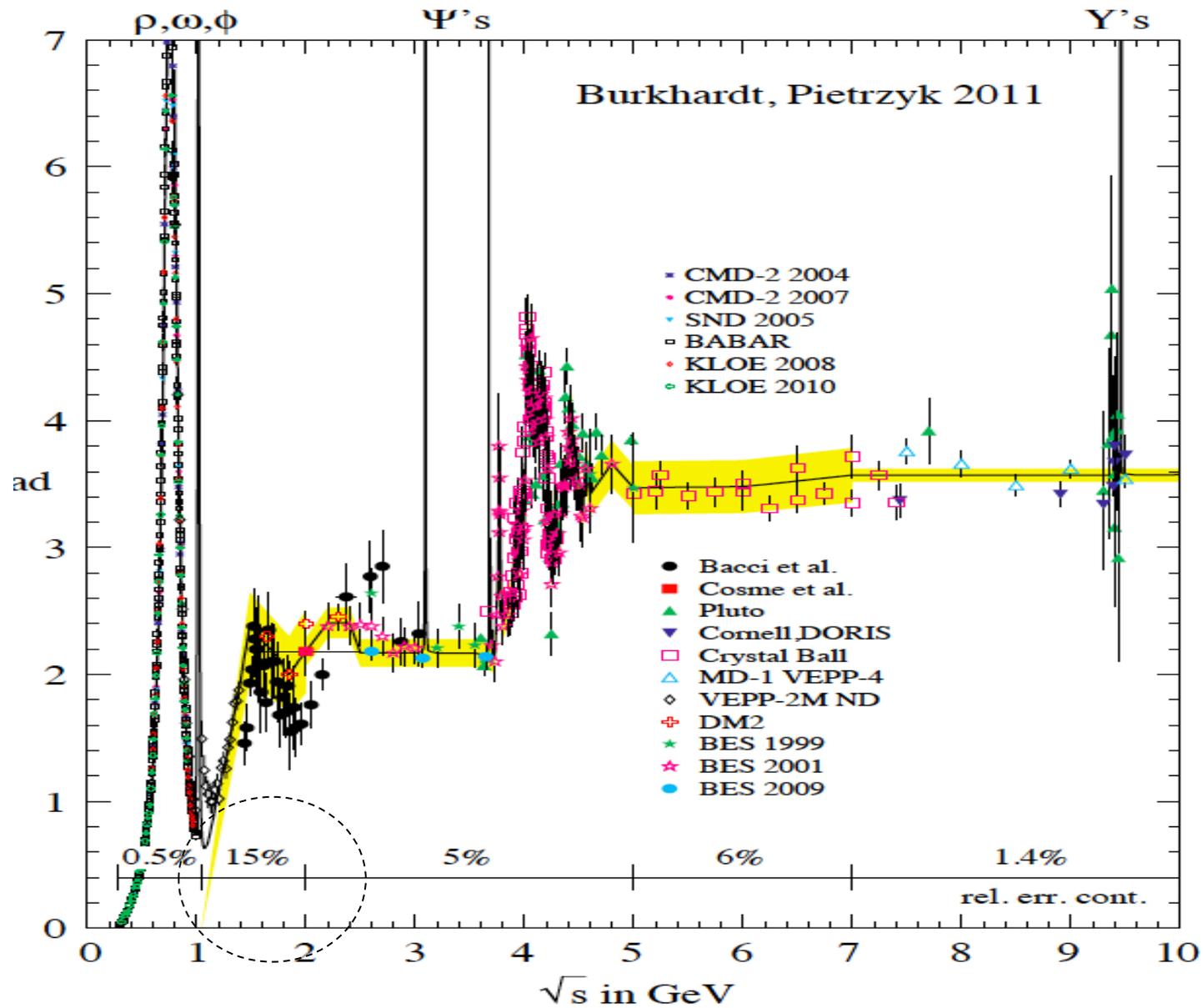
# Data at '95



# Data at '05



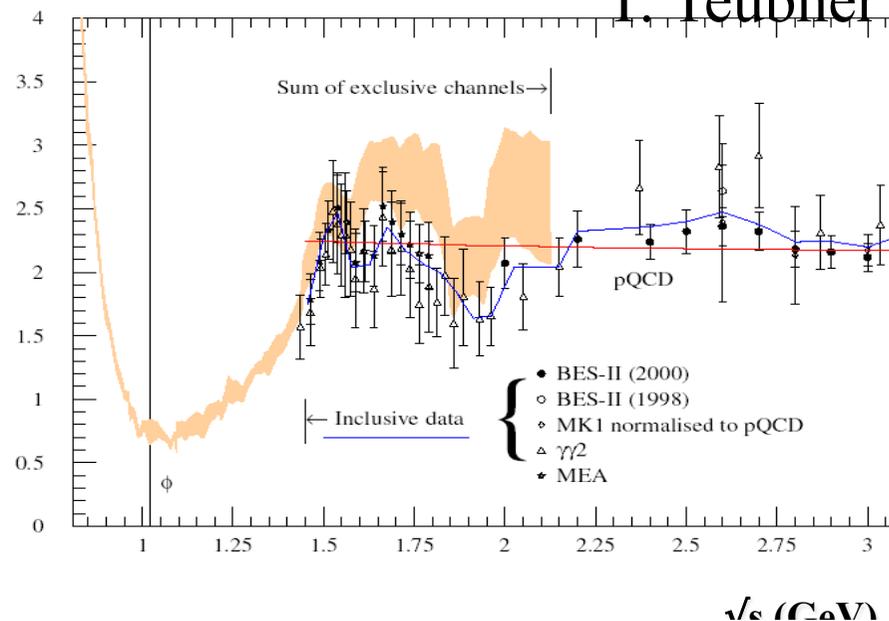
# Data at '11



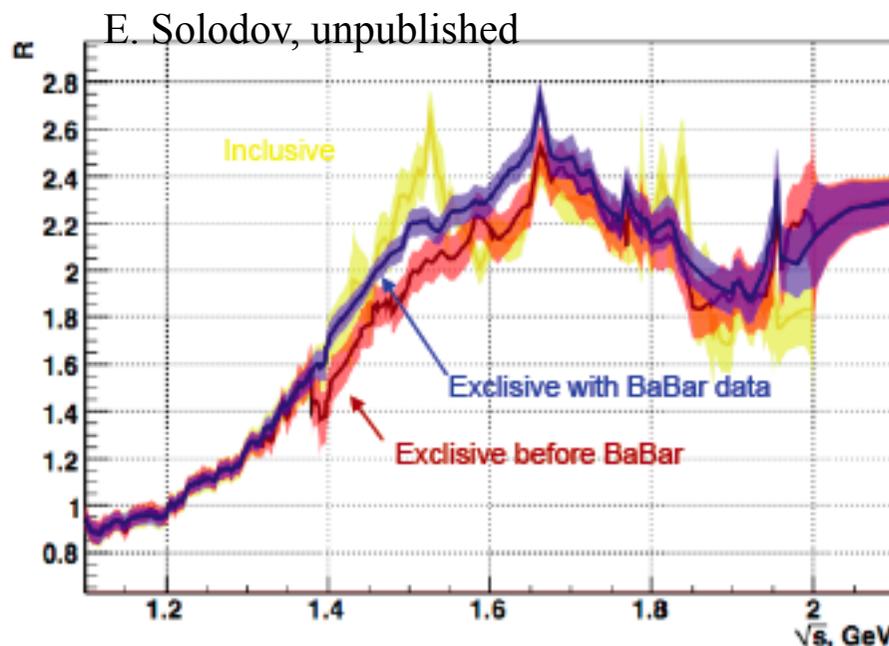
# Exclusive vs inclusive measurements?

T. Teubner

- 1) Most recent inclusive measurements: MEA and B antiB, with **total** integrated luminosity of **200 nb<sup>-1</sup>** (one hour of data taking at **10<sup>32</sup> cm<sup>-2</sup> sec<sup>-1</sup>**). **10% stat.+ 15% syst. Errors**



- 2) New BaBar data is improving a lot this region. However still the question on the completeness of exclusive data vs systematics of old inclusive measurements



# Radiative corrections are important!

- Unclear treatment of R.C. in old data.
- Reevaluation of RC leads to significant changes in recent data
- New data (CMD-2, SND, KLOE, Babar) paid more attention to :
  - ISR
  - Vacuum Polarization (VP)
  - FSR
- A lot of work for theorists to provide accurate MC generators (and for experimentalists to test it!)

$$\sigma_{bare} = \sigma_{dressed} |1 - \Pi(s)|^2 (1 + C_{FSR})$$

$$\bullet \sigma_{dressed} = \frac{N}{\int L dt \epsilon (1 + \delta_{ISR})}$$

$$\bullet \Pi(s) = \Pi_{lep}(s) + \Pi_{had}(s)$$

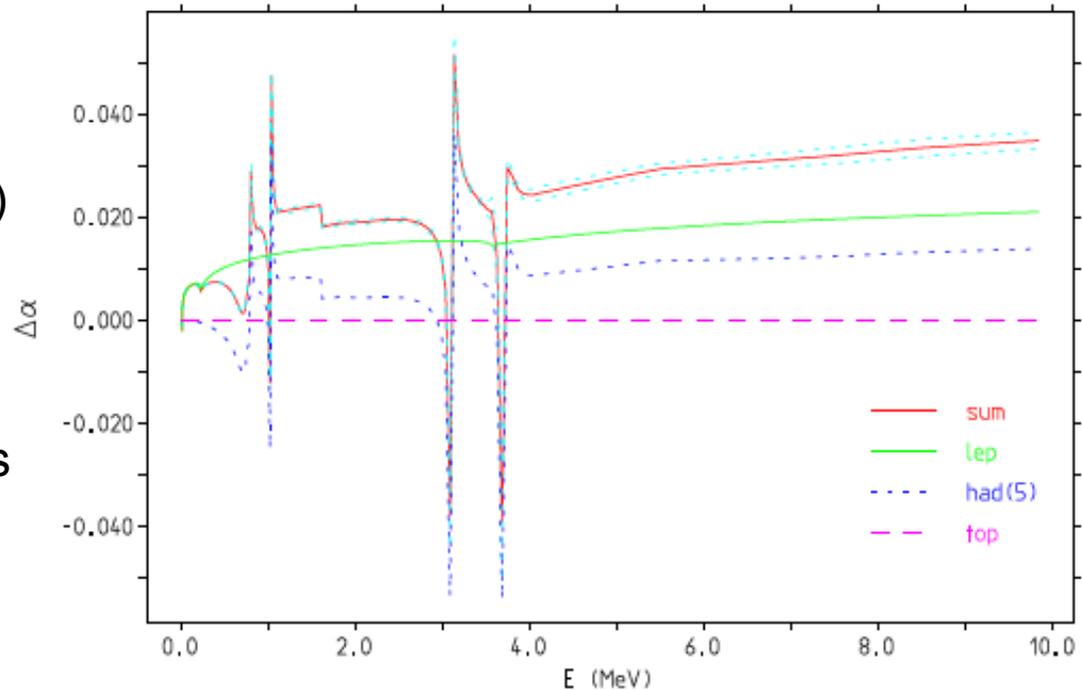


Figure from Fred Jegerlehner

# A common effort for RC and Monte Carlo tools

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THE EUROPEAN  
PHYSICAL JOURNAL C

Review

## Quest for precision in hadronic cross sections at low energy: Monte Carlo tools vs. experimental data

Working Group on Radiative Corrections and Monte Carlo Generators for Low Energies

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~60 participants, 13 countries

See [www.inf.infn.it/wg/sighad](http://www.inf.infn.it/wg/sighad) for more information  
(next meeting 11-12 April 2013, ECT\*)

## *"Old" Results on R from energy scan at $\sqrt{s} < 10$ GeV*

<u>Place</u>	<u>Ring</u>	<u>Detector</u>	<u><math>E_{cm}</math> (GeV)</u>	<u>pts</u>	<u>Year</u>
Novosibirsk	VEPP-2M	CMD2,SND	<1.4	128	<b>01-03</b>
	VEPP-2	Olya,ND,CMD	<1.4		79-85 97-99
Beijing	BEPC	BESII	2-5	85	<b>98-99</b>
Orsay	DCI	M3N,DMI,DM2	1.35-2.13	33	'78
Frascati	Adone	$\gamma\gamma$ 2,MEA, Boson,BCF	1.42-3.09	31	'78
SLAC	Spear	MarkI	2.8-7.8	78	'82
Cornell	CESR	CLEO	3-5		'05
Hamburg	Doris	DASP	3.1-5.2	64	'79
		PLUTO	3.6-4.8,9.46	27	'77
		C.Ball	5.0-7.4	11	'90
		LENA	7.4-9.4	95	'82
Novosibirsk	VEPP-4	MD-1	7.23-10.34	30	'91

## *Recent Results with ISR*

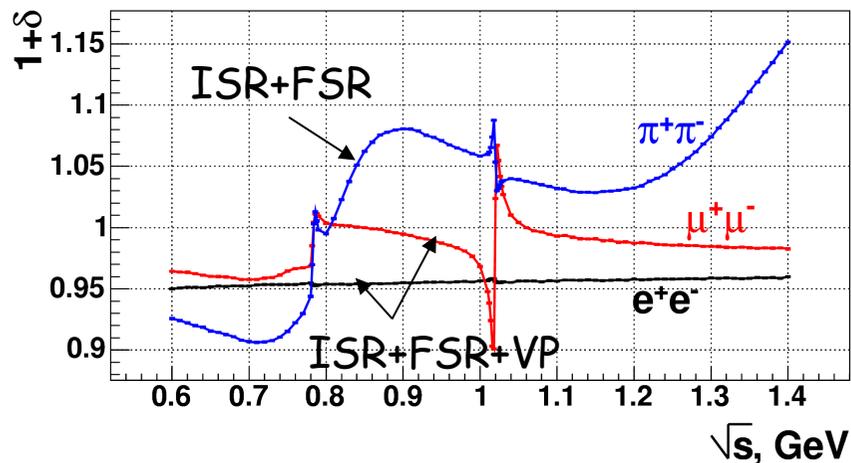
<u><i>Place</i></u>	<u><i>Ring</i></u>	<u><i>Detector</i></u>	<u><i>E<sub>cm</sub>(GeV)</i></u>	<u><i>pts</i></u>	<u><i>Year</i></u>
Frascati	DAΦNE	KLOE	<1 GeV		'05-08-10
SLAC	PEPII	BaBar	<5 GeV		'05-10...
Tsukuba	KEKB	Belle	<5 GeV		'08-10...

## *New Results or Upgrades*

<u><i>Place</i></u>	<u><i>Ring</i></u>	<u><i>Detector</i></u>	<u><i>E<sub>cm</sub>(GeV)</i></u>	<u><i>pts</i></u>	<u><i>Year</i></u>
Novosibirsk	VEPP-2000	CMD3 and SND2	<2		10
Beijing	BEPCII	BESIII	2-4.6 (<3 with ISR)		10
Frascati	DAΦNE	KLOE-2	<1 (→2.5?)		'12
Tsukuba	KEKB	SuperBelle	<5 GeV		'14?

# Recent results with energy scan:

- In the last years main results were published from: CMD2 and SND @VEPP-2M, BESII@BEPC, CLEO@CESR:
- 1)VEPP-2M, Novosibirsk (*exclusive* measurements)  $0.4 < E_{cm} < 1.4 \text{ GeV}$ 
  - New results on  $e^+e^- \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ ,  $\pi^+ \pi^- \pi^0 \pi^0$  ( $\sigma_{\text{syst}} \sim 7\%$ ),  $e^+e^- \rightarrow \pi^+ \pi^- \pi^0$  ( $\sigma_{\text{syst}} \sim 12\%$ ),  $e^+e^- \rightarrow K_S, K_L$ ,  $e^+e^- \rightarrow \omega \pi^+ \pi^-$ ,  $\eta \pi^+ \pi^-$  ( $\sigma_{\text{syst}} \sim 15\%$ ) from CMD2 and SND
  - $e^+e^- \rightarrow \pi^+ \pi^-$  from CMD2 with  $\sigma_{\text{syst}} \sim 1.0\%$  ( $\sigma_{\text{syst}} \sim 0.6\%$  in  $0.61 < E < 0.96 \text{ GeV}$ )
  - $e^+e^- \rightarrow \pi^+ \pi^-$  from SND with  $\sigma_{\text{syst}} \sim 1.3\%$



Sources of errors	CMD-2 $\sqrt{s} < 1 \text{ GeV}$	SND	CMD-2 $1.4 > \sqrt{s} > 1 \text{ GeV}$
Event separation method	0.2–0.4%	0.5%	0.2–1.5%
Fiducial volume	0.2%	0.8%	0.2–0.5%
Detection efficiency	0.2–0.5%	0.6%	0.5–2%
Corrections for pion losses	0.2%	0.2%	0.2%
Radiative corrections	0.3–0.4%	0.2%	0.5–2%
Beam energy determination	0.1–0.3%	0.3%	0.7–1.1%
Other corrections	0.2%	0.5%	0.6–2.2%
The total systematic error	0.6–0.8%	1.3%	1.2–4.2%

# How cross-section is measured

All modes except  $2\pi$

$$\sigma(e^+e^- \rightarrow H) = \frac{N_H - N_{bg}}{L \cdot \varepsilon \cdot (1 + \delta)}$$

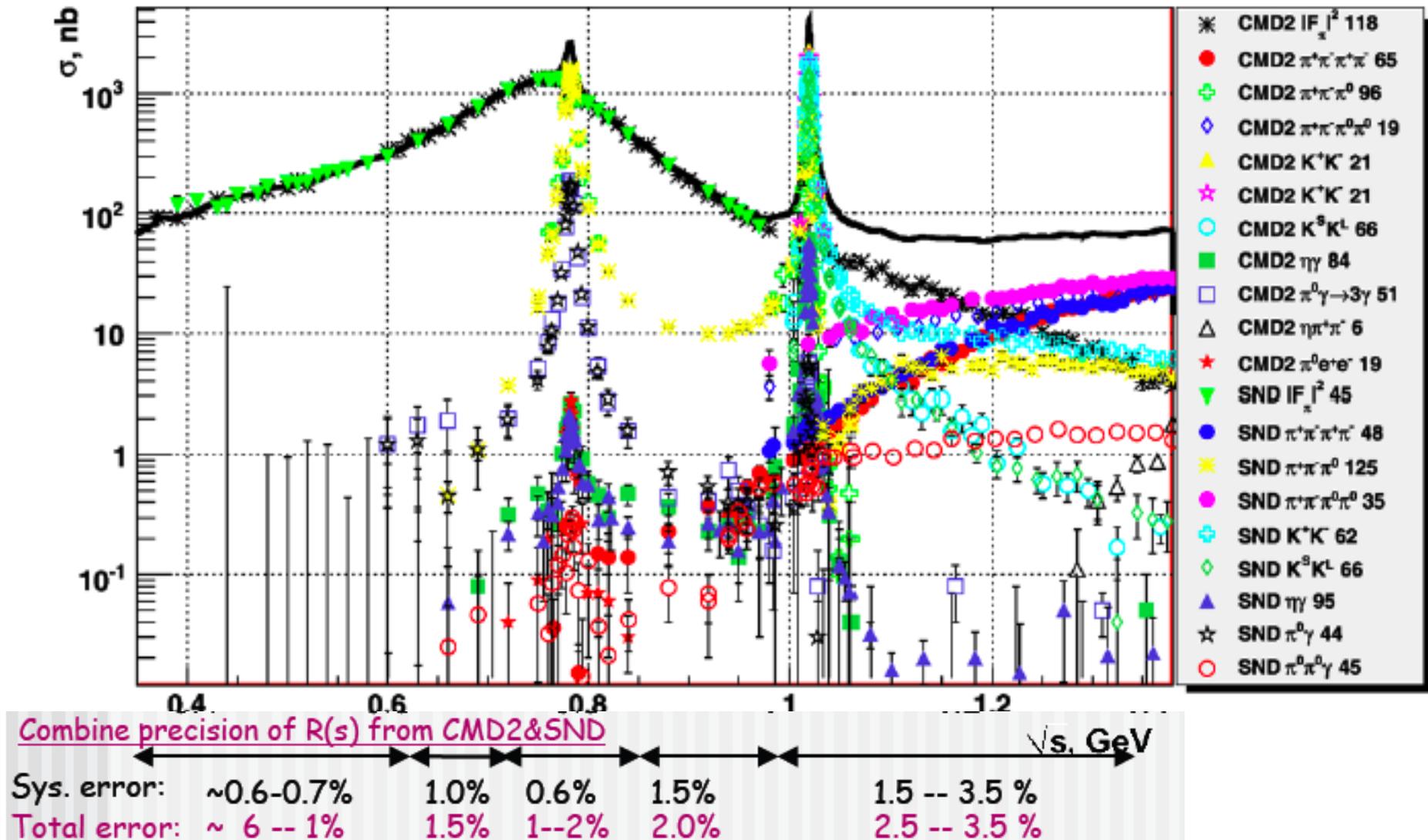
- Luminosity  $L$  is measured using Bhabha scattering at large angles
- Efficiency  $\varepsilon$  is calculated via Monte Carlo + corrections for imperfect detector
- Radiative correction  $\delta$  accounts for ISR effects only

$2\pi$

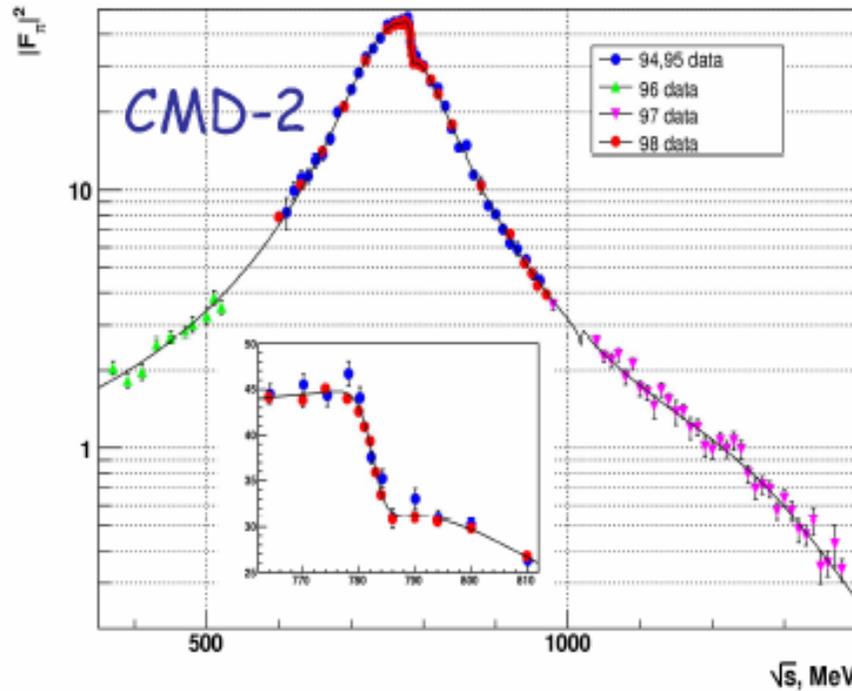
$$|F_\pi|^2 = \frac{N_{2\pi}}{N_{ee}} \cdot \frac{\sigma_{ee} \cdot (1 + \delta_{ee})}{\sigma_{2\pi}(\text{point-like } \pi) \cdot (1 + \delta_{2\pi})}$$

- Ratio  $N(2\pi)/N(ee)$  is measured directly  $\Rightarrow$  **detector inefficiencies are cancelled out**
- Virtually no background
- Analysis does not rely on simulation
- Radiative corrections account for ISR and FSR effects
- **Formfactor is measured to better precision than  $L$**

# Measurement of exclusive channels with CMD-2/SND



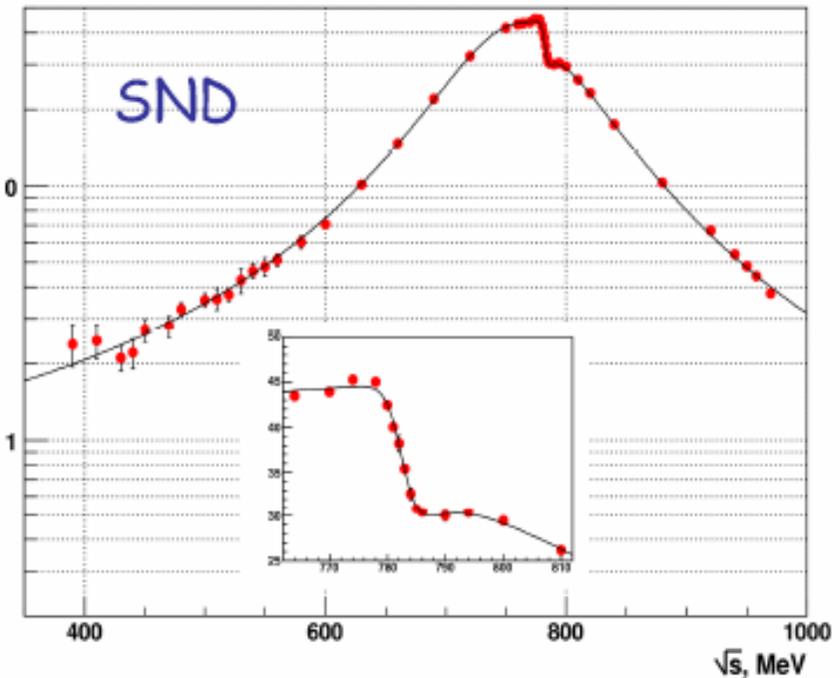
# Pion form factor @ Novosibirsk (with energy scan)



Systematic error  
 0.7%      0.6% / 0.8%      1.2-4.2%

CMD-2  $\sim 9 \cdot 10^5$  ev.

SND  $\sim 8 \cdot 10^5$  ev.



Systematic error  
 3.2%      1.3%      8

*Good agreement between the two spectra*

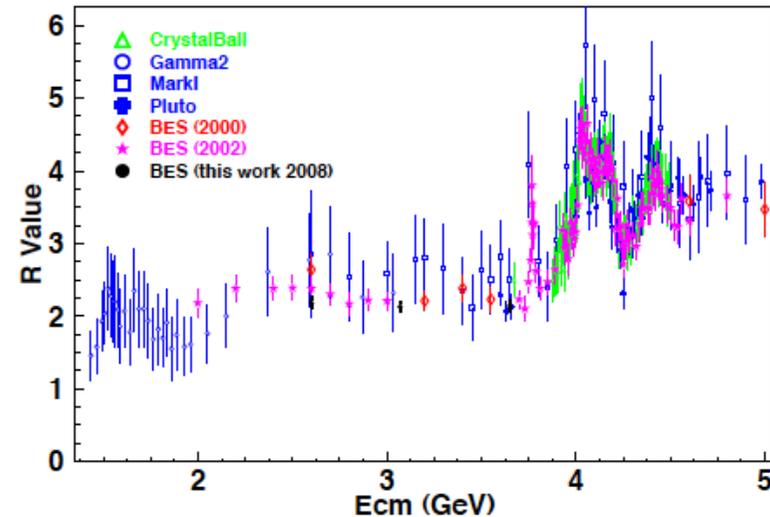
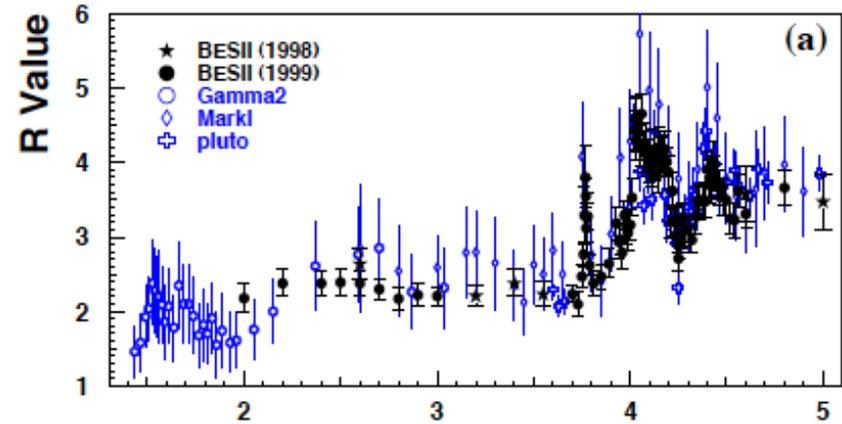
# R measurement at BESII

- BESII @ BEPC, Beijing (inclusive measurement)  $2 < E_{cm} < 5 \text{ GeV}$ 
  - 1998/99 new result of R in  $2 < E_{cm} < 5 \text{ GeV}$  from BESII, 91 points with  $\sigma_R/R \sim 7\%$  (improvement of a factor 2)
  - 2008: 3 points (2.6, 3.07 and 3.65 GeV) with 3.5% precision

$$R = \frac{N_{had}^{obs} - N_{bg} - \sum_l N_{ll} - N_{\gamma\gamma}}{\sigma_{\mu\mu}^0 \cdot L \cdot \epsilon_{trg} \cdot \bar{\epsilon}_{had} \cdot (1 + \delta)},$$

TABLE II. Contributions to systematic errors: experimental selection of hadronic events, luminosity determination, theoretical modeling of hadronic events, trigger efficiency, radiative corrections and total systematic error. All errors are in percentages (%).

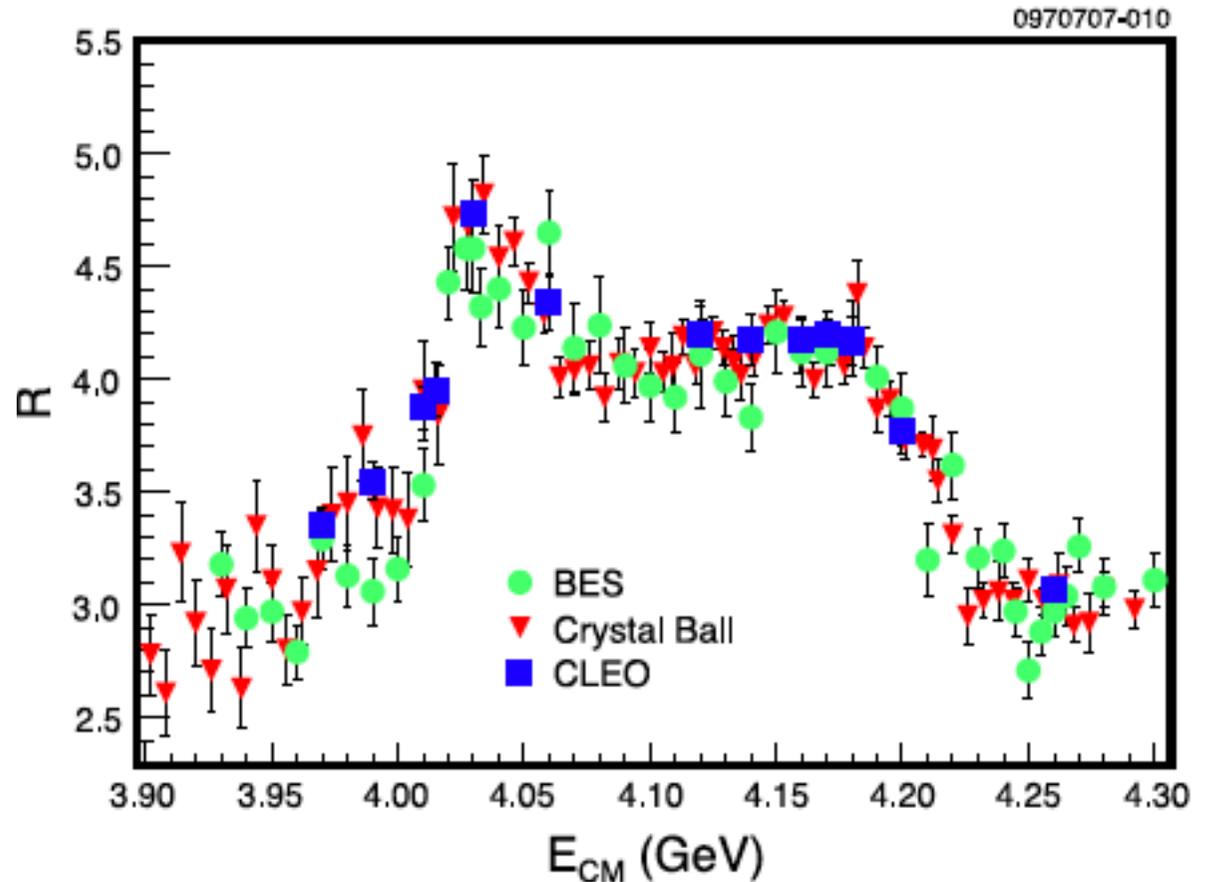
$E_{cm}$ (GeV)	hadron selection	$L$	M.C. modeling	trigger	radiative correction	total
2.000	7.07	2.81	2.62	0.5	1.06	8.13
3.000	3.30	2.30	2.66	0.5	1.32	5.02
4.000	2.64	2.43	2.25	0.5	1.82	4.64
4.800	3.58	1.74	3.05	0.5	1.02	5.14



# R measurement at CLEO

- CLEO@ CESR, Ithaca (inclusive measurement)  $3.9 < E_{cm} < 4.3 \text{ GeV}$ 
  - New result on R (inclusive measurement) in  $3.97 < E_{cm} < 4.26 \text{ GeV}$  (above the open charm threshold) with a  $\delta_{sys}$  between 5.2 and 6.1%. In agreement with the sum of exclusive measurement and previous experiments

Energy (MeV)	$R$ (ISR-corrected)
3970	$3.36 \pm 0.04 \pm 0.05$
3990	$3.55 \pm 0.05 \pm 0.06$
4010	$3.88 \pm 0.04 \pm 0.08$
4015	$3.95 \pm 0.08 \pm 0.08$
4030	$4.74 \pm 0.07 \pm 0.12$
4060	$4.34 \pm 0.05 \pm 0.10$
4120	$4.21 \pm 0.06 \pm 0.10$
4140	$4.18 \pm 0.04 \pm 0.10$
4160	$4.18 \pm 0.03 \pm 0.10$
4170	$4.20 \pm 0.01 \pm 0.10$
4180	$4.17 \pm 0.04 \pm 0.10$
4200	$3.77 \pm 0.05 \pm 0.08$
4260	$3.06 \pm 0.02 \pm 0.04$



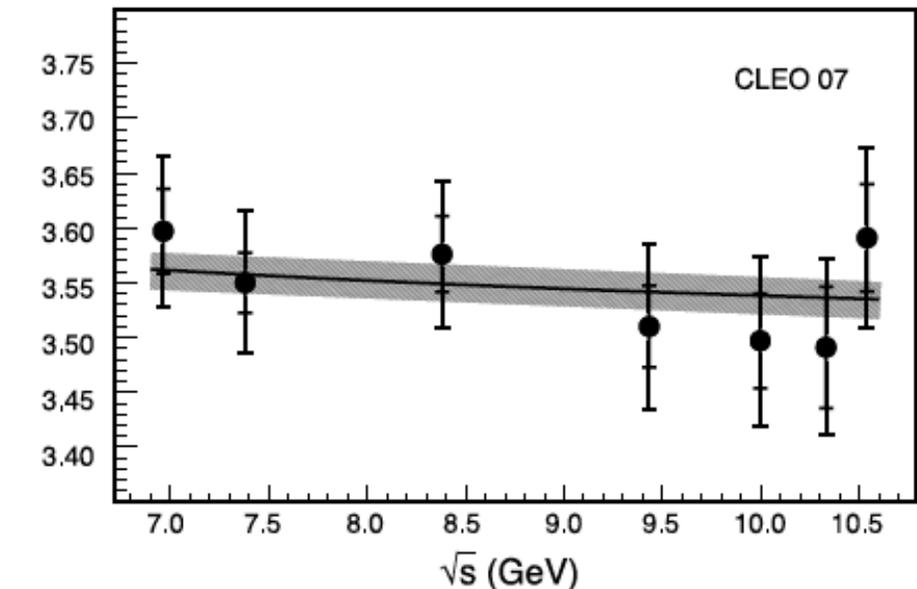
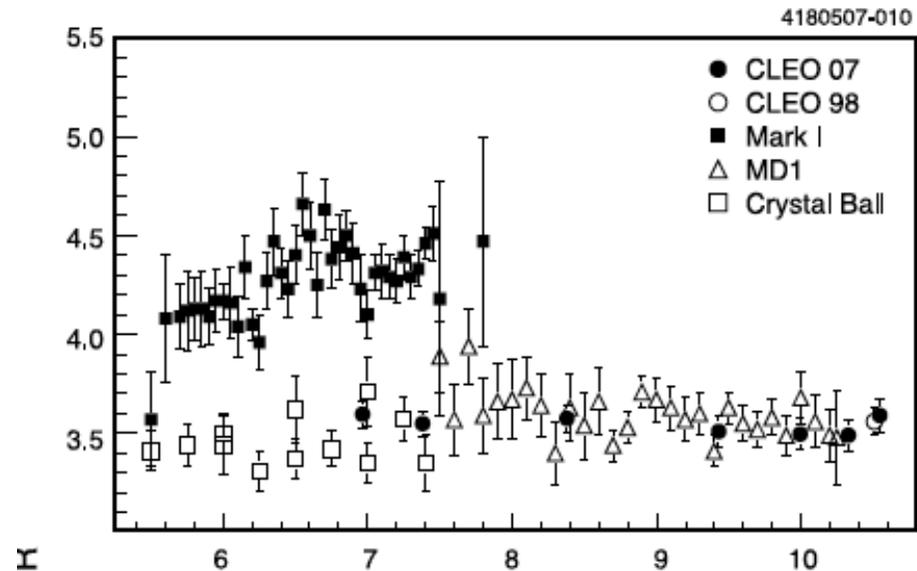
# R measurement at CLEO

• CLEO@ CESR, Ithaca (inclusive measurement)  $6.9 < E_{cm} < 10.5 \text{ GeV}$

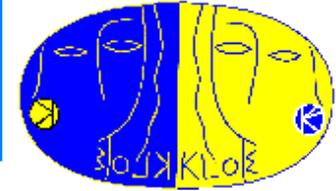
- New result on R (inclusive measurement) in  $6.964 < E_{cm} < 10.538 \text{ GeV}$  (7 points) with a  $\delta_{\text{sys}}$  of  $\sim 2\%$ . In agreement with previous experiments (but MARKI) and pQCD ( $\Lambda=0.31 \text{ GeV}$ )

$$R = \frac{N_{had}(1 - f)}{\mathcal{L}\epsilon_{had}(1 + \delta)\sigma_{\mu\mu}^0},$$

$\epsilon(1+\delta)$	1%
L	1%
Bckg/Hadr Modeling	0.7%
Dataset variation	0.3%
<b>TOTAL</b>	<b>1.8%</b>

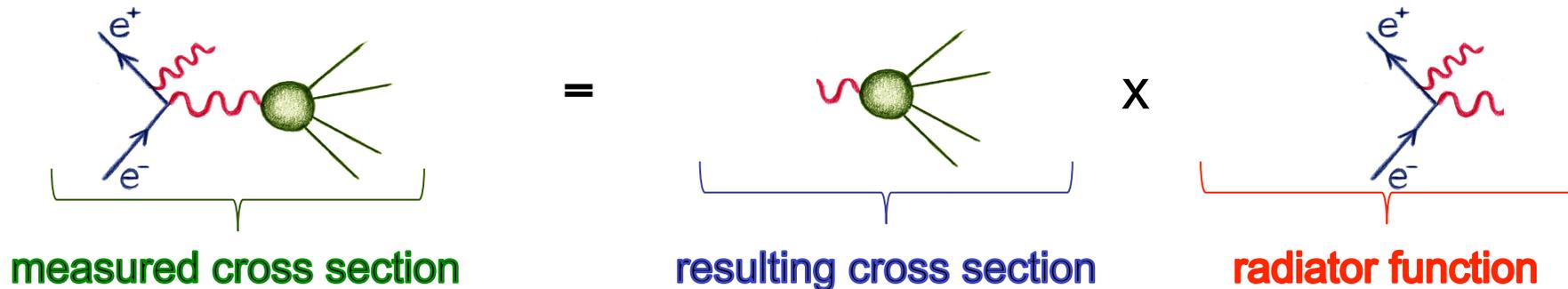


# ISR: Initial State Radiation



Neglecting final state radiation (FSR):

$$\frac{d\sigma(e^+ e^- \rightarrow \text{hadrons} + \gamma)}{dM^2_{\text{hadr}}} = \frac{\sigma(e^+ e^- \rightarrow \text{hadrons}, M^2_{\text{hadr}})}{s} H(s, M^2_{\text{hadr}})$$



**Theoretical input:** precise calculation of the radiation function  $H(s, M^2_{\text{hadr}})$

→ **EVA + PHOKHARA MC Generator**

Binner, Kühn, Melnikov; Phys. Lett. B 459, 1999

H. Czyż, A. Grzebińska, J.H. Kühn, G. Rodrigo, Eur. Phys. J. C 27, 2003

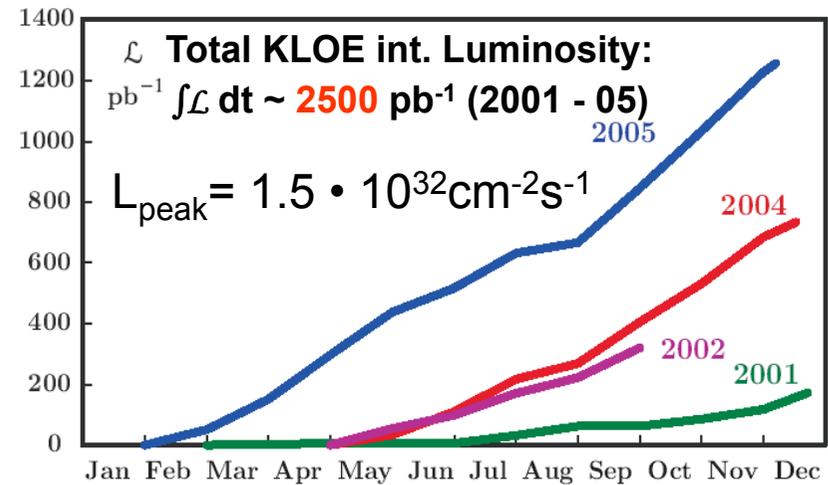
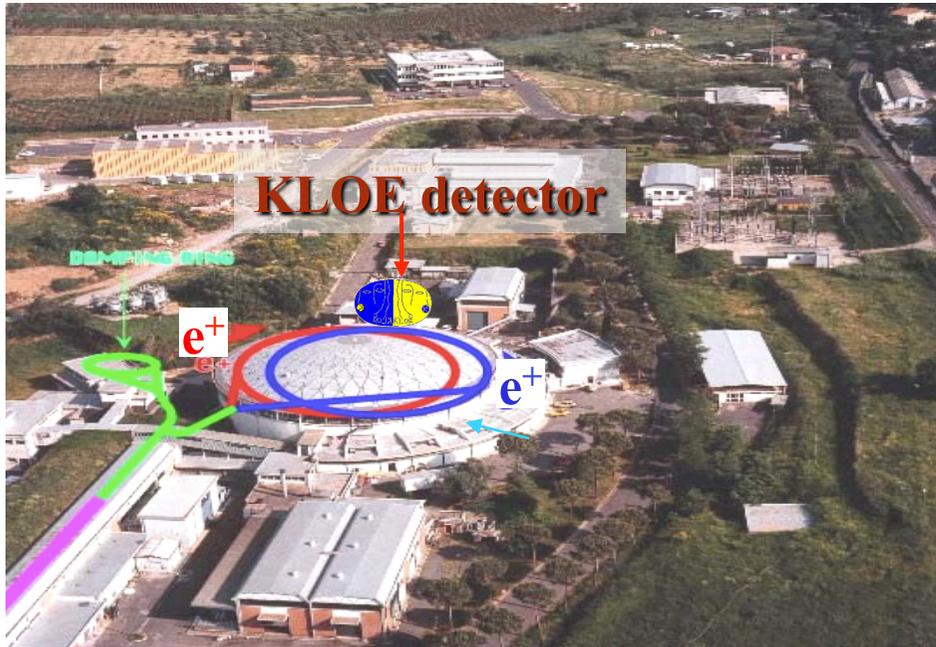
(exact next-to-leading order QED calculation of the radiator function)

**IN 2005 KLOE has published the first precision measurement of  $\sigma(e^+e^- \rightarrow \pi^+\pi^-)$  with ISR using 2001 data ( $140\text{pb}^{-1}$ ) PLB606(2005)12  $\Rightarrow \sim 3\sigma$  discrepancy btw  $a_\mu^{\text{SM}}$  and  $a_\mu^{\text{exp}}$**

# DAΦNE: A Φ-Factory in Frascati (near Rome)

$e^+e^-$  - collider with  $\sqrt{s}=m_\Phi \approx 1.0195$  GeV

*Integrated Luminosity*



**2006**

- Energy scan (4 points around  $m_\Phi$ -peak)
- **240 pb<sup>-1</sup> at  $\sqrt{s} = 1000$  MeV (off-peak data)**

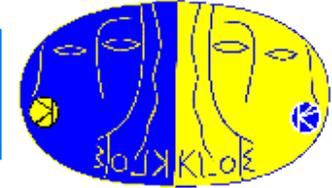
**KLOE05 measurement (PLB606 (2005)12 ) was based on 140pb<sup>-1</sup> of 2001 data!**

**KLOE10 measurement (PLB700 (2011) 102) based on 233 pb<sup>-1</sup> of 2006 data (at 1 GeV, different event selection)**

**KLOE08 measurement (PLB670 (2009)285) was based on 240pb<sup>-1</sup> from 2002 data!**

**NEW: KLOE12 measurement (submitted to PLB) based on 240 pb<sup>-1</sup> of 2002 data from  $\pi\pi\gamma/\mu\mu\gamma$  ratio**

# KLOE result (KLOE08)



Systematic errors on  $a_{\mu}^{\text{pp}}$ :

Reconstruction Filter	negligible
Background	0.3%
Trackmass/Miss. Mass	0.2%
p/e-ID and TCA	negligible
Tracking	0.3%
Trigger	0.1%
Acceptance ( $\mathbb{W}_{\pi\pi}$ )	0.1%
Acceptance ( $\mathbb{W}_{\mathbb{W}}$ )	negligible
Unfolding	negligible
Software Trigger	0.1%
$\sqrt{s}$ dep. Of H	0.2%
Luminosity( $0.1_{\text{th}} \oplus 0.3_{\text{exp}}$ )%	0.3%

**experimental fractional error on  $a_{\mu} = 0.6\%$**

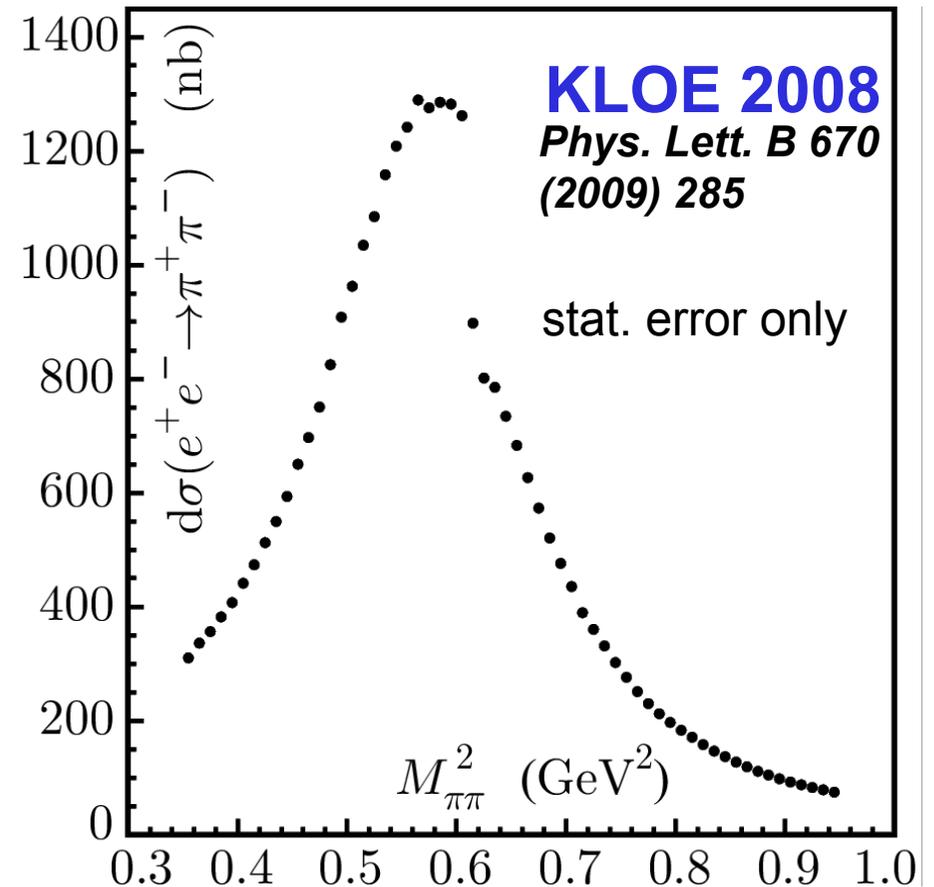
FSR resummation	0.3%
Radiator H	0.5%
Vacuum polarization	0.1%

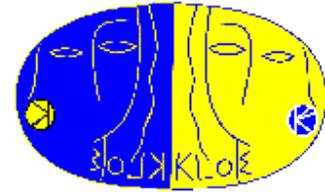
**theoretical fractional error on  $a_{\mu} = 0.6\%$**

$$a_{\mu}^{\pi\pi} = \int_{x_1}^{x_2} \sigma_{ee \rightarrow \pi\pi}(s) K(s) ds$$

$$a_{\mu}^{\pi\pi}(0.35-0.95\text{GeV}^2) = (387.2 \pm 0.5_{\text{stat}} \pm 2.4_{\text{sys}} \pm 2.3_{\text{theo}}) \cdot 10^{-10}$$

$\sigma_{\pi\pi}$ , undressed from VP, inclusive for FSR as function of  $(M_{\pi\pi}^0)^2$





# KLOE10 result: Pion Form Factor

arXiv:1006.5313

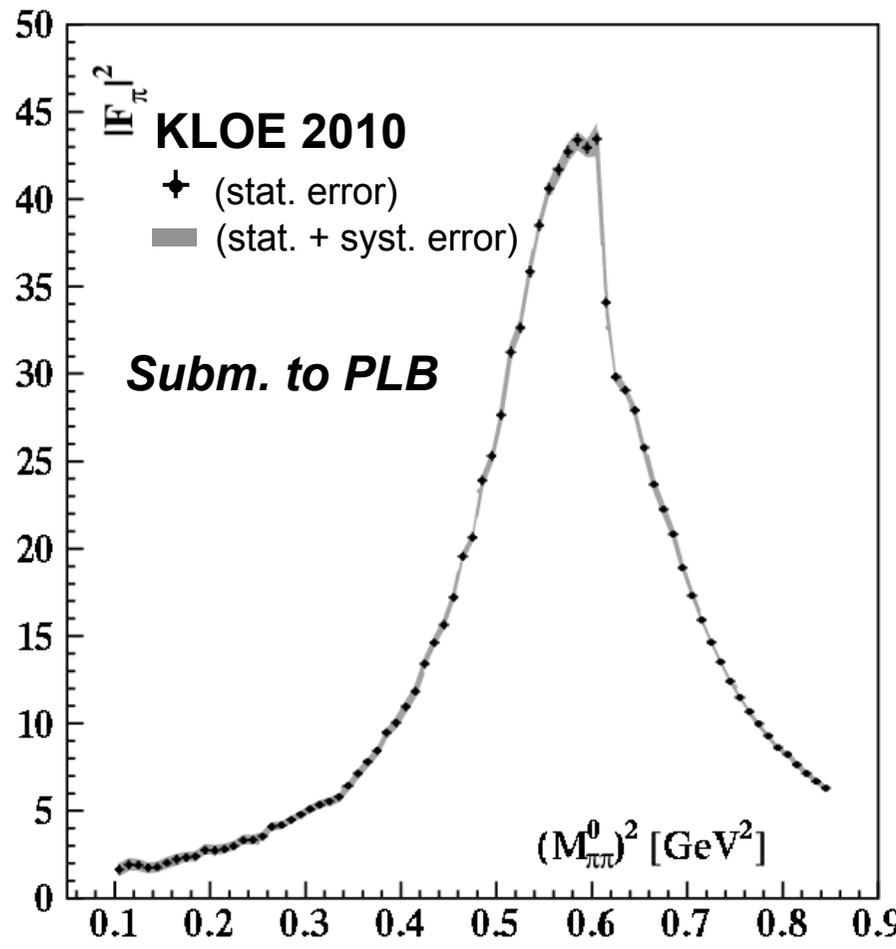


Table of systematic errors on  $a_\mu^{pp}(0.1-0.85 \text{ GeV}^2)$ :

Reconstruction Filter	< 0.1%
Background	0.5%
$f_0+rp$	0.4%
Omega	0.2%
Trackmass	0.5%
p/e-ID and TCA	< 0.1%
Tracking	0.3%
Trigger	0.2%
Acceptance	0.4%
Unfolding	negligible
Software Trigger	0.1%
Luminosity( $0.1_{th} \oplus 0.3_{exp}$ )%	0.3%

experimental fractional error on  $a_\mu = 1.0 \%$

FSR resummation	0.3%
Radiator H	0.5%
Vacuum polarization	< 0.1%

theoretical fractional error on  $a_\mu = 0.6 \%$

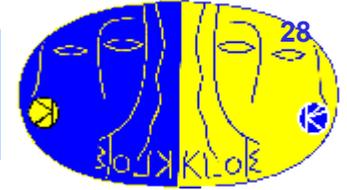
Disp. Integral:

$$a_\mu^{\pi\pi} = \int_{x_1}^{x_2} \sigma_{ee \rightarrow \pi\pi}(s) K(s) ds$$

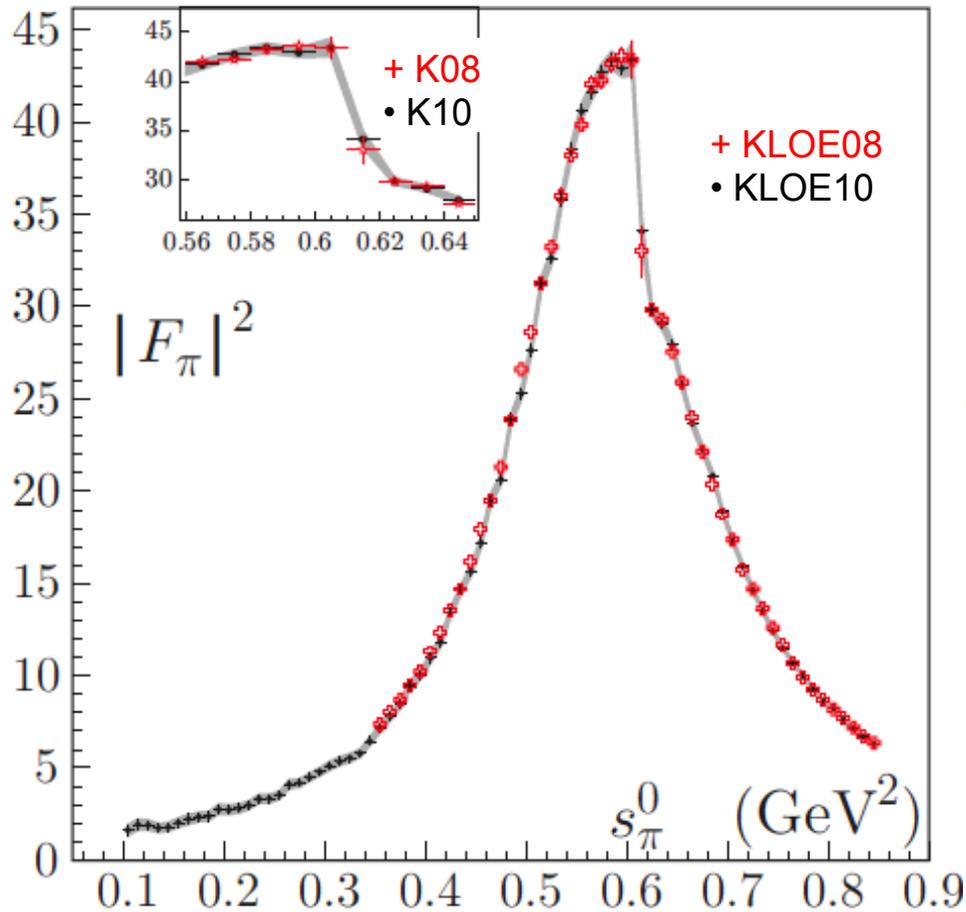
$$a_\mu^{\pi\pi}(0.1-0.85 \text{ GeV}^2) = (478.5 \pm 2.0_{\text{stat}} \pm 4.8_{\text{sys}} \pm 2.9_{\text{theo}}) \cdot 10^{-10}$$

0.4%    1.0%    0.6%

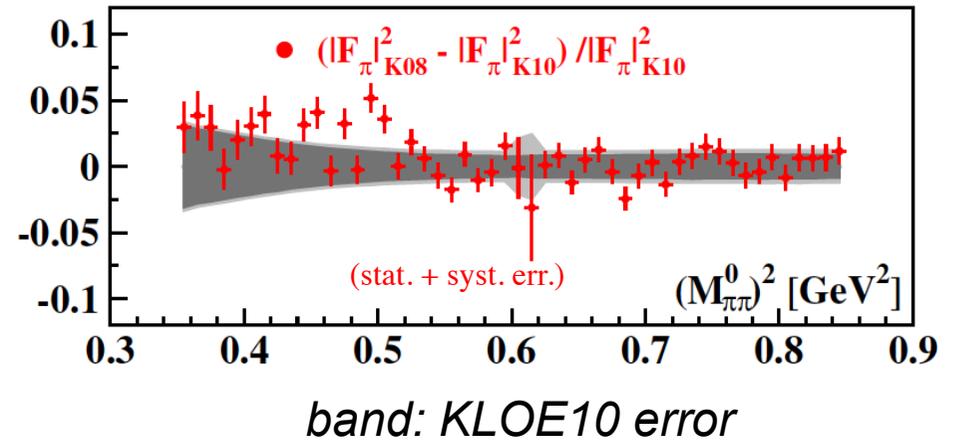
# Comparison of results: KLOE10 vs KLOE08



KLOE08 result compared to KLOE10:



Fractional difference:

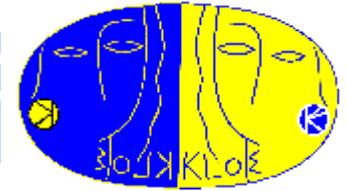


Excellent agreement with KLOE08, especially above 0.5 GeV<sup>2</sup>

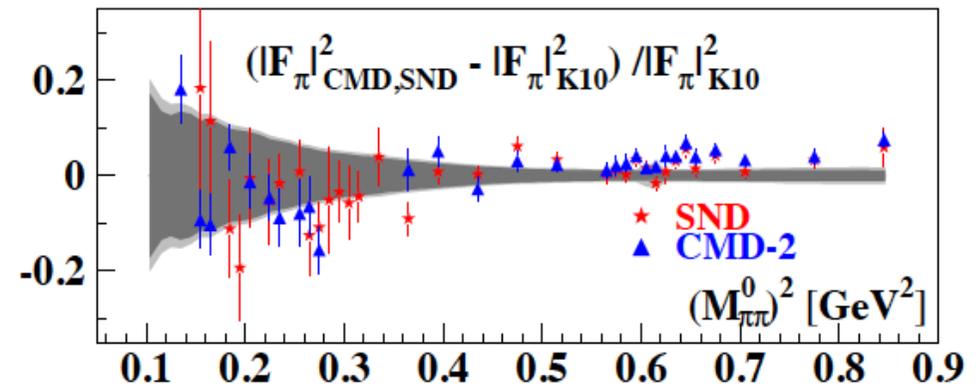
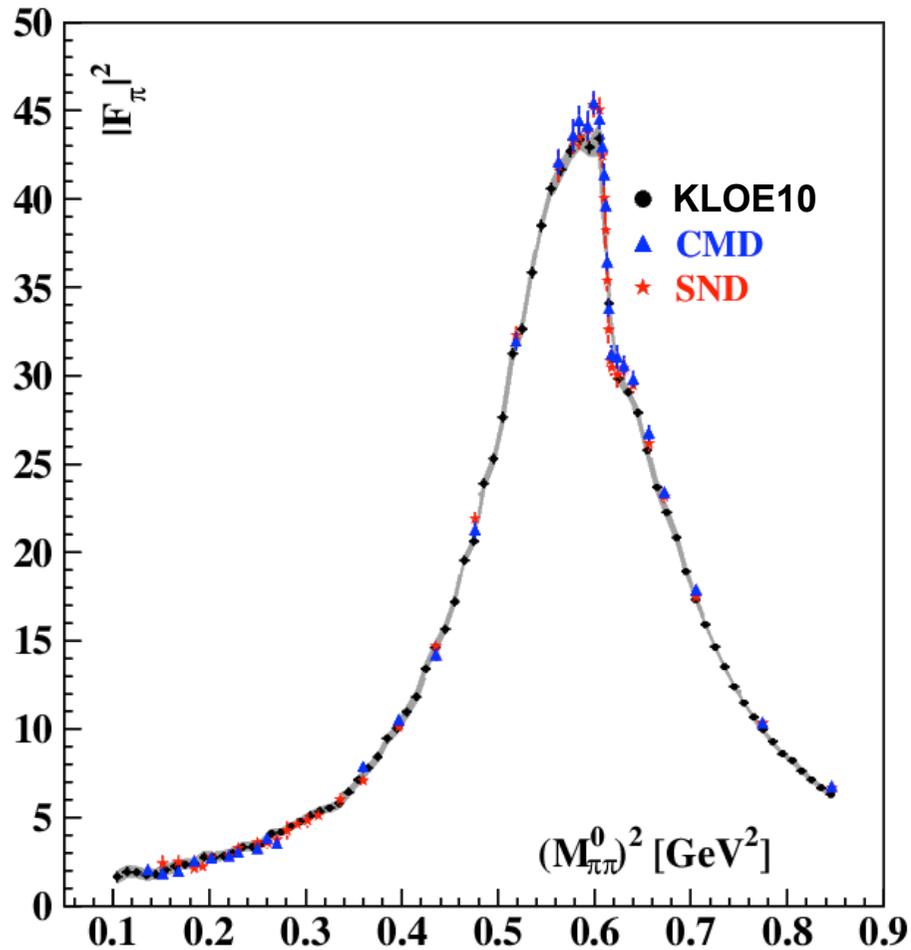
Combination of KLOE08 and KLOE10:  
 $a_\mu^{\pi\pi}(0.1-0.95 \text{ GeV}^2) = (488.6 \pm 5.0) \cdot 10^{-10}$

KLOE covers  $\sim 70\%$  of total  $a_\mu^{\text{HLO}}$  with a fractional error of 1.0%

# Comparison of results: KLOE10 vs CMD-2/SND



CMD and SND results compared to KLOE10: Fractional difference

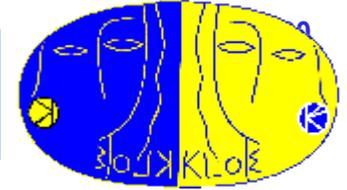


band: KLOE10 error

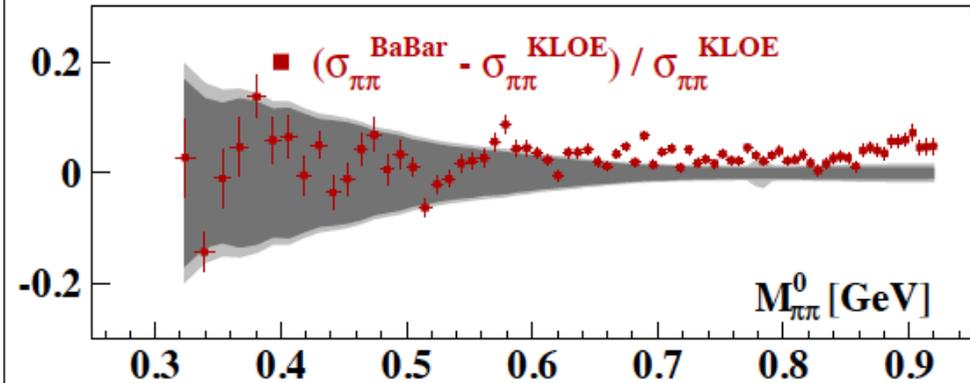
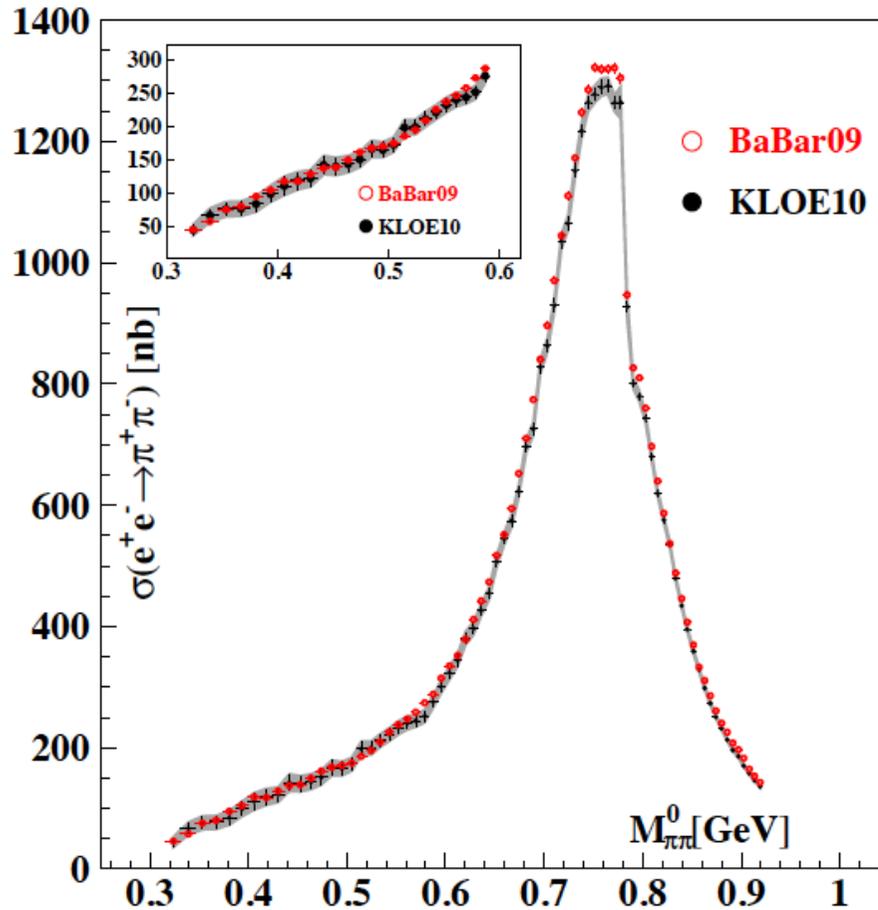
*Below the  $\rho$  peak good agreement with CMD-2/SND.*

*Above the  $\rho$  peak KLOE10 slightly lower (as KLOE08)*

# Comparison of results: KLOE10 vs BaBar



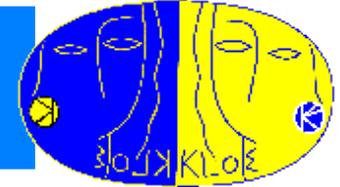
BaBar results compared to KLOE10: Fractional difference



band: KLOE10 error

Agreement within errors below 0.6 GeV; BaBar higher by 2-3% above

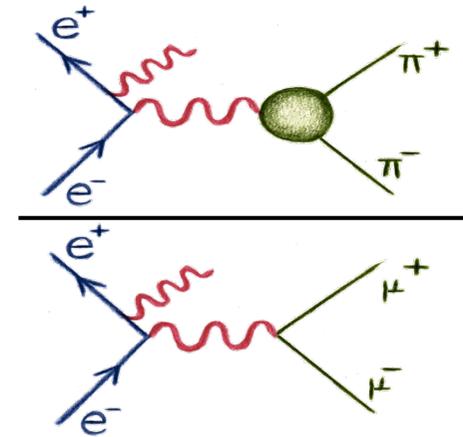
# New $\sigma_{\pi\pi}$ measurement from $\pi\pi\gamma/\mu\mu\gamma$



An alternative way to obtain  $|F_\pi|^2$  is the bin-by-bin ratio of pion over muon yields (instead of using absolute normalization with Bhabhas).

$$|F_\pi(s')|^2 \approx \underbrace{\frac{4(1 + 2m_\mu^2/s')\beta_\mu}{\beta_\pi^3}}_{\text{kinematical factor}} \underbrace{\frac{d\sigma_{\pi\pi\gamma}/ds'}{d\sigma_{\mu\mu\gamma}/ds'}}_{\text{meas. quantities}}$$

$(s_{\text{mm}}^{\text{Born}} / s_{\text{pp}}^{\text{Born}})$



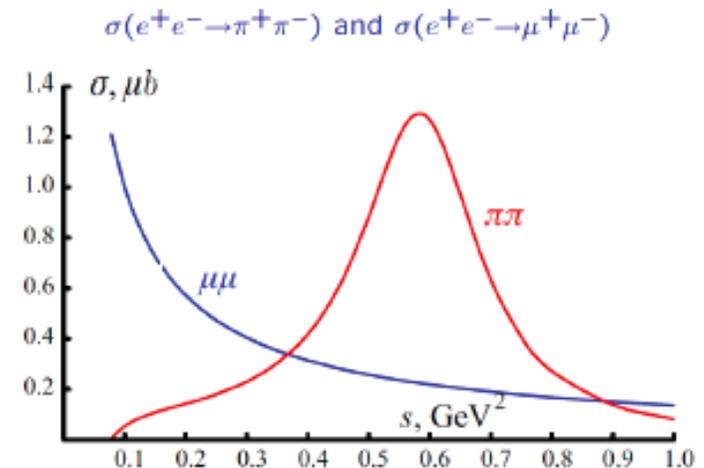
Many radiative corrections drop out:

- radiator function
- int. luminosity from Bhabhas
- Vacuum polarization

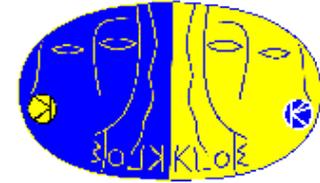
Separation btw  $\pi\pi\gamma$  and  $\mu\mu\gamma$  using  $M_{\text{TRK}}$

- muons:  $M_{\text{Trk}} < 115 \text{ MeV}$
- pions:  $M_{\text{Trk}} > 130 \text{ MeV}$

Very important control of  $\pi/\mu$  separation in the  $\rho$  region! ( $\sigma_{\pi\pi} \gg \sigma_{\mu\mu}$ )



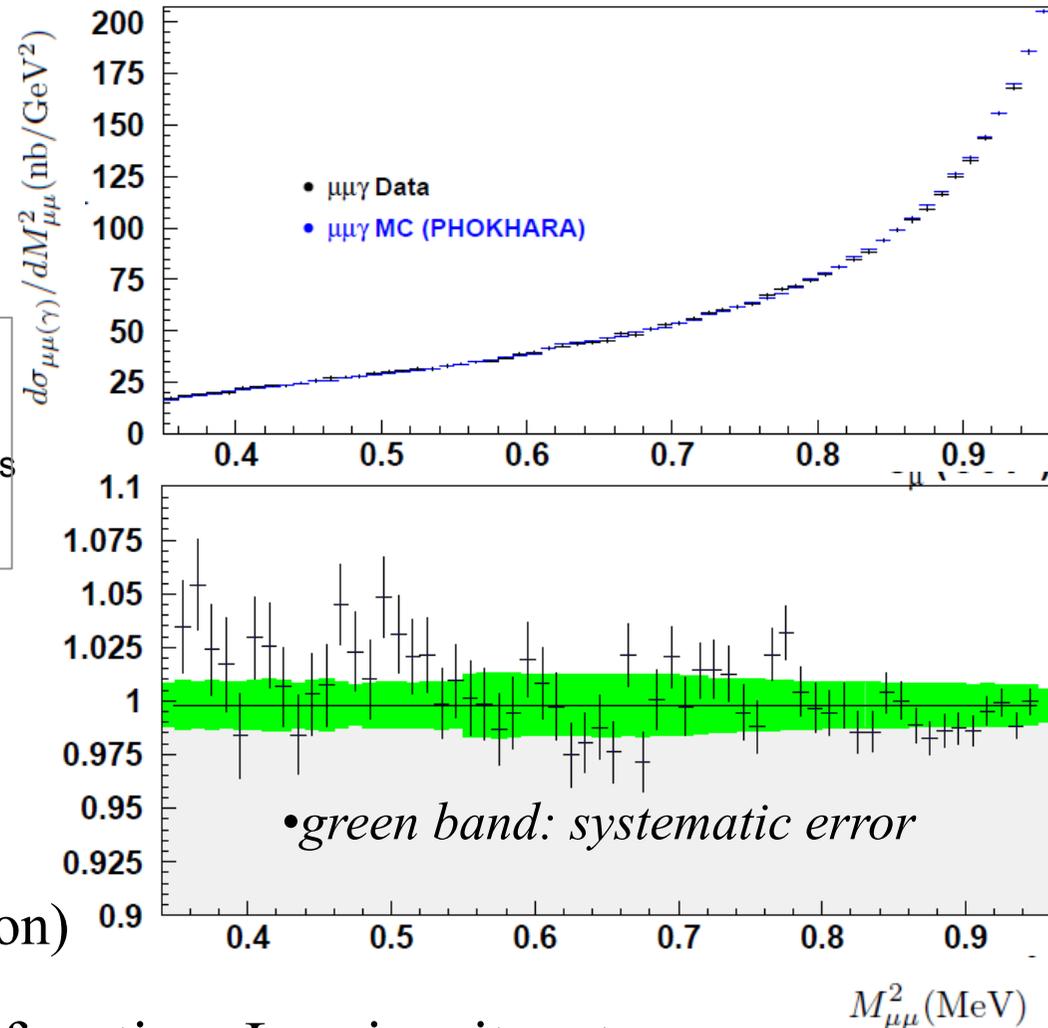
# $\mu\mu\gamma$ cross section: data/MC comparison



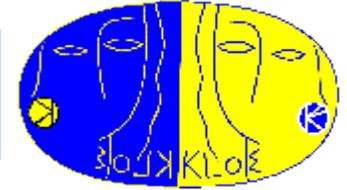
$$\frac{d\sigma_{\mu\mu(\gamma)}^{obs}}{dM_{\mu\mu}^2} = \frac{\Delta N_{Obs} - \Delta N_{Bkg}}{\Delta M_{\mu\mu}^2} \cdot \frac{1}{\epsilon_{Sel}} \cdot \frac{1}{\int L dt}$$

$$\frac{d\sigma_{\mu\mu(\gamma)}^{DATA}}{d\sigma_{\mu\mu(\gamma)}^{MC}} = 0.998 \pm 0.001_{stat} \pm 0.011_{sys}$$

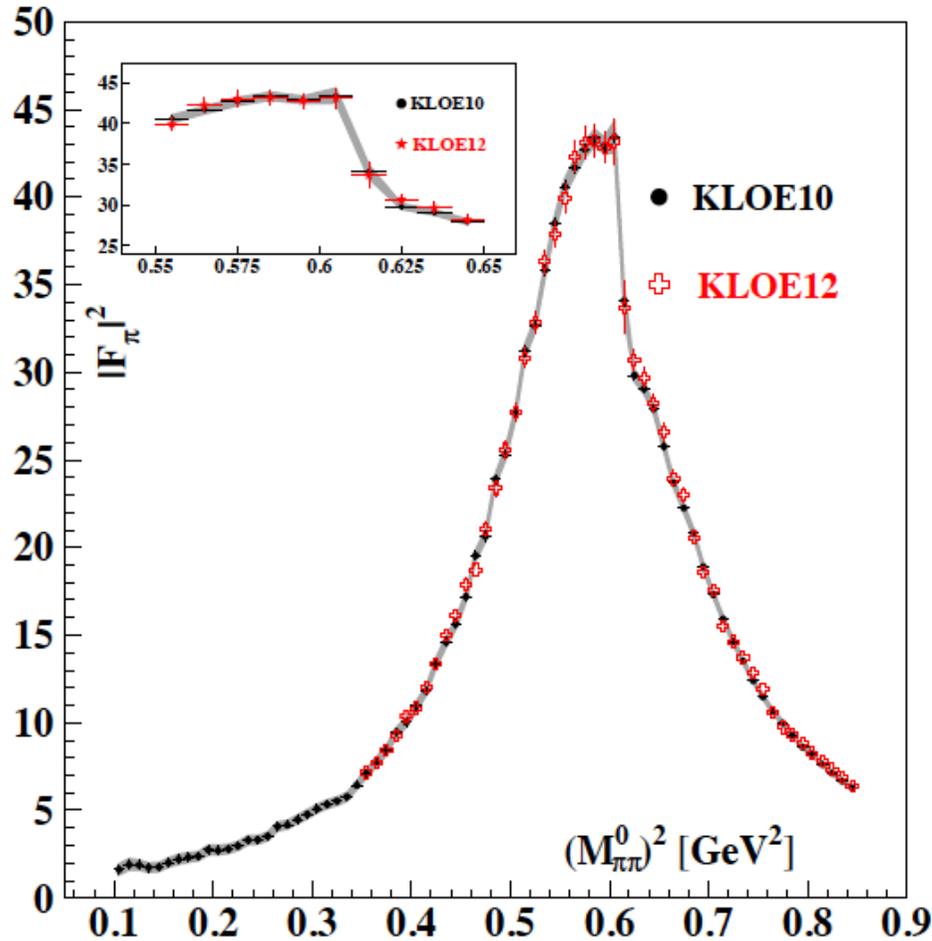
- The systematic error has been averaged on  $M_{\mu\mu}^2$
- Good agreement with PHOKHARA MC (NLO Calculation)
- Consistency check of Radiator function, Luminosity, etc...



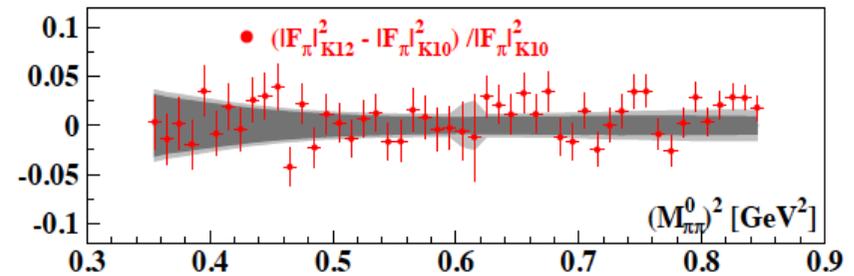
# Comparison of results: KLOE12 vs KLOE10



KLOE12 result compared to KLOE10:



Fractional difference:



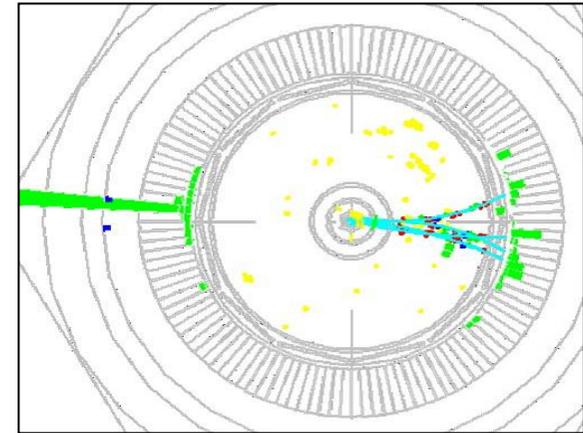
*band: KLOE10 error*

**Excellent agreement between the two independent measurements!**

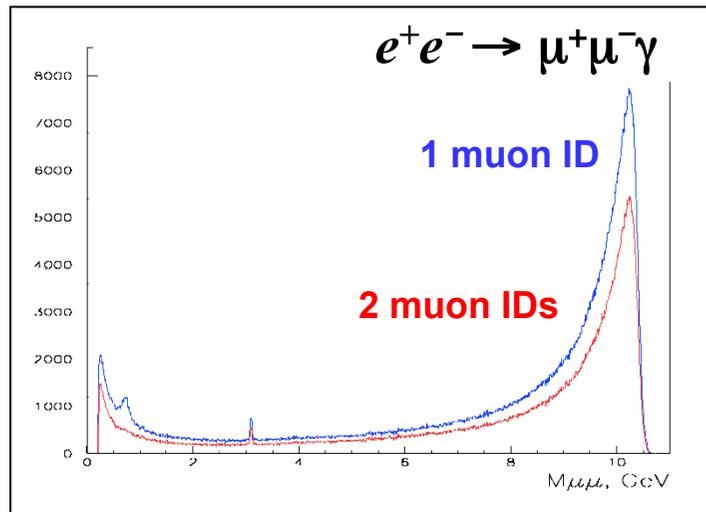
Analysis	$a_\mu^{\pi\pi}(0.35 - 0.85 \text{ GeV}^2) \times 10^{10}$
KLOE12	$377.4 \pm 1.1_{\text{stat}} \pm 2.7_{\text{sys+theo}}$
KLOE10	$376.6 \pm 0.9_{\text{stat}} \pm 3.3_{\text{sys+theo}}$

# BABAR results on R using ISR:

- Center-of-mass energy of machine PEP-II ( $\sqrt{s}=m_{\Upsilon(4s)}=10.6$  GeV) far from mass range of interest (ca.  $< 4$  GeV)
  - requires **high energy photon**  $E_{\gamma}^*=(3 - 5.3)$  GeV
  - requires **high integrated luminosity** of PEP-II
- Hard **ISR-photon back-to-back to hadrons**
  - only acceptance for large angle photons
  - **photon tagging!**



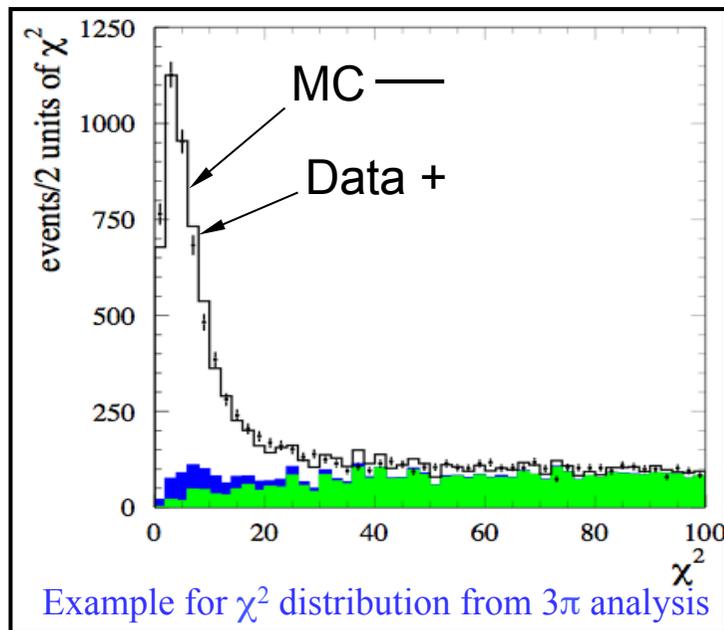
Event-Display of an ISR-Event in transversal plane



- **Normalisation:**
  - to integrated luminosity and radiator function (not for  $2\pi$  mode)
  - to radiative muon pairs, which are selected with high precision (for  $2\pi$  mode)

# BABAR results on R using ISR:

- Mass resolution of hadronic system **improved by means of a kinematic fit**
  - Input to the fit: Momentum and direction of ISR-photon (not energy!)
  - Constraints: energy and momentum conservation (and  $\pi^0$  mass)



- $\chi^2$ -distribution of kinematic fit is the **main tool for background subtraction**
  - long tail due radiative corrections (NLO)
  - remaining background obtained from MC (for qq events) or from data with sideband technique (for ISR events)

- **Background** from  $\Upsilon(4s)$  and from B-decays is very small ( $E_\gamma > 3$  GeV)
  - main background from **other ISR-events**
  - background from **continuum processes**  $e^+e^- \rightarrow qq$

*From A. Denig, Phipsi06*

# The BaBar ISR program

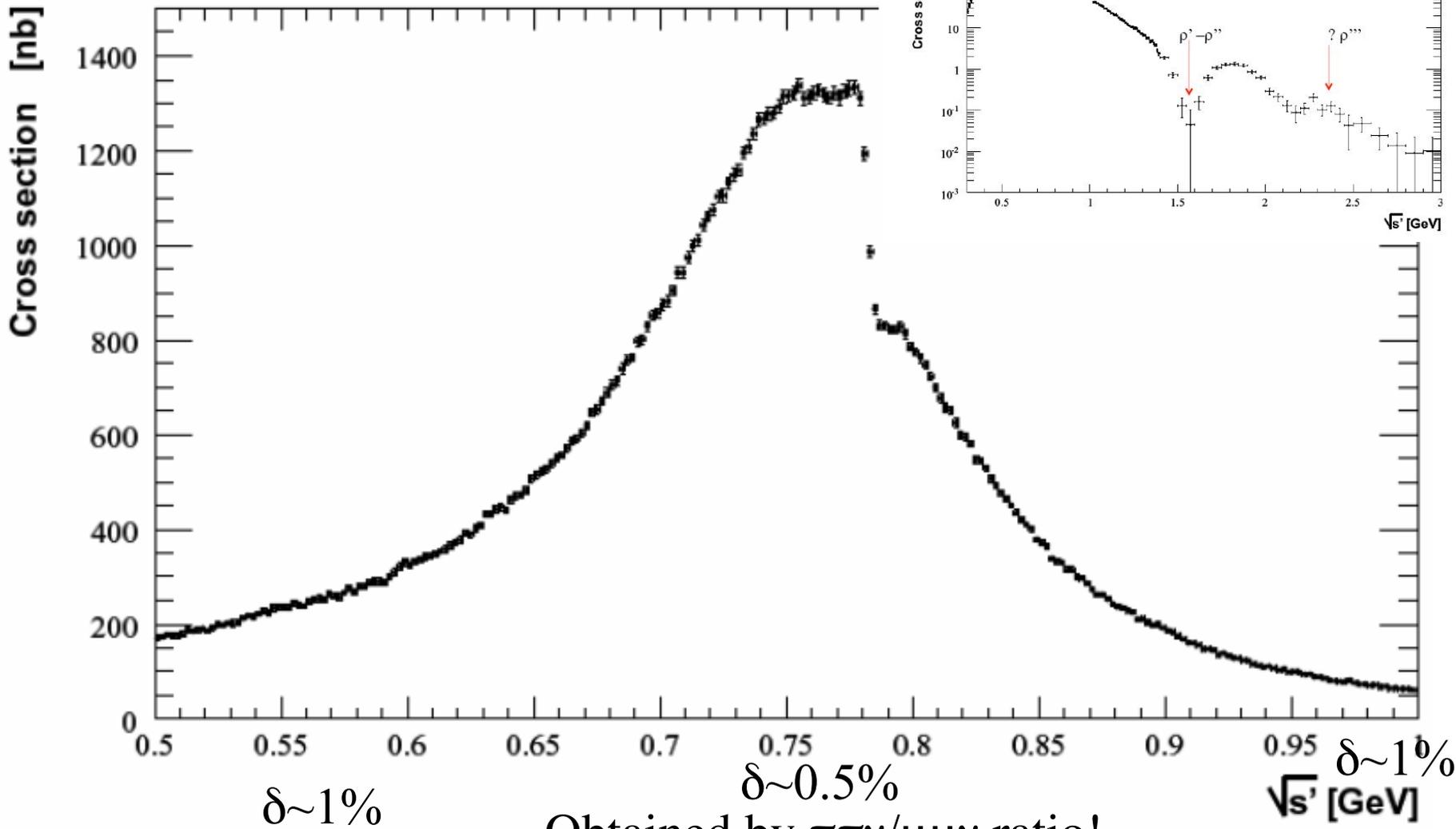
- cover an almost complete set of significant exclusive  $e^+e^-$  annihilation channels up to 2 GeV
- published:
 

$\pi^+\pi^-$	PRL 2009; PRD 2012
$\pi^+\pi^-\pi^0$	PRD 2004
$2(\pi^+\pi^-)$ , $K^+K^-\pi^+\pi^-$ , $K^+K^-2\pi^0$ , $2(K^+K^-)$	PRD 2007; PRD 2012; PRD 2012
$K_S^0 K^+ \pi^-$ , $K^+K^-\pi^0$ , $K^+K^-\eta$	PRD 2005; PRD 2008
$2(\pi^+\pi^-)\pi^0$ , $2(\pi^+\pi^-)\eta$ , $K^+K^-\pi^+\pi^-\pi^0$ , $K^+K^-\pi^+\pi^-\eta$	PRD 2007
$3(\pi^+\pi^-)$ , $2(\pi^+\pi^-\pi^0)$ , $2(\pi^+\pi^-)K^+K^-$	PRD 2006
$\Phi f^0(980)$	PRD 2006; PRD 2007
$\rho \bar{\rho}$	PRD 2006
$\Lambda \Lambda$ , $\Lambda \Sigma^0$ , $\Sigma^0 \Sigma^0$	PRD 2007
- preliminary results at this workshop:
  - $K^+K^-$
- in progress:
  - $\pi^+\pi^-2\pi^0$ ,  $K_S^0 K_L^0$ ,  $K_S^0 K_L^0 \pi^+\pi^-$ ,  $K_S^0 K^+ \pi^+\pi^0$ ,  $K_S^0 K^+ \pi^+\eta$



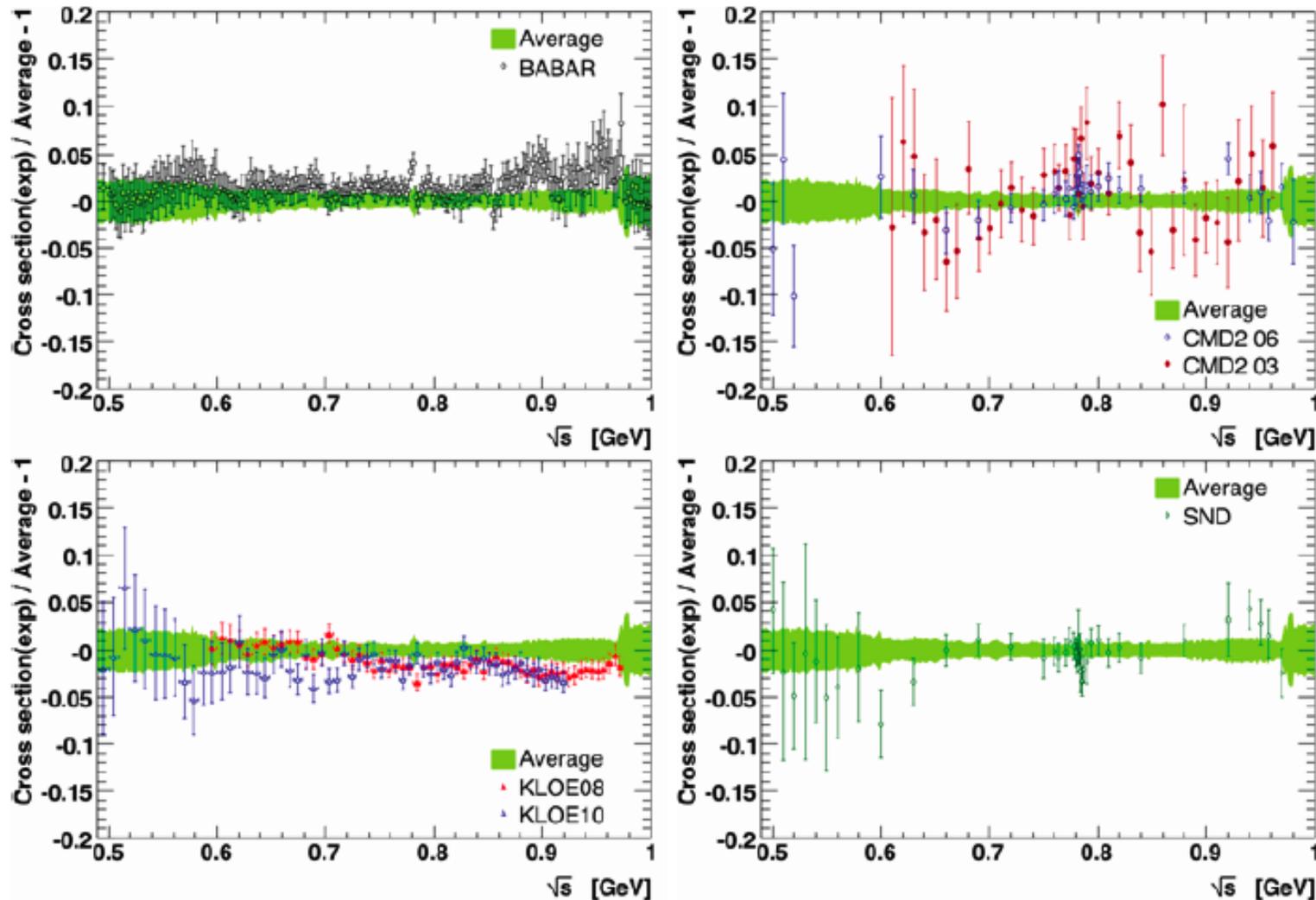
# BaBar results on $e^+e^- \rightarrow \pi^+\pi^-(\gamma)$ using ISR:

BaBar (PRL Dec 2009)



Obtained by  $\pi\pi\gamma/\mu\mu\gamma$  ratio!

# Comparison of input $ee \rightarrow \pi\pi$ data



# ISR: KLOE vs BaBar $2\pi$

## KLOE:

- The photon is “soft” (detected or not)
- No Kinematic fit
- Bin of  $0.01 \text{ GeV}^2$  ( $\sim 8 \text{ MeV}$  at  $\rho$  peak)  $\gg \delta M_{\pi\pi}^2 \sim 2 \cdot 10^{-3} \text{ GeV}^2$   
 $\Rightarrow$  Unfolding only relevant at low  $M_{\pi\pi}^2$  (up to 4%) and at  $\rho$ - $\omega$  cusp,
- Negligible contribution of LO FSR, and  $< 2\%$  contribution of NLO FSR ( $1\gamma_{\text{ISR}} + 1\gamma_{\text{FSR}}$ ) only at low  $M_{\pi\pi}^2$
- Normalize to  $ee(\gamma)$ ,  $\mu\mu\gamma$
- Use **Phokhara** for acceptance, radiator and additional-photon effects

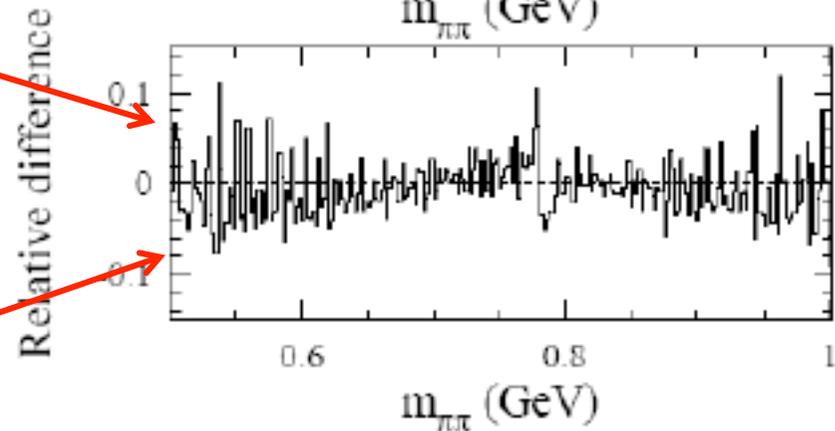
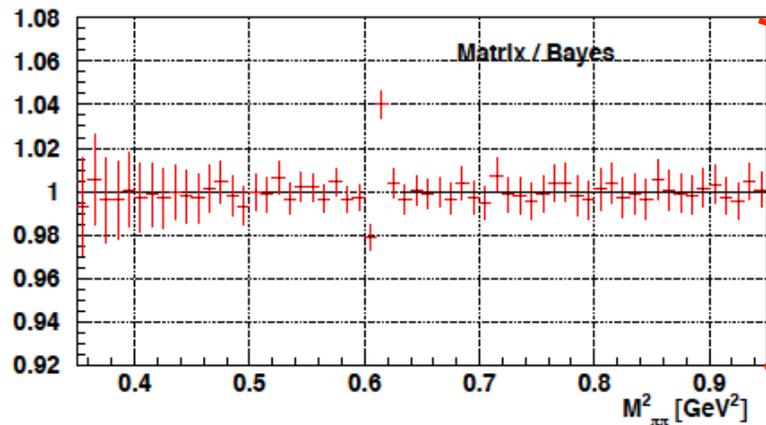
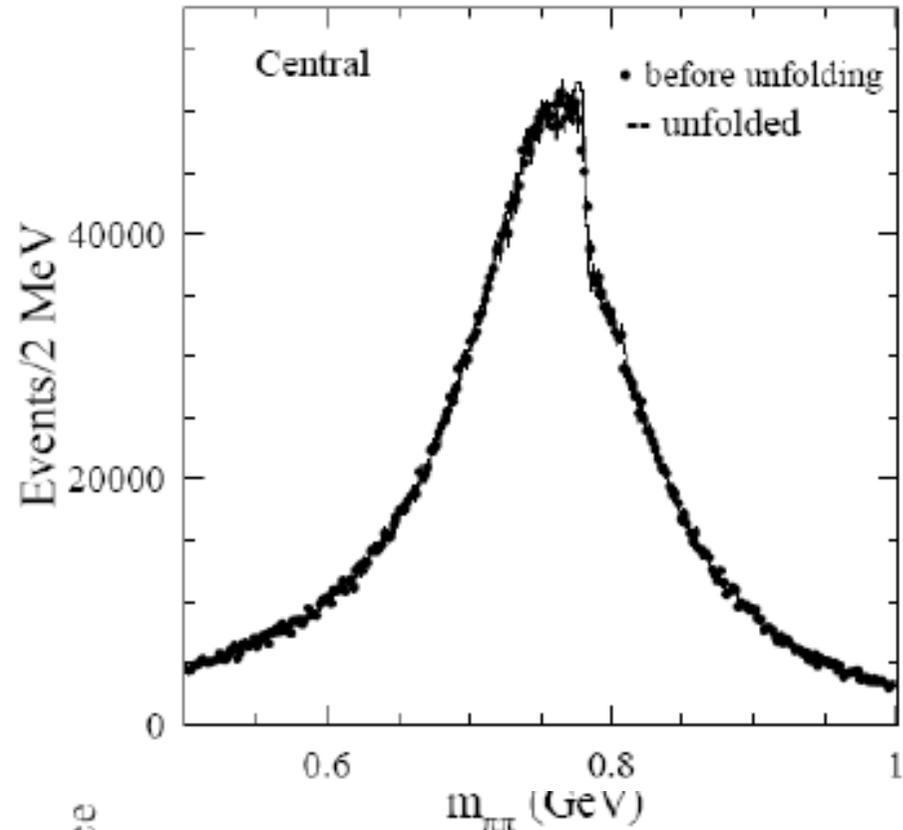
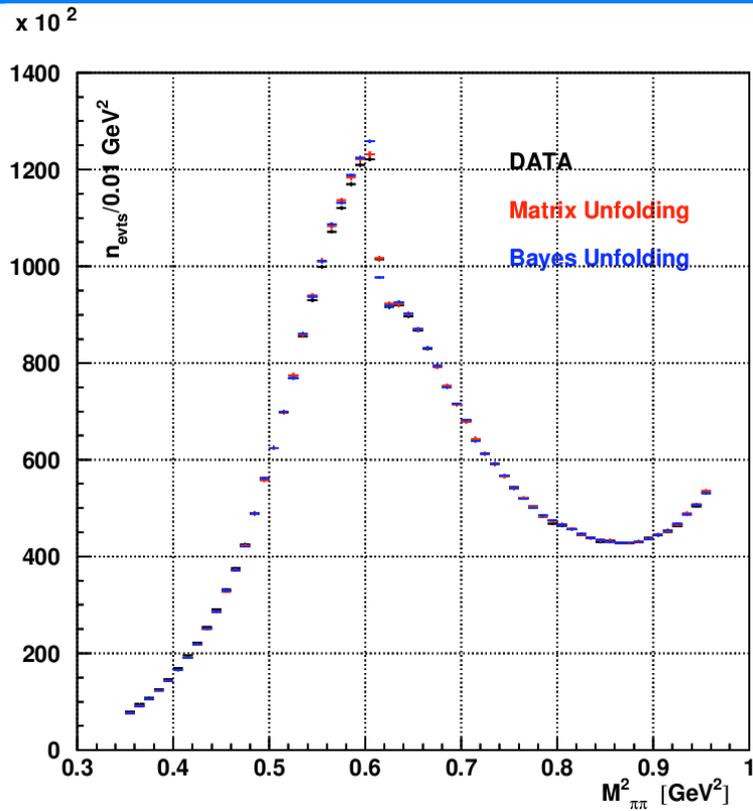
## BaBar:

- The photon is “hard” and detected
- Kinematic fit to improve resolution
- Bin of  $2 \text{ MeV}$  in the region  $0.5$ - $1 \text{ GeV}$   
 $\Rightarrow$  Larger effects on the unfolding
- Negligible contribution of LO FSR, % contribution of NLO FSR ( $1\gamma_{\text{ISR}} + 1\gamma_{\text{FSR}}$ )
- Normalize to  $\mu\mu\gamma$
- Interplay btw **Phokhara** and **AfKQED** to estimate additional-photon effects

**Different selections and use of theoretical ingredients (R.C., Luminosity, Radiator).**

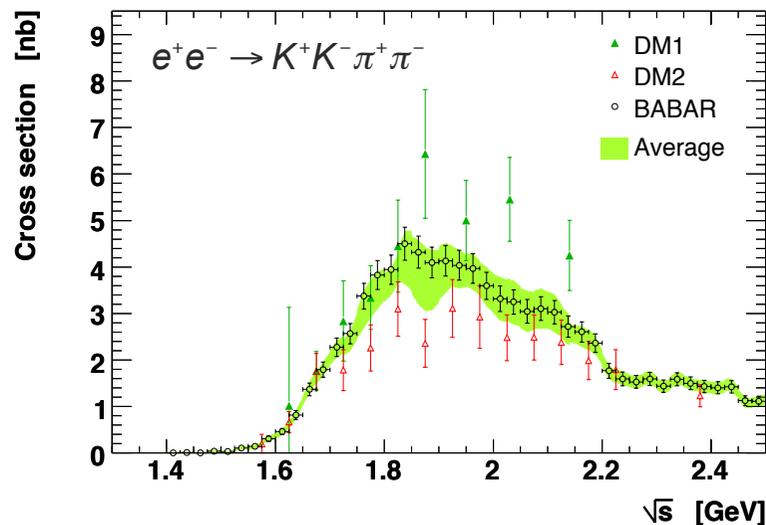
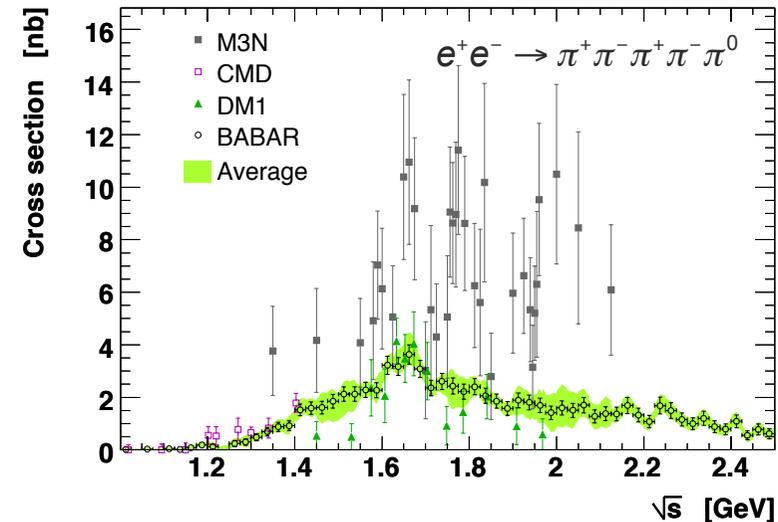
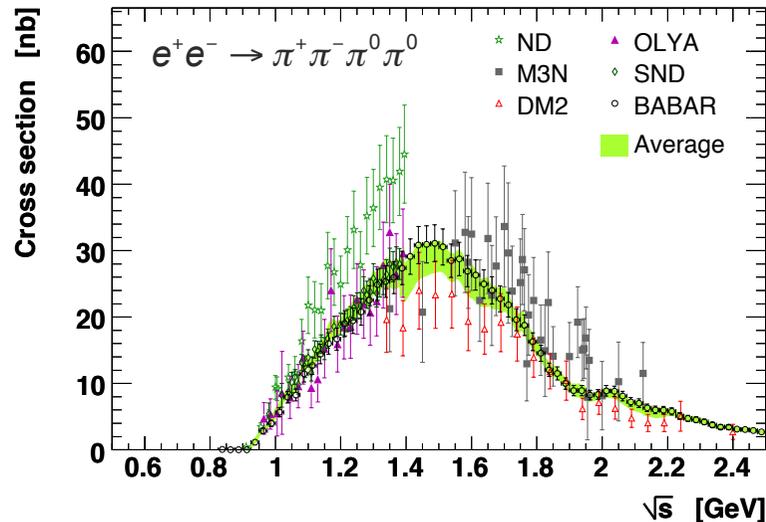
**Additional cross checks are possible (and needed)**

# Unfolding: KLOE vs Babar $2\pi$ :



# Multihadron channels between 1 and 2.5 GeV

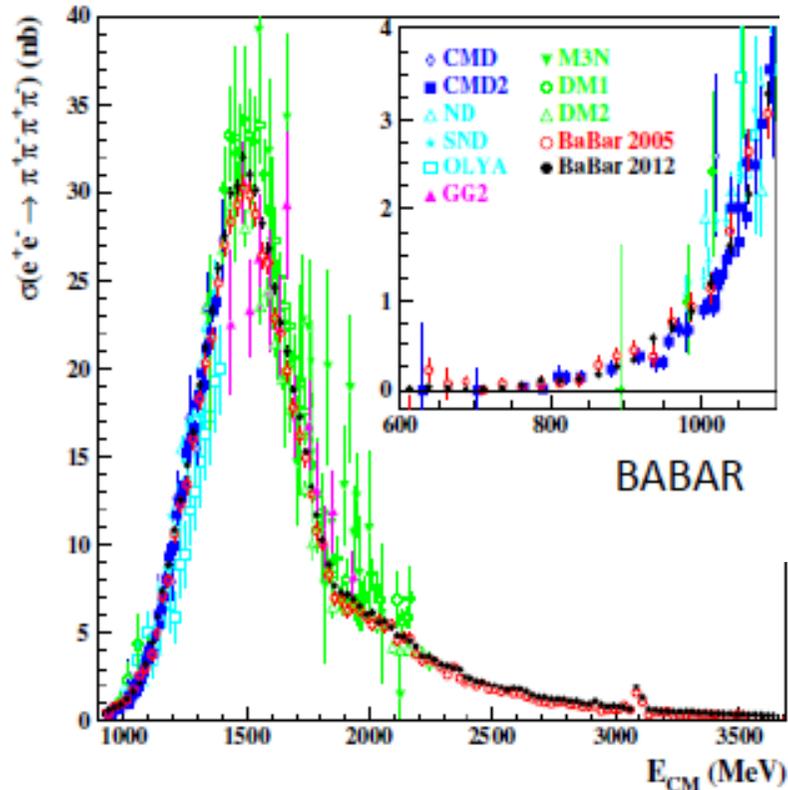
Davier *et al.*, EPJ C 71, 1515 (2011)



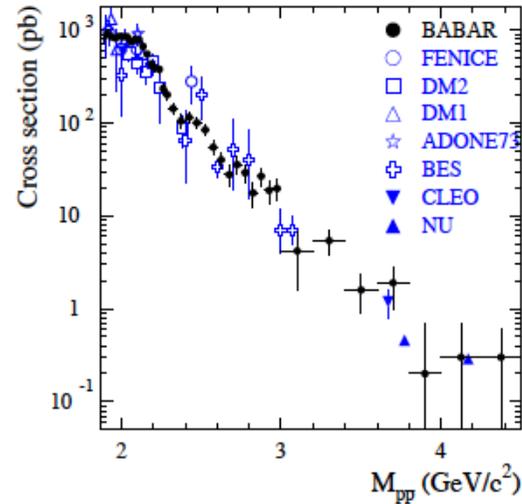
BABAR measured (almost) all the exclusive  $e^+e^- \rightarrow$  hadrons modes  
Many inconsistencies resolved  
Huge impact on hadronic vacuum polarisation calculation

# New cross section results

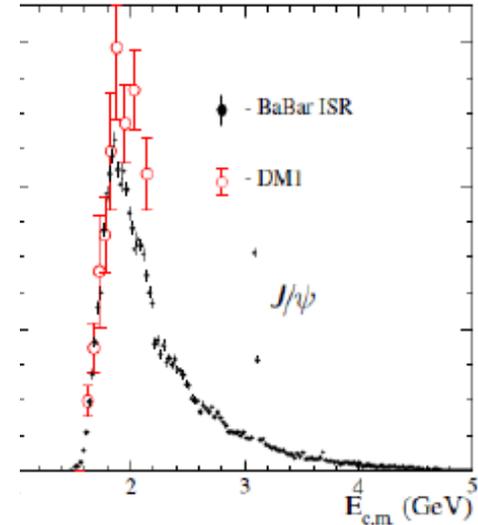
$$e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-(\gamma)$$



$$e^+e^- \rightarrow p\bar{p}$$

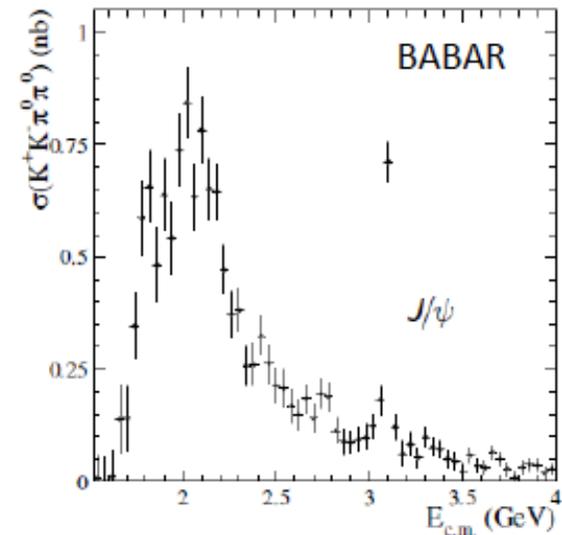


$$e^+e^- \rightarrow K^+K^-\pi^+\pi^-$$



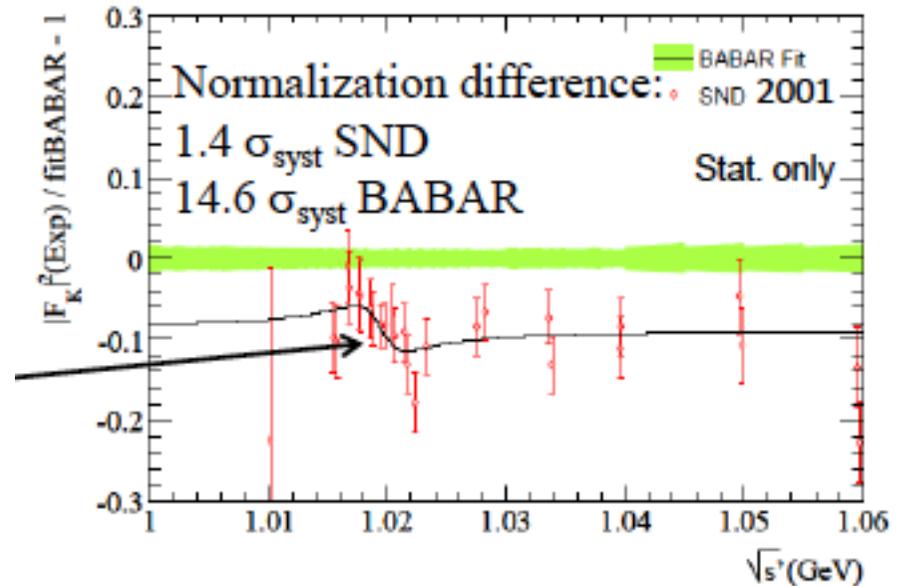
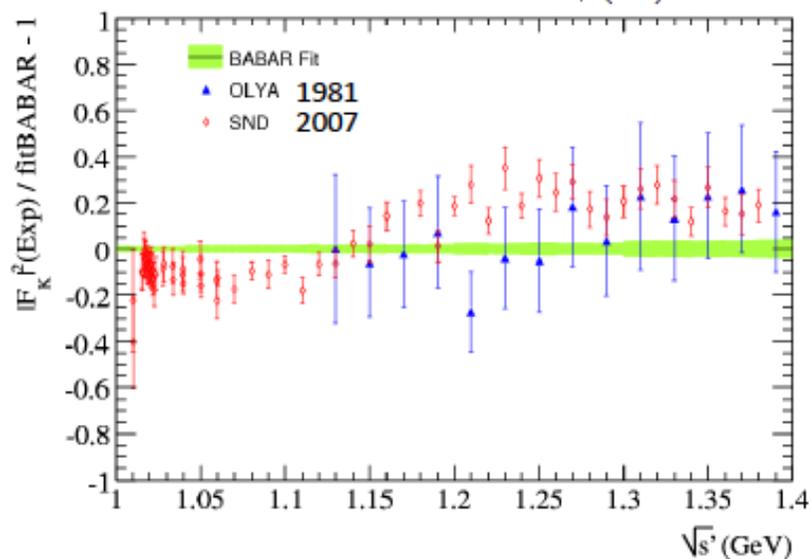
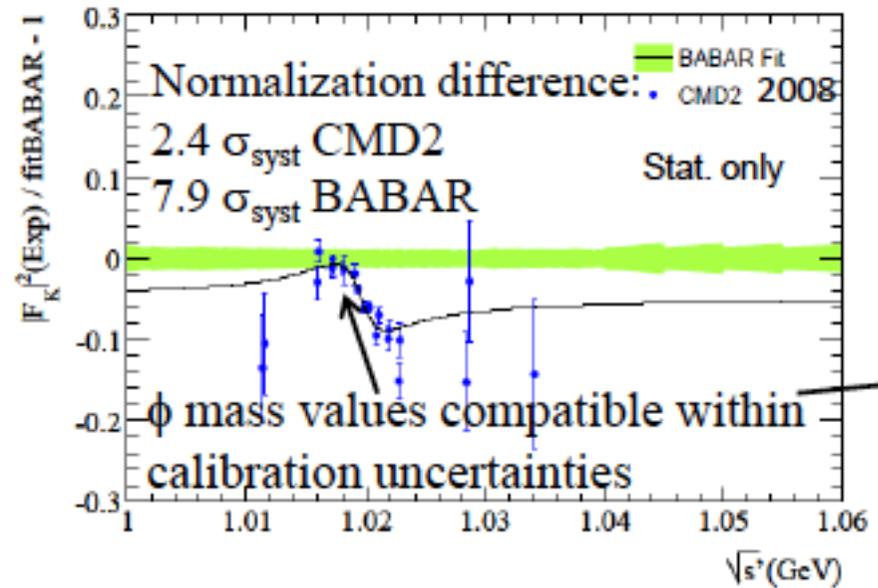
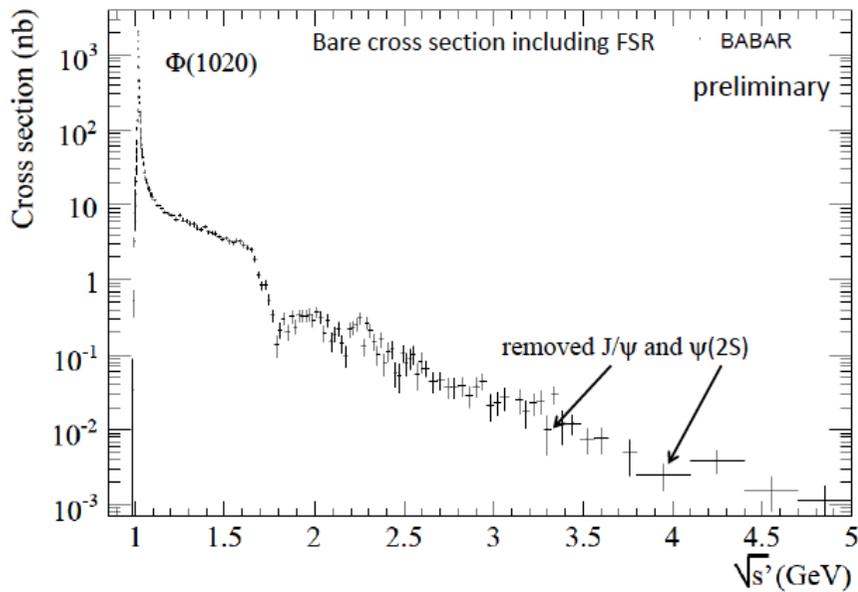
**Systematic  
uncertainties  
btw 2-15%**

- $< 1.4 \text{ GeV}$ : agreement with previous *BABAR* results, SND and CMD-2 data
- $> 1.4 \text{ GeV}$ : highest precision (DM2, 20%)



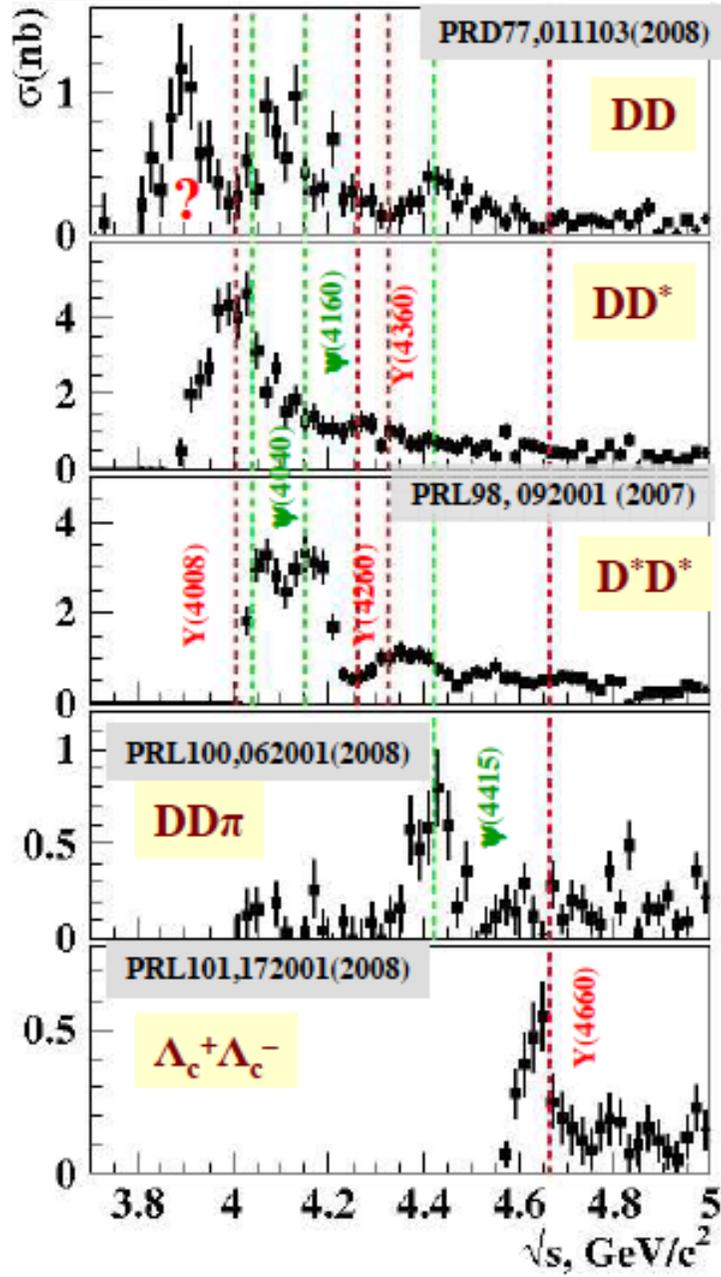
$$e^+e^- \rightarrow K^+K^-\pi^0\pi^0$$

# New: $e^+e^- \rightarrow K^+K^-(\gamma)$ cross section (preliminary)

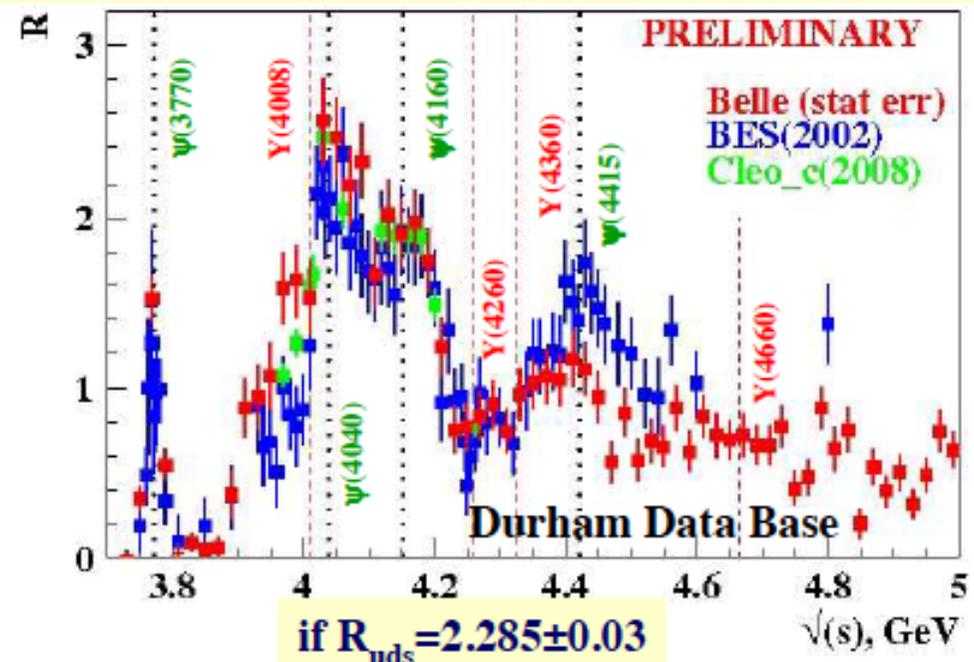




# $\sigma(e+e-\rightarrow\text{open charm})$ at Belle



## Belle: Sum of all measured exclusive contributions



### Y states vs exclusive cross sections

- Y(4008) mass coincides with DD\* peak
- Y(4260) mass corresponds to dip in D\*D\* cross-sect
- Y(4660) mass is close to  $\Lambda_c^+\Lambda_c^-$  peak
- Enhancement near 3.9 GeV in  $ee\rightarrow DD$  coupled channel effect?

$\psi(4415)$  still some unaccounted-for decay channels

Charm strange final states contribution

to be factor of 10 less

# $\sigma(e^+e^- \rightarrow \text{open charm})$ at Belle

*Six exclusive open charm final states were measured*

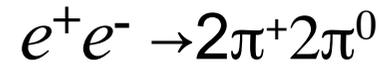
$$DD, DD\pi, DD^*\pi, D^*D, D^*D^*, \Lambda_c \Lambda_c$$

- Their sum is close to  $e^+e^- \rightarrow \text{hadrons}$
  - Belle & BaBar & Cleo\_c cross section measurements are consistent with each other in corresponding energy ranges
  - $D^*D^*$  (main contribution)
    - complicated shape of cross section
    - clear dip at  $M(D^*D^*) \sim 4260 \text{ GeV}$  (similar to inclusive R)
  - $DD^*$  (main contribution)
    - broad peak at threshold (shifted relative to 4040 GeV)
  - $DD$ 
    - complicated shape of cross section
    - broad enhancement  $\sim 3.9 \text{ GeV}$  – coupled channel effect?
  - $DD\pi$ 
    - $\psi(4415)$  signal observed, dominated by  $\psi(4415) \rightarrow DD_2$  (2460)
  - $DD^*\pi$ 
    - No evident structures observed
- In charm meson final states no evident peaks corresponding to members of charmoniumlike  $1^{--}$  family are found !*
- $\Lambda_c \Lambda_c$ 
    - Enhancement at threshold, quantum numbers, mass and width are consistent with  $Y(4660)$

# New data at the horizon:

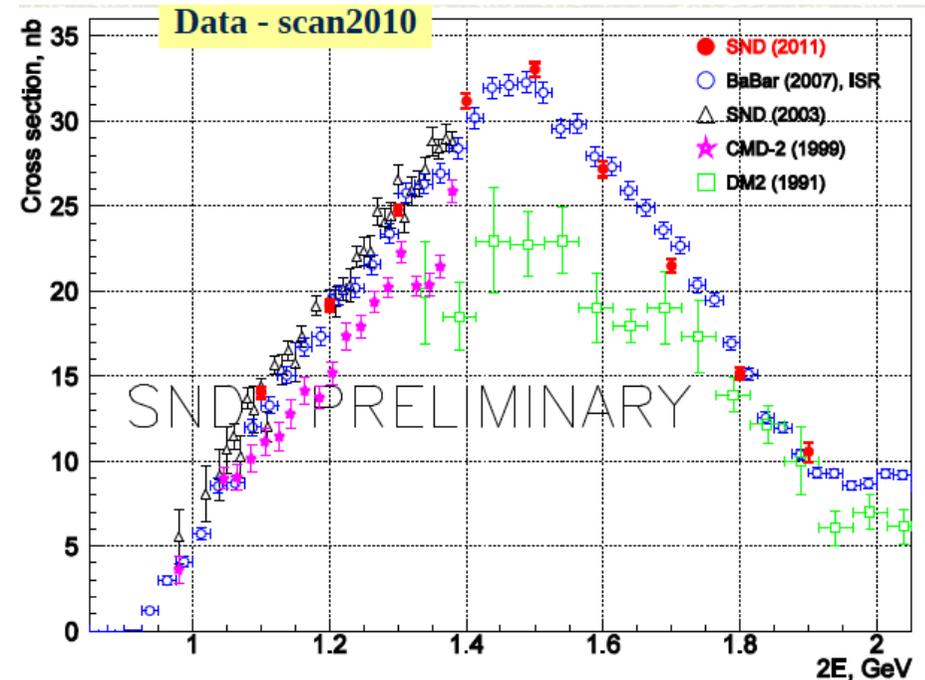
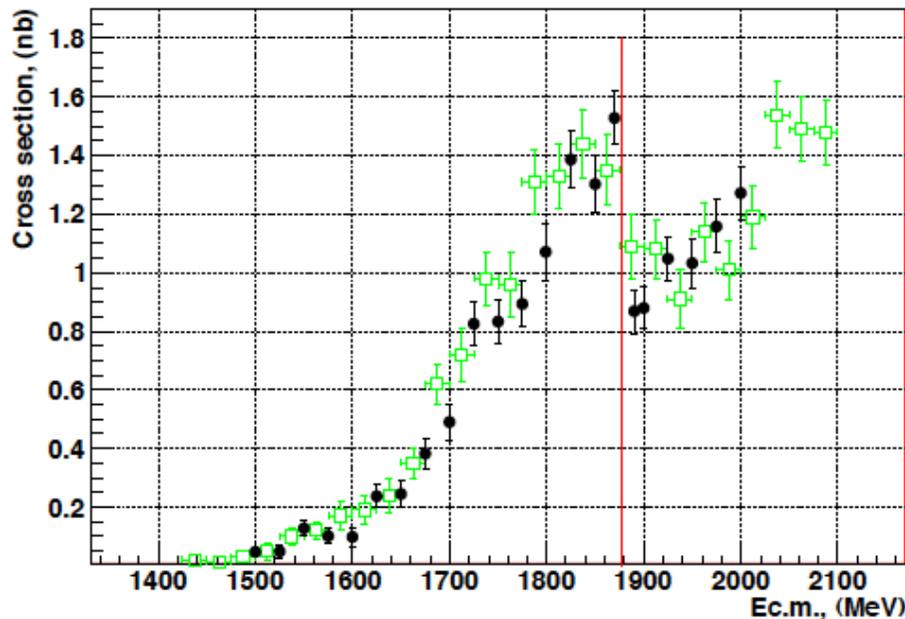
First data from VEPP-2000 @Novosibirsk  
( $L \sim 10^{31} \text{ cm}^{-2} \text{ sec}^{-1}$ )

$$\int L \sim 30 \text{ pb}^{-1}$$



SND

CMD3  $e^+e^- \rightarrow 3\pi^+3\pi^-$

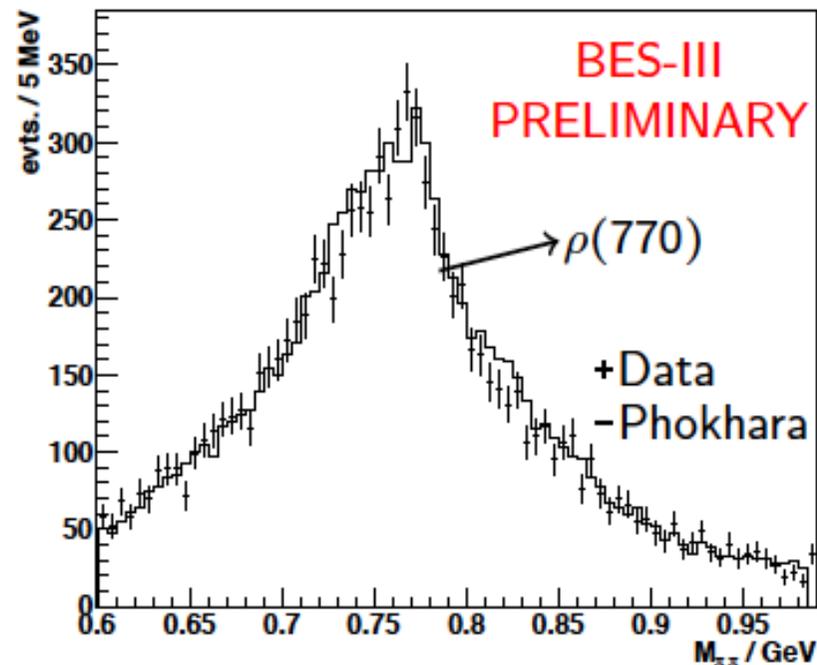


Additional results also from BaBar, Belle, BES with ISR, and possibly with DAFNE upgraded in energy (DAFNE-2, see [arXiv:1007.521](https://arxiv.org/abs/1007.521))

# Feasibility study of ISR analyses at BES-III on $\Psi''$

$$e^+e^- \rightarrow \pi^+\pi^-\gamma_{ISR}$$

- Phokhara event generator (within BES simulation framework)
- Data: pre-analysis (tagged) on  $400 \text{ pb}^{-1}$  performed

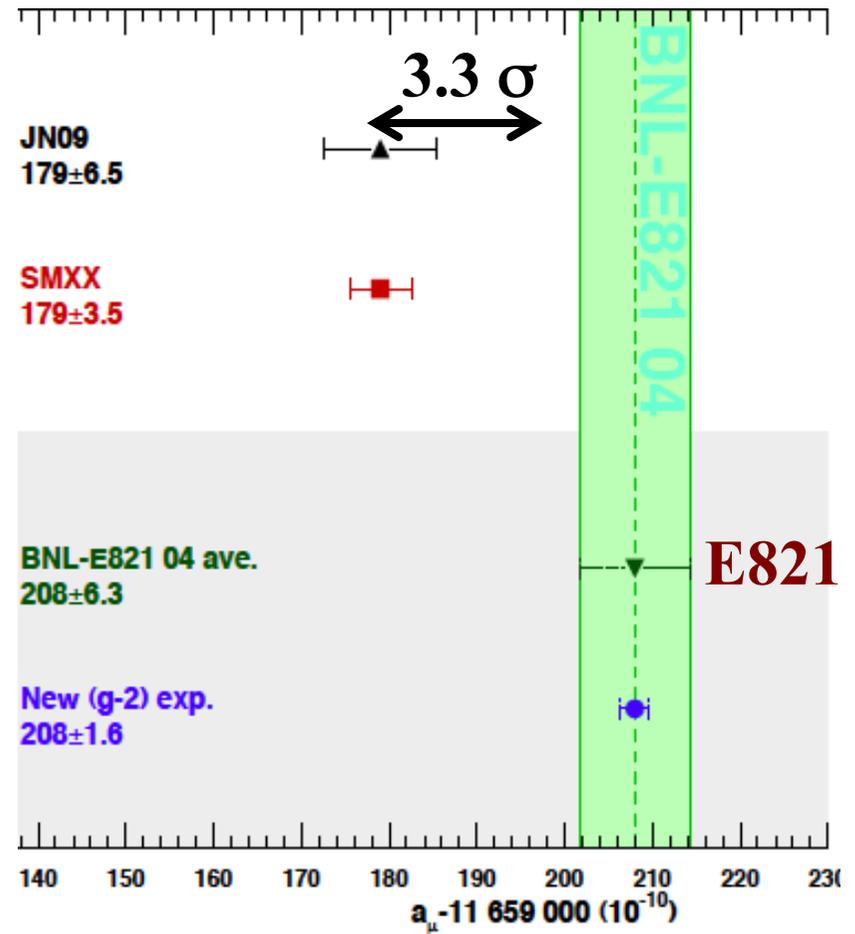


Diploma Thesis Zimmermann

# A rough estimate for g-2: now

$$a_{\mu}^{\text{exp}} - a_{\mu}^{\text{theo,SM}} = (27.7 \pm 8.4) 10^{-10} \quad (3.3\sigma)$$

$$8.4 = \sim 5_{\text{HLO}} \oplus \sim 3_{\text{HLbL}} \oplus 6_{\text{BNL}}$$



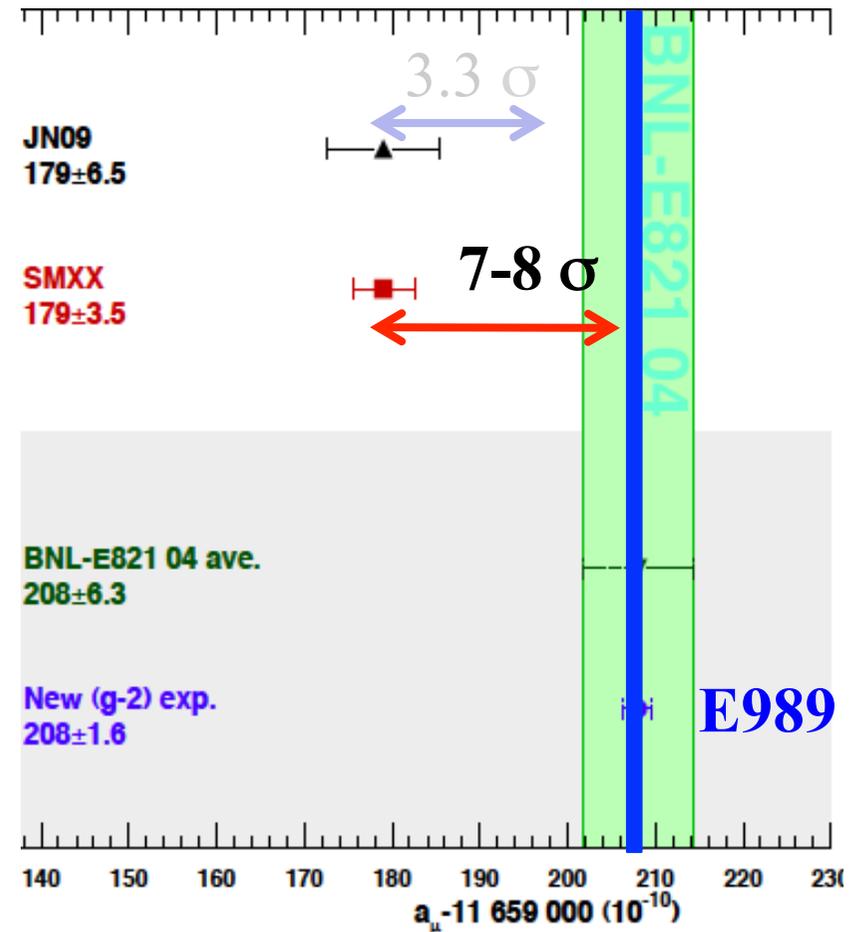
$$\delta a_{\mu}^{\text{HLO}} = 5.3 = 3.3(\sqrt{s} < 1\text{GeV}) \oplus 3.9(1 < \sqrt{s} < 2\text{GeV}) \oplus 1.2(\sqrt{s} > 2\text{GeV})$$

# A rough estimate for g-2: ...and (possible) future

$$a_{\mu}^{\text{exp}} - a_{\mu}^{\text{theo,SM}} = (27.7 \pm 8.4) 10^{-10} \quad (3.3\sigma)$$

$$8.4 = \sim 5_{\text{HLO}} \oplus \sim 3_{\text{HLbL}} \oplus 6_{\text{BNL}}$$

$\downarrow$                        $\downarrow$                        $\downarrow$                        $\downarrow$   
 4                      3                      3                      1.6 NEW G-2



$$a_{\mu}^{\text{exp}} - a_{\mu}^{\text{theo,SM}} = (\text{XXX} \pm 3.8) 10^{-10}$$

If central value is the same  $\rightarrow 7-8\sigma$

(if no progress on theory  $\rightarrow 5\sigma$ )

$$\delta a_{\mu}^{\text{HLO}} \rightarrow 2.6 = 1.9 (\sqrt{s} < 1 \text{ GeV}) \oplus 1.3 (1 < \sqrt{s} < 2 \text{ GeV}) \oplus 1.2 (\sqrt{s} > 2 \text{ GeV})$$

This is possible if:

- $\delta\sigma_{\text{HAD}} \sim 0.4\%$   $\sqrt{s} < 1\text{GeV}$  (instead of 0.7% as now)
- $\delta\sigma_{\text{HAD}} \sim 2\%$   $1 < \sqrt{s} < 2\text{GeV}$  (instead of 6% as now)

(Possible with direct scan or ISR at Flavour factories)



$$\delta a_{\mu}^{\text{HLO}} = 2.6 \cdot 10^{-10} \text{ (instead of } \sim 5 \text{ as now)}$$

A similar improvement on  $\delta\alpha_{\text{em}}(\text{Mz})$  using Adler function method

# Conclusion

- Significant improvement on R measurement in the last 15 years due to more precise data. Interplay with theorists for the control of RC and development of MC
- ISR opened a new way to precisely measure the hadronic cross sections
- New data are expected from DAFNE, VEPP2000, BESIII and (Super)B factories which will continue to improve the region below 5 GeV with ISR.
- These data would allow to reduce of a factor  $\sim 2$  the uncertainty on the hadronic contribution to  $g-2$  to match the request from the next  $g-2$  experiments (at FNAL and J-PARC). A similar improvement is expected on  $\alpha_{em}(Mz)$ .

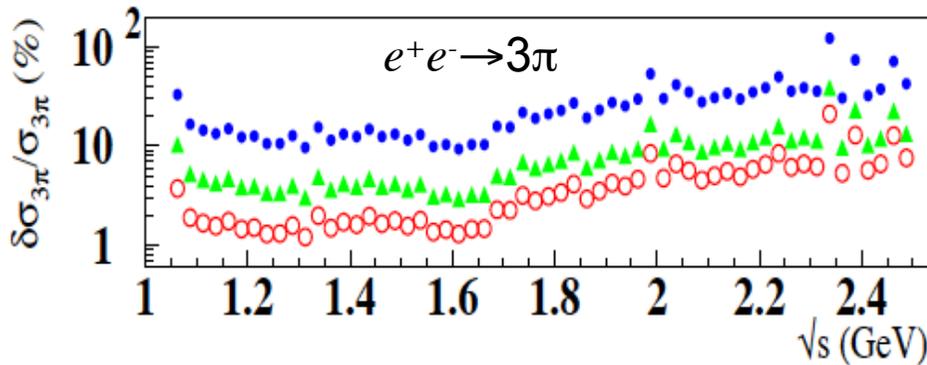
Stay tuned!

Thanks!

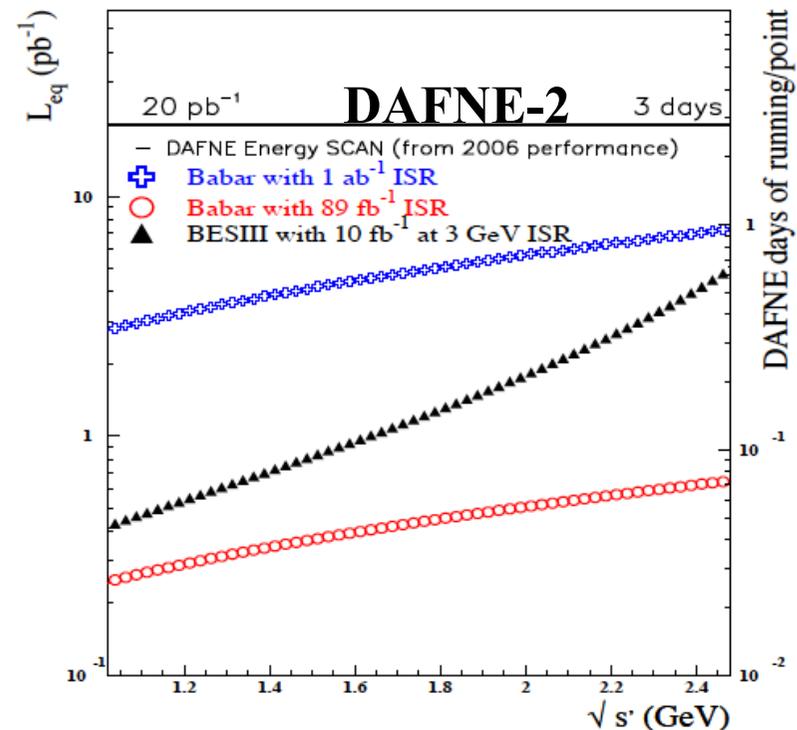
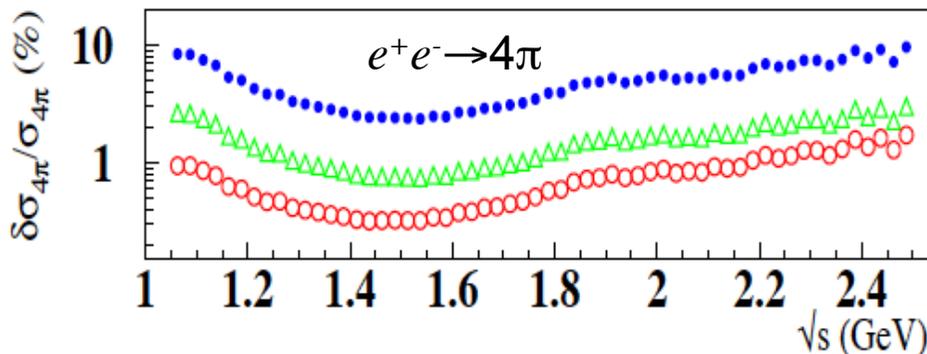
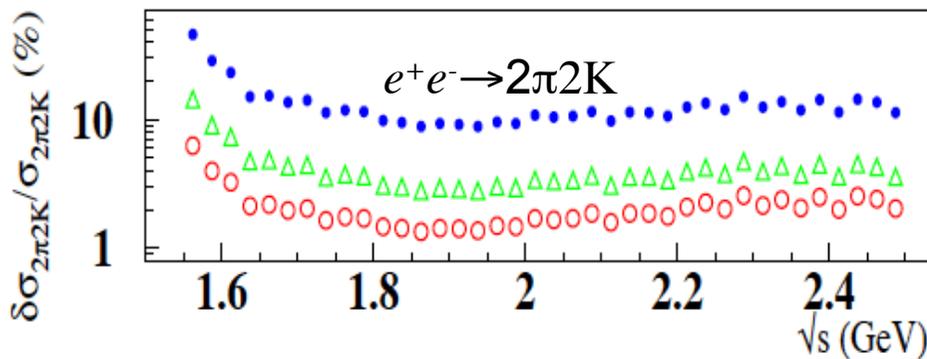
SPARE

# Impact of DAFNE-2 on exclusive channels in the range [1-2.5] GeV with a scan (Statistics only)

arXiv:1007.521



- Published BaBar results:  $89 \text{ fb}^{-1}$  (ISR)
- ▲ “BaBar”  $\times 10$  ( $890 \text{ fb}^{-1}$ )
- KLOE-2 energy scan:  $20 \text{ pb}^{-1}/\text{point}$   
@  $L = 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$ , 25 MeV bin  
 $\Rightarrow$  1 year data-taking

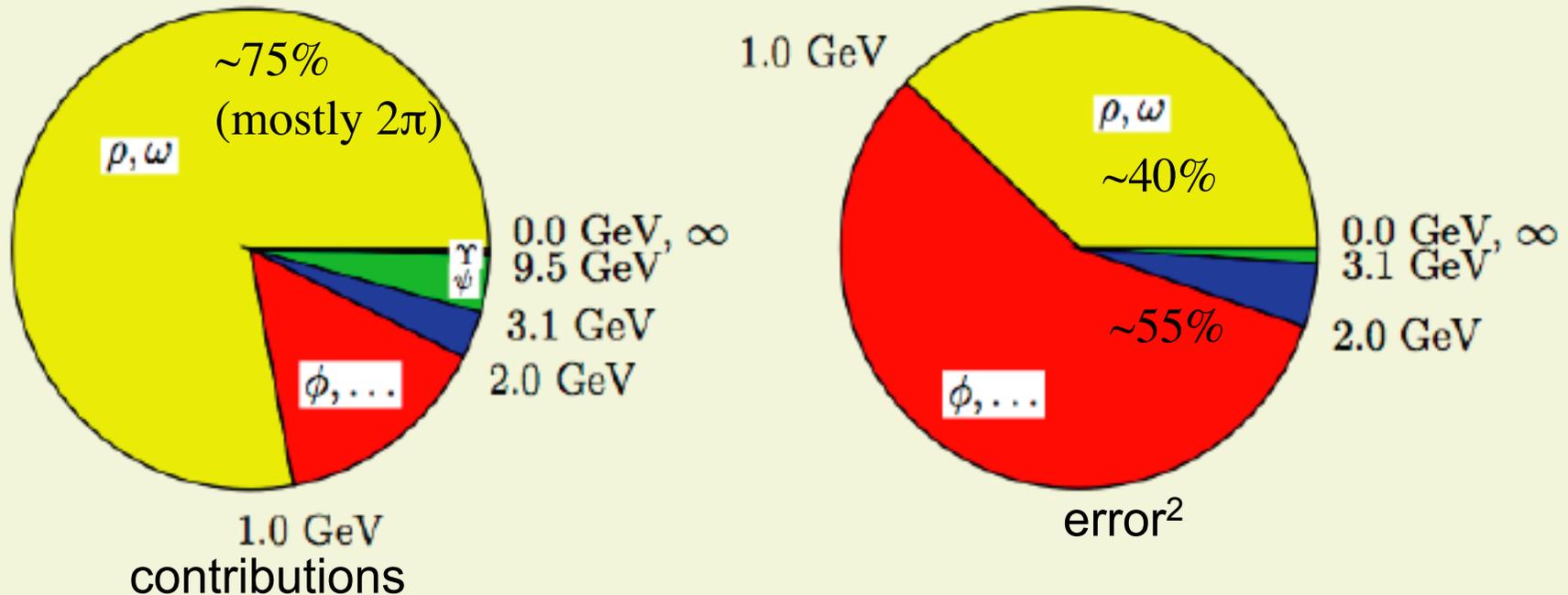


DAFNE-2 is statistically equivalent to  $5\div 10 \text{ ab}^{-1}$  (Super)B-factory

# Error budget on $a_{\mu}^{\text{HLO}}$

$$\delta a_{\mu}^{\text{HLO}} = 5.3 = 3.3(\sqrt{s} < 1 \text{ GeV}) \oplus 3.9(1 < \sqrt{s} < 2 \text{ GeV}) \oplus 1.2(\sqrt{s} > 2 \text{ GeV})$$

F. Jegerlehner, Talk at PHIPSI08

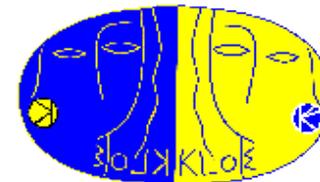


**in the range  $< 1 \text{ GeV}$   
contributes to 70% !**

But

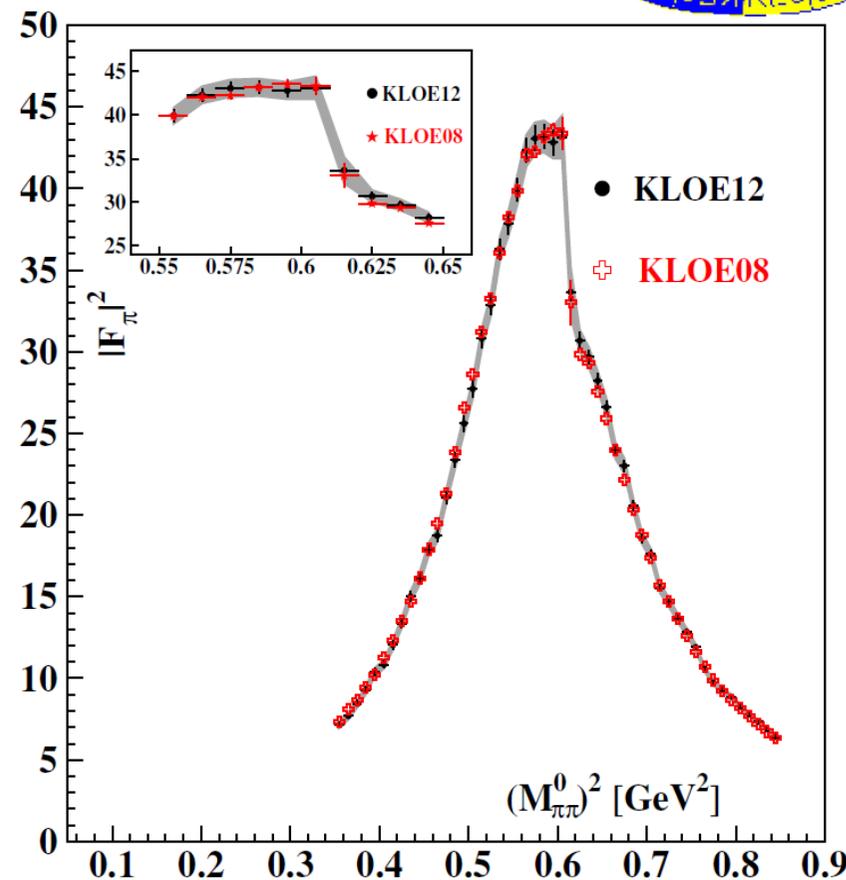
**Very important also the  
region 1-2 GeV !!!**

# KLOE12 result on $|F_\pi|^2$ and comp. with KLOE08



**KLOE08      KLOE12**

Syst. errors (%)	$\Delta^{\pi\pi} a_\mu$ abs	$\Delta^{\pi\pi} a_\mu$ ratio
Reconstruction Filter	negligible	negligible
Background subtraction	0.3	0.6
Trackmass	0.2	0.2
Particle ID	negligible	negligible
Tracking	0.3	0.1
Trigger	0.1	0.1
Unfolding	negligible	negligible
Acceptance ( $\theta_{\pi\pi}$ )	0.2	negligible
Acceptance ( $\theta_\pi$ )	negligible	negligible
Software Trigger (L3)	0.1	0.1
Luminosity	0.3 ( $0.1_{th} \oplus 0.3_{exp}$ )	-
$\sqrt{s}$ dep. of $H$	0.2	-
Total exp systematics	0.6	0.7
Vacuum Polarization	0.1	-
FSR treatment	0.3	0.2
Rad. function $H$	0.5	-
Total theory systematics	0.6	0.2
Total systematic error	0.9	0.7



	$a_\mu^{\pi\pi}(0.35 - 0.95 \text{ GeV}^2) \times 10^{10}$
<b>KLOE12</b>	$385.1 \pm 1.1_{\text{stat}} \pm 2.7_{\text{sys+theo}}$
<b>KLOE08</b>	$387.2 \pm 0.5_{\text{stat}} \pm 3.3_{\text{sys+theo}}$

- Good agreement btw the two measurements, especially in the  $\rho$  region.
- Improved syst. error in KLOE12. Theoretical error strongly reduced
- The two measurements are not independent ( $\pi\pi\gamma$  sample is the same)...

# Prospects on R?

- An significant improvement on  $\delta\alpha_{em}(M_Z^2)$  would require 1% up to 10 GeV (using the standard integration method of data ) or up to  $\sim 3$  GeV using the Adler function (+ improvements from Theory)
- But how realistic is this possibility?
- Remember the error is:

*F. Jegerlehner*

Energy (GeV)	< 1	1-2	2-3	3-9.5 (exc. J/ $\psi$ and $\Upsilon$ )	9.5-13
$\delta_{\text{tot}} R/R$	$\sim 0.5\%$	6%	4%	0.7%	5.5%
$\delta^2 \Delta \alpha_{\text{had}}^{(5)}(M_Z^2)$	$\sim 1\%$	<b>36%</b>	11%	2%	<b>31%</b>
$\delta^2 \Delta \alpha_{\text{had}}^{(5)}(-2.5 \text{ GeV})$	$\sim 4\%$	<b>75%</b>	12%	<1%	<1%

•(Super)B factories will continue to improve the region below 5 GeV with ISR. BESIII will also enter in the game both with a scan above 2-3 GeV and with ISR below. However not easy to keep the systematic error at 1% level using ISR (FSR, RC?).

# Prospects on R?

- VEPP2000 could improve the situation below 2 GeV by a direct scan
- An energy upgrade of Dafne would improve the region below 2/3 GeV as well
- This would allow to matches the request in precision using the Adler function method.
- However in the direct integration not clear how to reduce the error in the region 9.5 -13 GeV (unless using theory?)

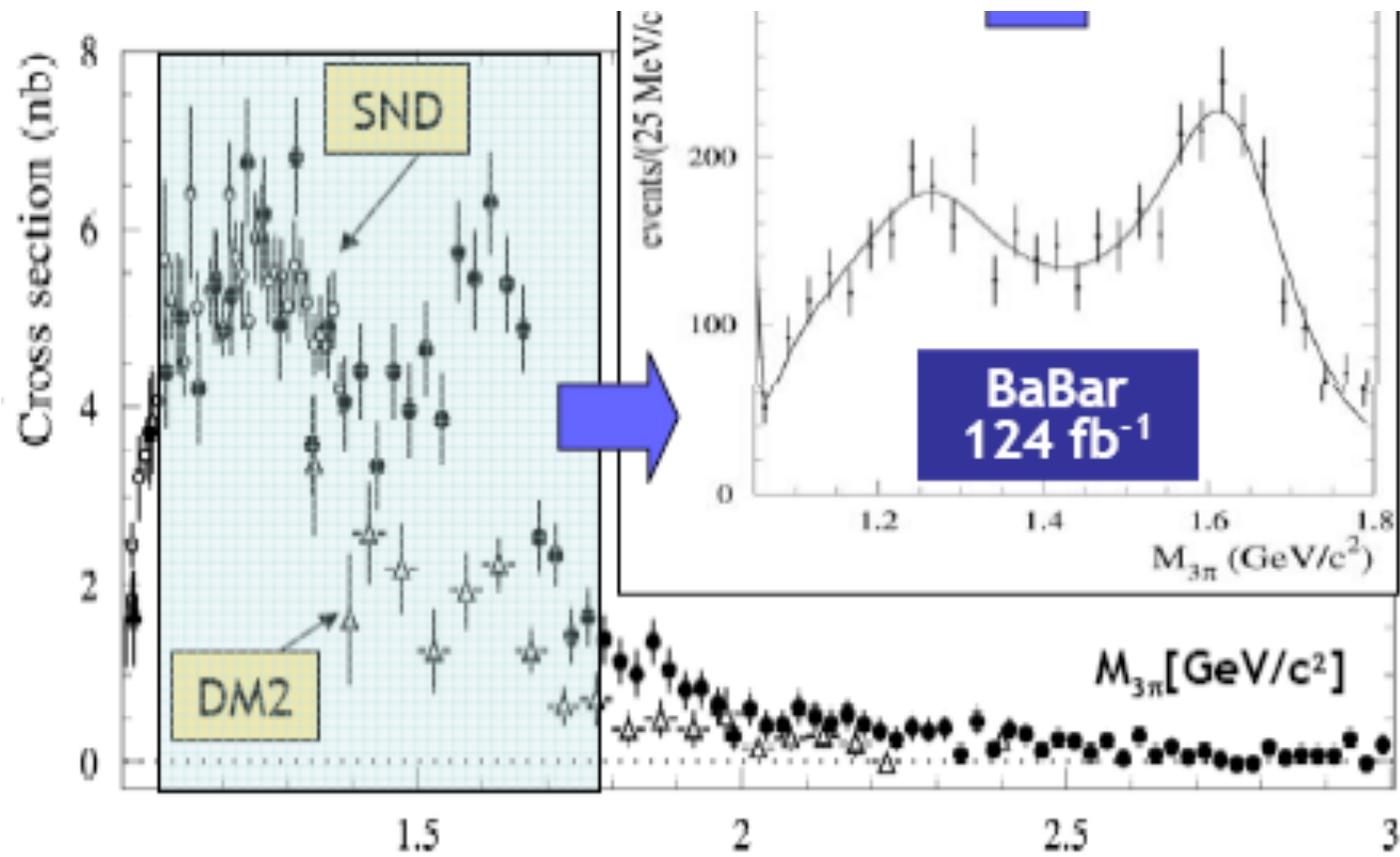
Energy (GeV)	< 1	1-2	2-3	3-9.5 (exc.J/ψ and Υ)	9.5-13
$\delta_{\text{tot}} R/R$	~0.5%	6%	4%	0.7%	5.5%
$\delta^2 \Delta \alpha_{\text{had}}^{(5)}(M_Z^2)$	~1%	<b>36%</b>	11%	2%	<b>31%</b>
$\delta^2 \Delta \alpha_{\text{had}}^{(5)}(-2.5\text{GeV})$	~4%	<b>75%</b>	12%	<1%	<1%

*F. Jegerlehner*

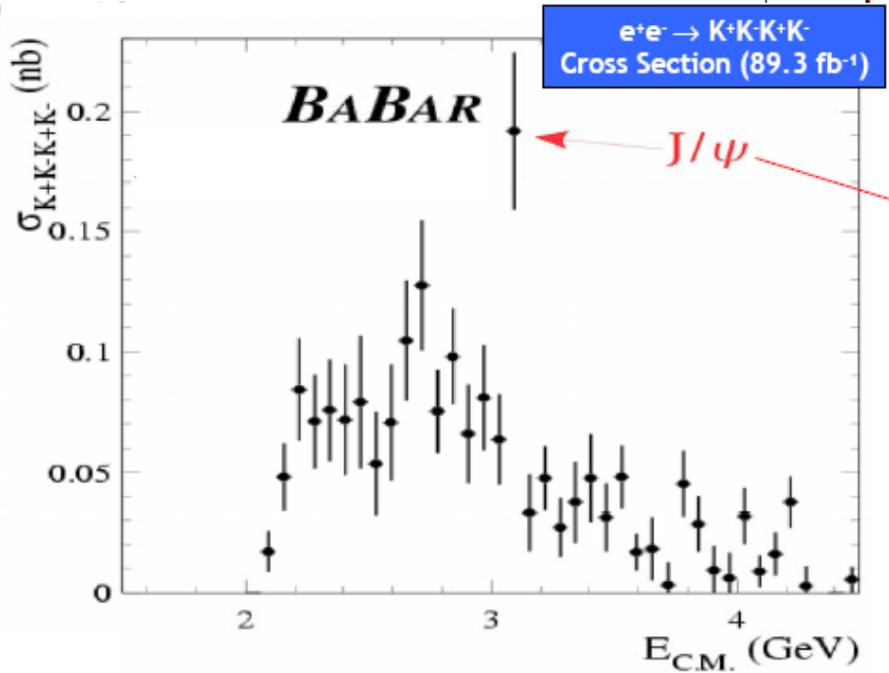
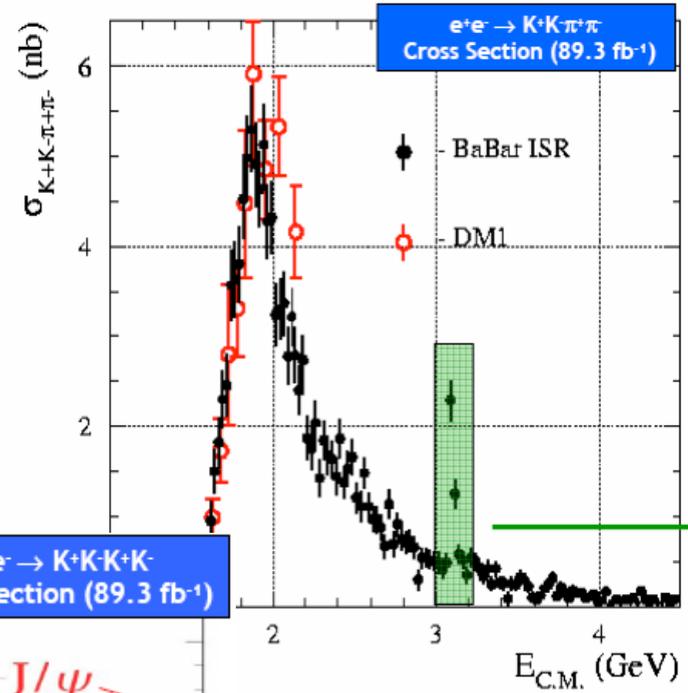
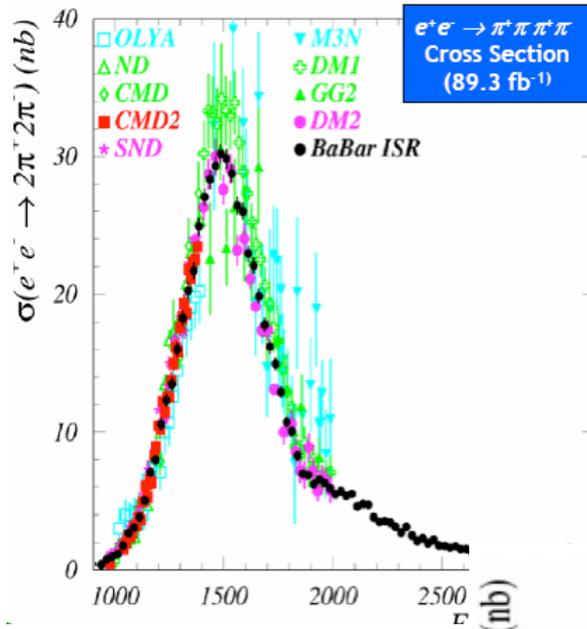
Thanks!

# Babar: $3\pi$

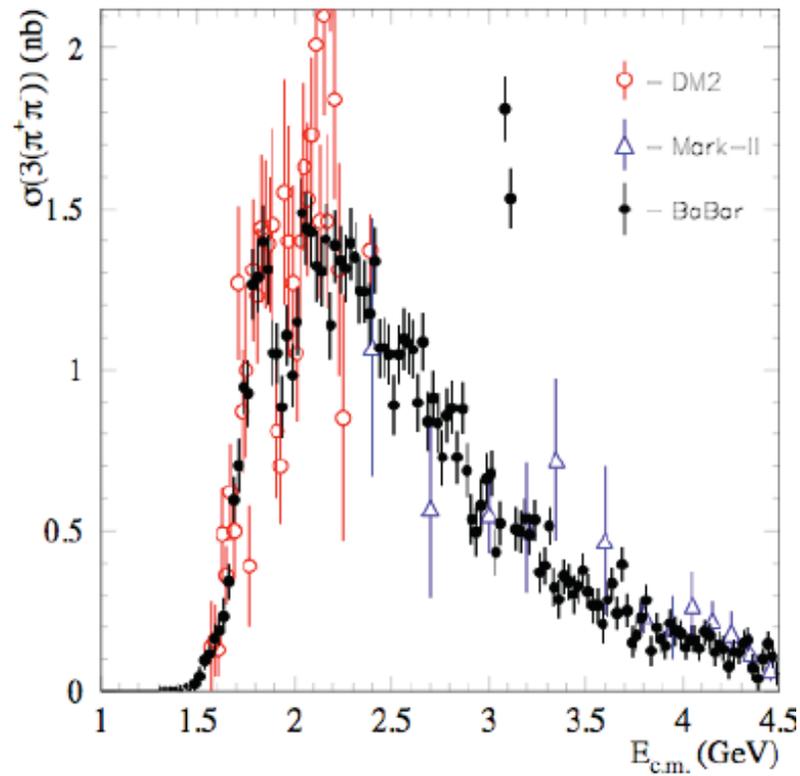
$\pi^+\pi^-\pi^0$



# Babar: 4h

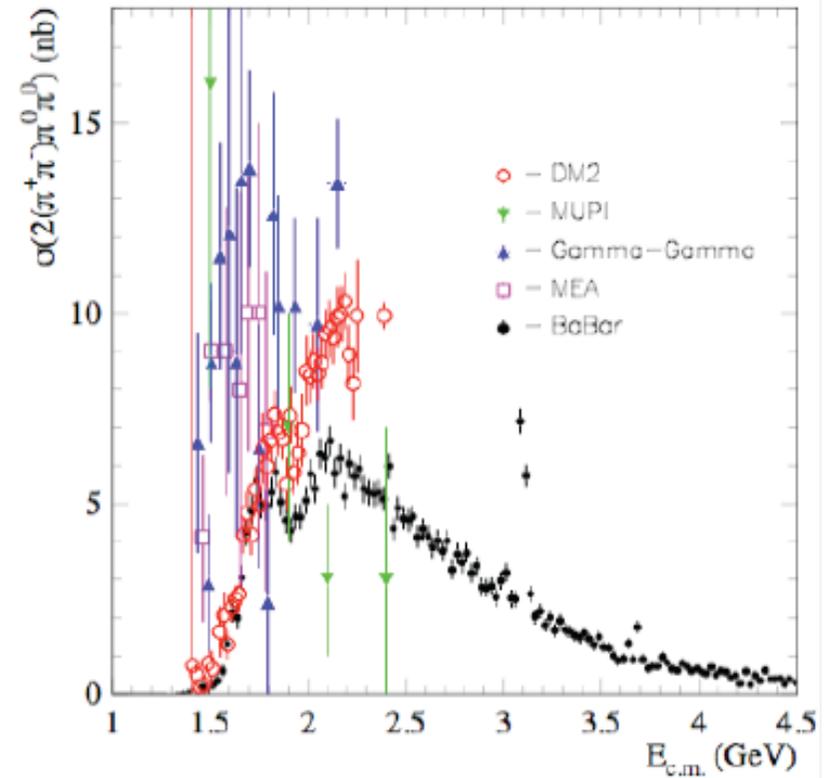


# Babar: $6\pi$



$3(\pi^+\pi^-)$

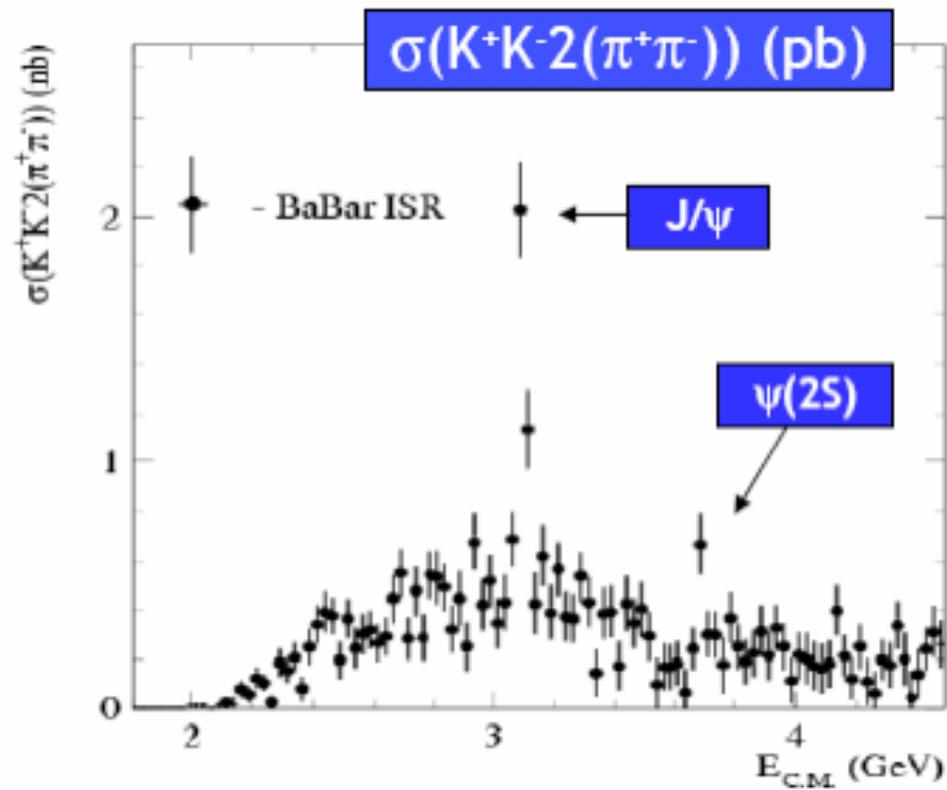
Total systematic: ~6-8%



$2(\pi^+\pi^-)\pi^0\pi^0$

Total systematic: ~11%

# Babar: $2K4\pi$



$2(\pi^+\pi^-)K^+K^-$

Total systematic:  $\sim 7\%$

# PION FORM FACTOR AT BABAR

## SYSTEMATIC ERRORS

$\sqrt{s}$ ' intervals (GeV)

errors in  $10^{-3}$

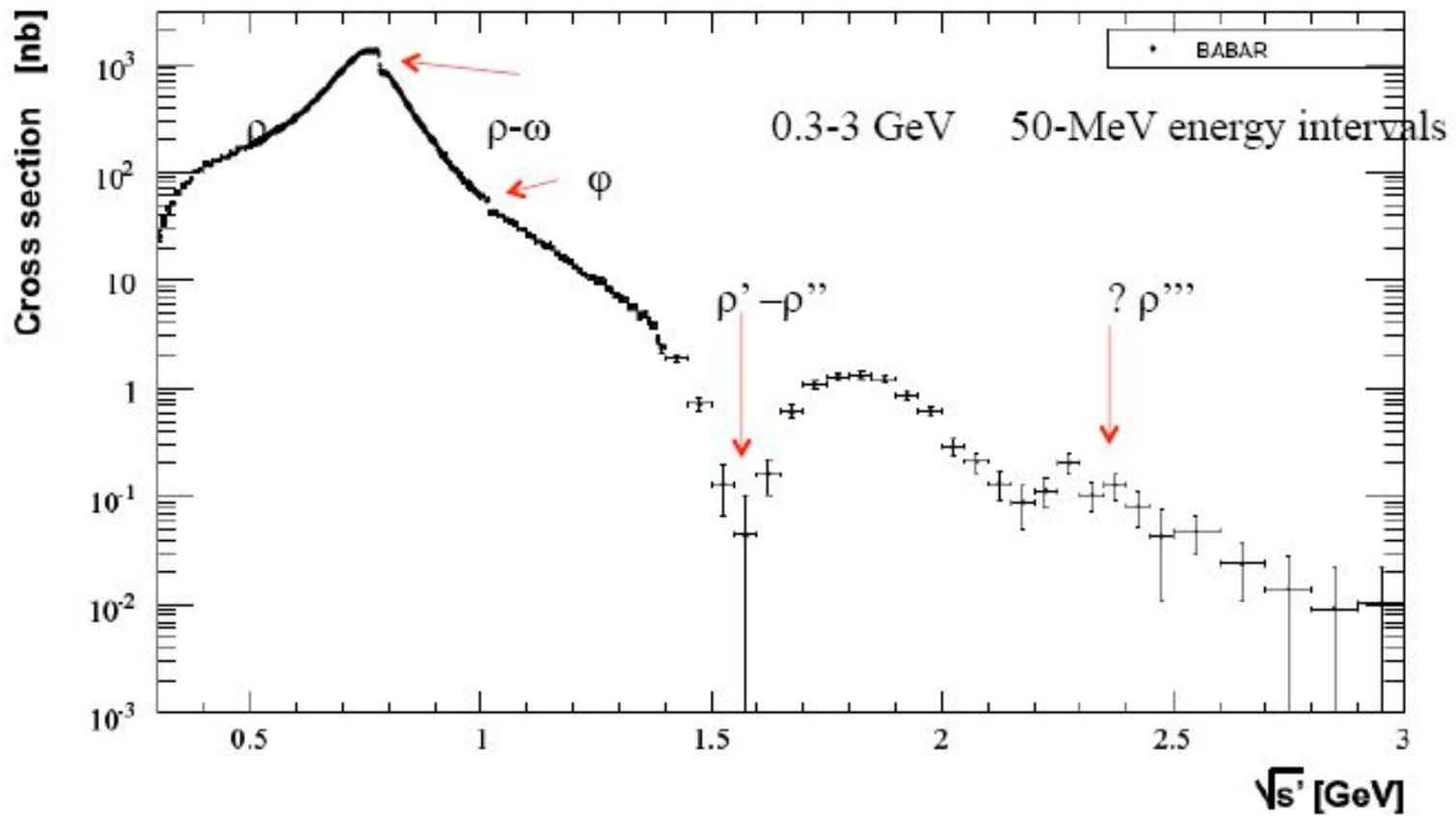
sources	0.3-0.4	0.4-0.5	0.5-0.6	0.6-0.9	0.9-1.2	1.2-1.4	1.4-2.0	2.0-3.0
trigger/ filter	5.3	2.7	1.9	1.0	0.5	0.4	0.3	0.3
tracking	3.8	2.1	2.1	1.1	1.7	3.1	3.1	3.1
$\pi$ -ID	10.1	2.5	6.2	2.4	4.2	10.1	10.1	10.1
background	3.5	4.3	5.2	1.0	3.0	7.0	12.0	50.0
acceptance	1.6	1.6	1.0	1.0	1.6	1.6	1.6	1.6
kinematic fit ( $\chi^2$ )	0.9	0.9	0.3	0.3	0.9	0.9	0.9	0.9
correl $\mu\mu$ ID loss	3.0	2.0	3.0	1.3	2.0	3.0	10.0	10.0
$\pi\pi/\mu\mu$ cancel.	2.7	1.4	1.6	1.1	1.3	2.7	5.1	5.1
unfolding	1.0	2.7	2.7	1.0	1.3	1.0	1.0	1.0
ISR luminosity	3.4	3.4	3.4	3.4	3.4	3.4	3.4	3.4
sum (cross section)	13.8	8.1	10.2	5.0	6.5	13.9	19.8	52.4

Dominated by particle ID ( $\pi$ -ID, correlated  $\mu\mu \rightarrow \pi\pi$ ,  $\mu$ -ID in ISR luminosity)

# PION FORM FACTOR AT BABAR

## CROSS SECTION

$e^+ e^- \rightarrow \pi^+ \pi^- (\gamma)$  bare (no VP) cross section diagonal errors stat+syst



## BaBar results with ISR: an incomplete list

- $e^+e^- \rightarrow \pi^+ \pi^- \pi^0$  between 1. and 3 GeV with  $\sigma_{\text{syst}} \sim 5\%-10\%$
- $e^+e^- \rightarrow 4h$  ( $\pi^+ \pi^- \pi^+ \pi^-$ ,  $\pi^+ \pi^- K^+ K^-$ ,  $K^+ K^- K^+ K^-$ ) between 0.6 and 4.5 GeV
  - $\sigma_{\text{syst}}(\pi^+ \pi^- \pi^+ \pi^-)$  is 12% (<1GeV), 5%(1.-3 GeV), 16% (>3 GeV)
  - $\sigma_{\text{syst}}(\pi^+ \pi^- K^+ K^-)$  is 15% (1.5-4.5 GeV)
  - $\sigma_{\text{syst}}(K^+ K^- K^+ K^-)$  is 20% (2.0-4.5 GeV)
- $e^+e^- \rightarrow 6h$  ( $3(\pi^+ \pi^-)$ ,  $2(\pi^+ \pi^-) \pi^0 \pi^0$ ,  $2(\pi^+ \pi^-) K^+ K^-$ ) between 1.5 and 4.5 GeV with  $\sigma_{\text{syst}}$  between 6 and 10%
- $e^+e^- \rightarrow \pi^+ \pi^-$  with  $\sigma_{\text{sys}} \sim 0.6\%$  (around the  $\rho$ )

Process	Systematic accuracy
$\pi^+ \pi^- \pi^0$	(6-8)%
$2\pi^+ 2\pi^-$	5%
$2\pi^+ 2\pi^0$	(8-14)%
$2\pi^+ 2\pi^- \pi^0$	(8-11)%
$2\pi^+ 2\pi^- \eta$	7%
$3\pi^+ 3\pi^- + 2\pi^+ 2\pi^- 2\pi^0$	(6-11)%
$KK\pi$	(5-6)%
$K^+ K^- \pi\pi$	(8-11)%

# BABAR RESULTS being updated

$$e^+e^- \rightarrow 2\mu\gamma, 2\pi\gamma, 2K\gamma, 2p\gamma, 2\Lambda\gamma, 2\Sigma\gamma, \Lambda\Sigma\gamma$$

$$e^+e^- \rightarrow 3\pi\gamma$$

$$e^+e^- \rightarrow 2(\pi^+\pi^-)\gamma, K^+K^-\pi^+\pi^-\gamma, K^+K^-\pi^0\pi^0\gamma, 2(K^+K^-)\gamma$$

$$e^+e^- \rightarrow 2(\pi^+\pi^-)\pi^0\pi^0\gamma, 3(\pi^+\pi^-)\gamma, K^+K^-\pi^+\pi^-\gamma$$

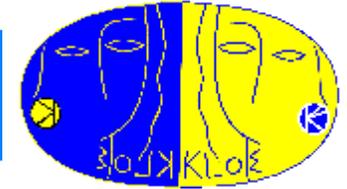
$$e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0\gamma, \pi^+\pi^-\pi^0\pi^0\pi^0\gamma, \pi^+\pi^-\pi^0\eta\gamma \dots$$

$$e^+e^- \rightarrow K^+K^-\pi^0\gamma, K^+K^-\eta\gamma \text{ (} KK^*\gamma, \phi\pi^0\gamma, \phi\eta\gamma \dots)$$

$$e^+e^- \rightarrow \pi^+\pi^-\pi^+\pi^-\pi^0/\eta\gamma, K^+K^-\pi^+\pi^-\pi^0/\eta\gamma$$

Are being updated to full BaBar data with  $\sim 500\text{fb}^{-1}$

# Extracting $\sigma_{\pi\pi}$ and $|F_{\Psi}|^2$ from $\pi\pi\gamma$



## a) Via absolute Normalisation to VLAB Luminosity (as in 2005 analysis):

$$1) \quad \frac{d\sigma_{\pi\pi(\gamma)}^{obs}}{dM_{\pi\pi}^2} = \frac{\Delta N_{Obs} - \Delta N_{Bkg}}{\Delta M_{\pi\pi}^2} \cdot \frac{1}{\epsilon_{Sel}} \cdot \frac{1}{\int L dt}$$

$ds_{\Psi\Psi g(g)}/dM^2$  is obtained by subtracting background from observed event spectrum, divide by selection efficiencies, and *int. luminosity*:

$$2) \quad \sigma_{\pi\pi}(s) \approx s \frac{d\sigma_{\pi\pi(\gamma)}^{obs}}{dM_{\pi\pi}^2} \cdot \frac{1}{H(s)}$$

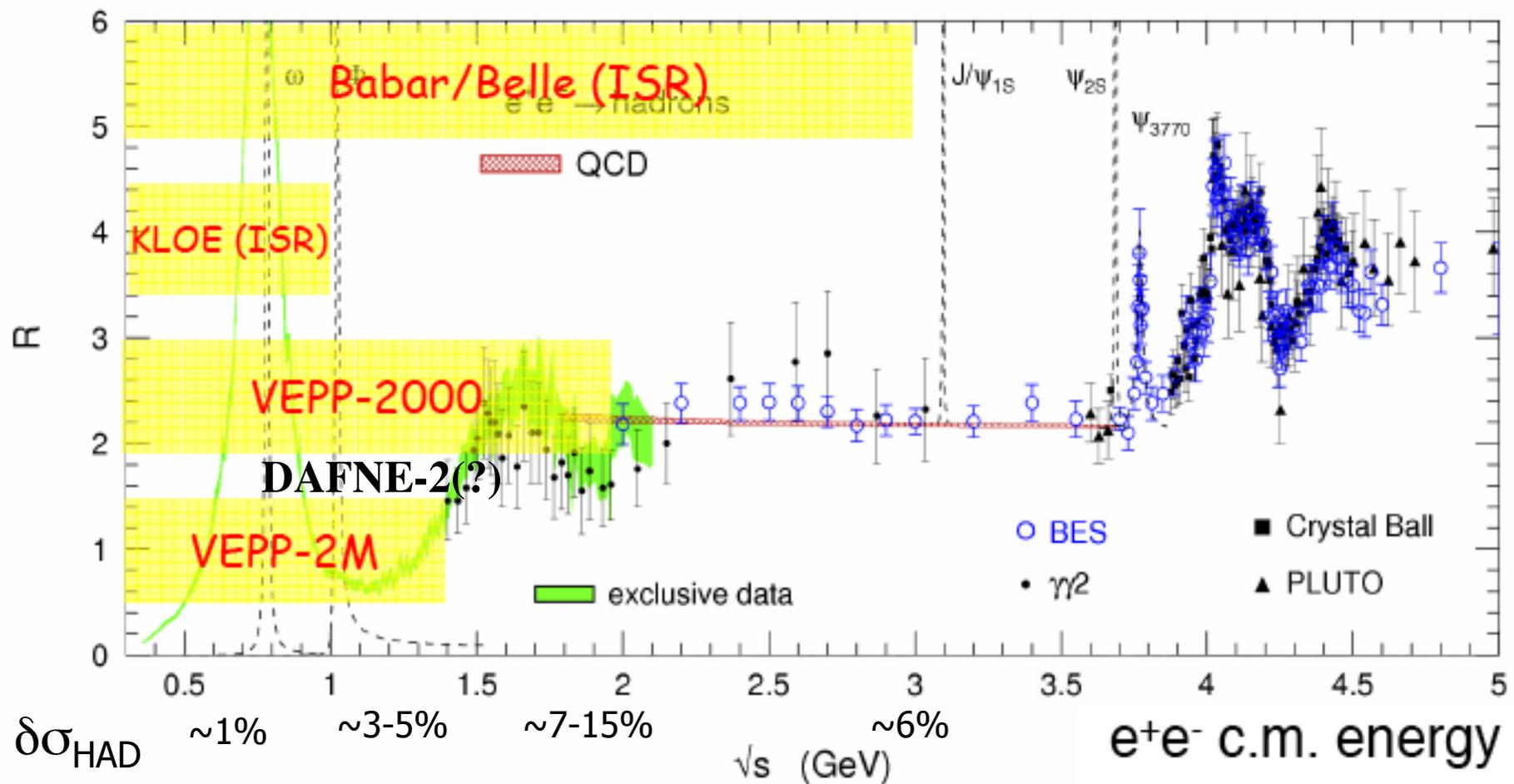
Obtain  $s_{\Psi\Psi}$  from (ISR) - radiative cross section  $ds_{\Psi\Psi g(g)}/dM^2$  via theoretical radiator function  $H(s)$ :

$$3) \quad |F_{\pi}|^2 = \frac{3s}{\pi\alpha^2\beta_{\pi}^3} \sigma_{\pi\pi}(s)$$

Relation between  $|F_p|^2$  and the cross section  $s(e^+e^- \Psi \Psi^+ \Psi^-)$

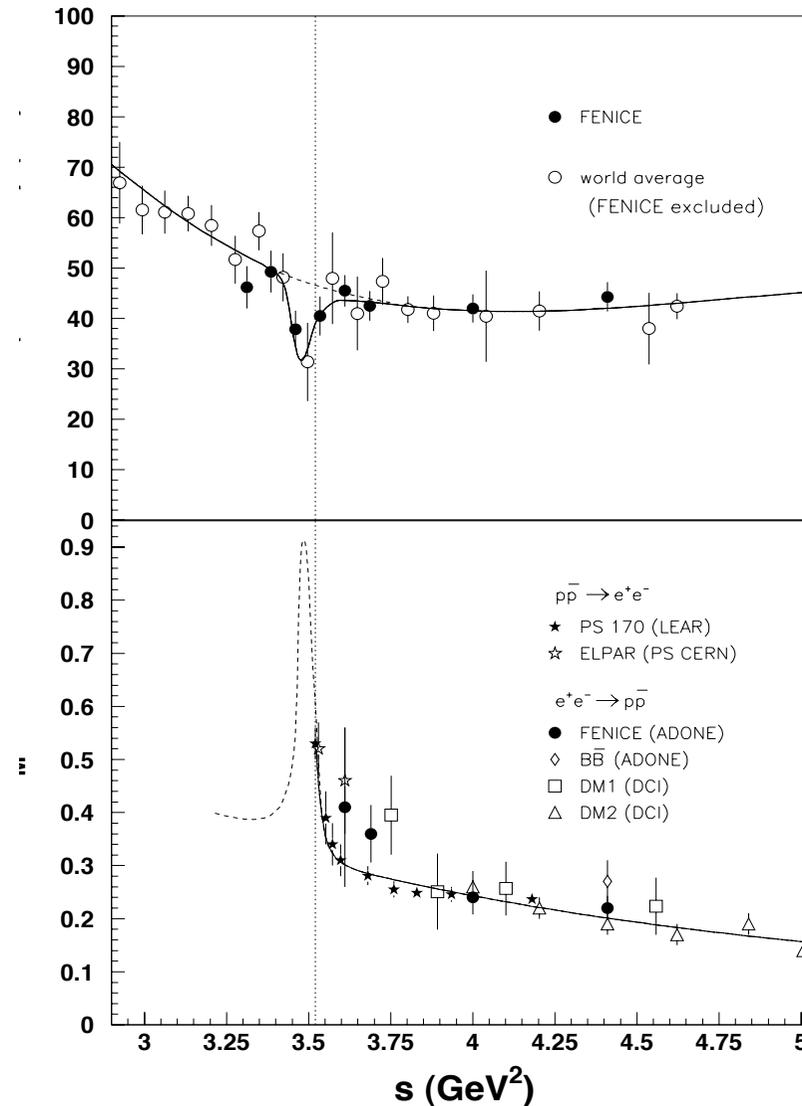
## b) Via bin-by-bin Normalisation to rad. Muon events

# $e^+e^-$ data: current and future/activities



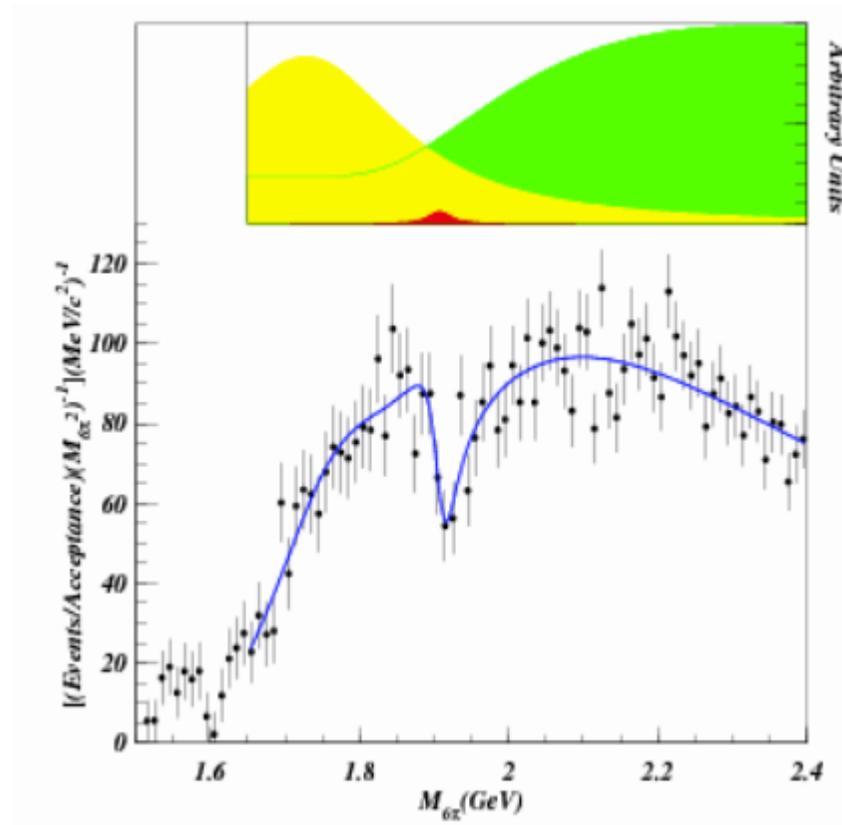
# Open issues

- Buco nella sezione d'urto multiadronica vicino a soglia  $p\bar{b}$
- narrow vector meson resonance, with a mass  $M \sim 1.87 \text{ GeV}$  and a width  $\Gamma \sim 10\text{-}20 \text{ MeV}$ , consistent with an  $N\bar{N}$  bound state

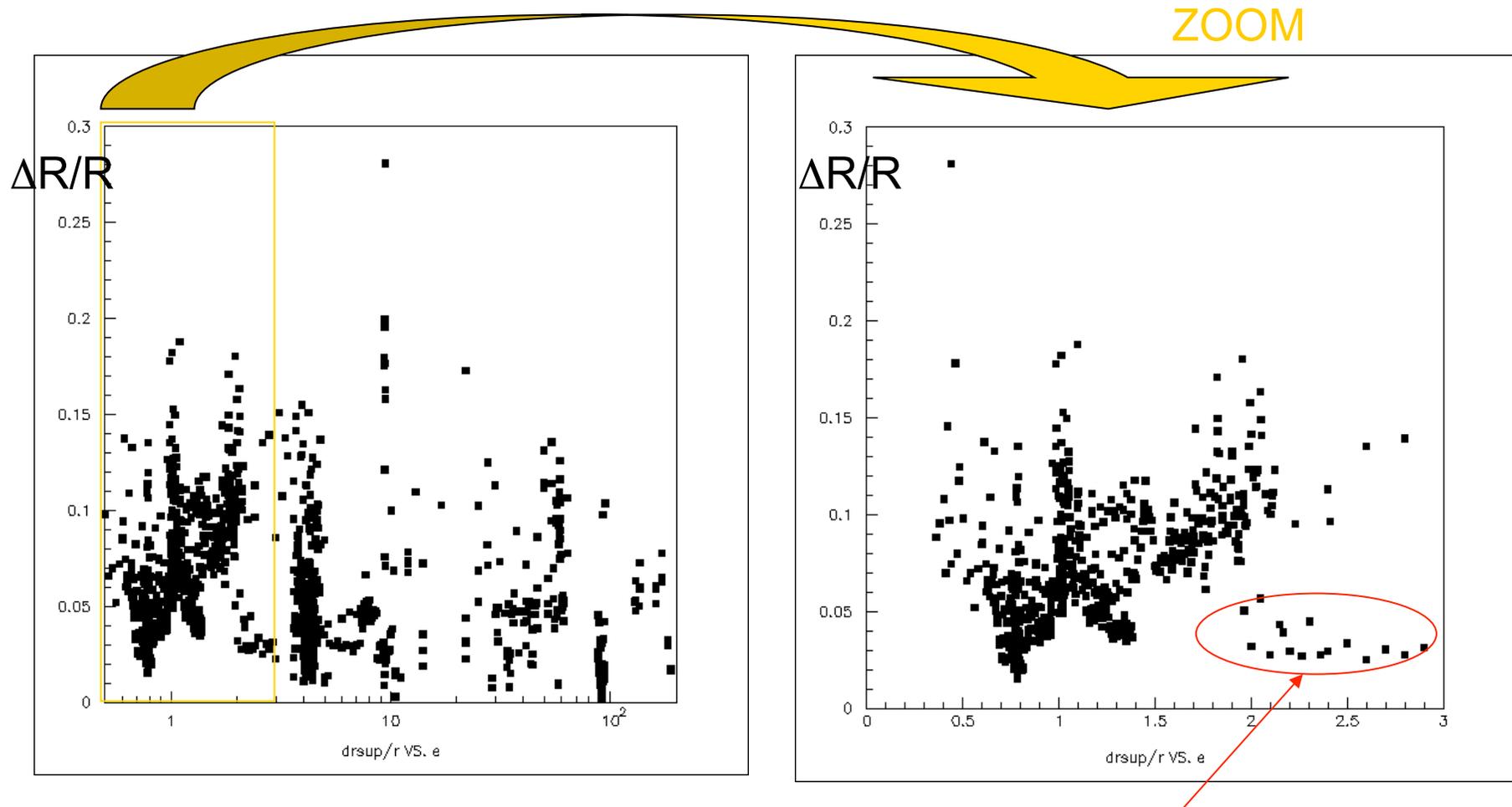


# Open issues

- Buco di FOCUS nella sezione d'urto dei  $6\pi$
- Babar conferma in entrambi i canali



# Errore percentuale



Punti con errore  $\sim 3\%$  dalla misura inclusiva di BES

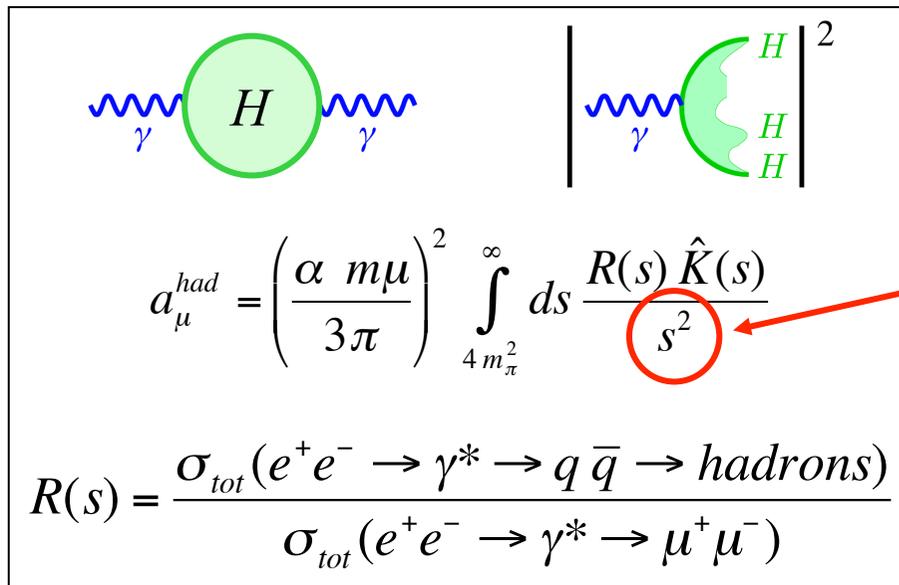
PRL 84, 594 (2000) – PRL 88, 101802 (2002)

## Comparison of different evaluations of $\Delta\alpha^{(5)}_{\text{had}}$

$\Delta\alpha^{(5)}_{\text{had}}$	Method	Ref
$0.0280 \pm 0.00065$	data < 12 GeV	S.Eidelman F.Jegerlehner '95
$0.02777 \pm 0.00017$	data < 1.8 GeV	J.H.Kuhen, M.Steinhauser '98
$0.02763 \pm 0.00016$	data < 1.8 GeV	M.Davier, A.Höcker '98
$0.027730 \pm 0.000148$	Euclidean > 2.5 GeV	F.Jegerlehner '99
$0.027426 \pm 0.000190$	scaled data, pQCD 2.8-3.7, 5- $\infty$	A.D.Martin et al. '00
$0.027896 \pm 0.000391$	data < 12 GeV (new data CMD2 & BES)	F.Jegerlehner '01
$0.02761 \pm 0.00036$	data < 12 GeV (new data CMD2 & BES)	H.Burkhardt, B.Pietrzyk '01 ( '05)
0.00007 (0.00005)	$\delta\sigma \sim 1\%$ up to $J/\psi$ ( $\delta\sigma \sim 1\%$ up to $\Upsilon$ )	

# $a_{\mu}^{\text{HLO}}$ :

L.O. Hadronic contribution to  $a_{\mu}$  can be estimated by means of a dispersion integral:



The diagram shows two Feynman diagrams. The left one is a tree-level diagram with a photon (wavy line) entering a green circle labeled 'H', and another photon (wavy line) exiting. The right one is a loop diagram with a photon (wavy line) entering a green loop labeled 'H', and another photon (wavy line) exiting. Below the diagrams is the dispersion integral for  $a_{\mu}^{\text{had}}$ :

$$a_{\mu}^{\text{had}} = \left( \frac{\alpha m_{\mu}}{3\pi} \right)^2 \int_{4m_{\pi}^2}^{\infty} ds \frac{R(s) \hat{K}(s)}{s^2}$$

The  $s^2$  in the denominator is circled in red. Below the integral is the definition of  $R(s)$ :

$$R(s) = \frac{\sigma_{\text{tot}}(e^+e^- \rightarrow \gamma^* \rightarrow q\bar{q} \rightarrow \text{hadrons})}{\sigma_{\text{tot}}(e^+e^- \rightarrow \gamma^* \rightarrow \mu^+\mu^-)}$$

$1/s^2$  makes **low energy contributions** especially important:

$$e^+e^- \rightarrow \pi^+\pi^-$$

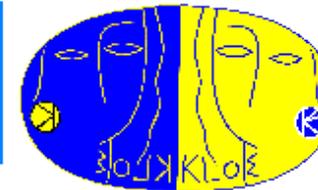
in the range  $< 1$  GeV contributes to 70% !

- $K(s)$  = analytic kernel-function
- above sufficiently high energy value, typically 2...5 GeV, use *pQCD*

Input:

- hadronic electron-positron cross section data (G.dR 69, E.J.95, A.D.H.'97,...)
- hadronic  $t$ - decays, which can be used with the help of the CVC-theorem and an isospin rotation (plus isospin breaking corrections)

# LA Event Selection (KLOE10)



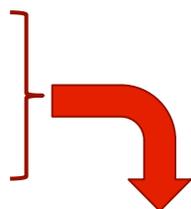
**2 pion tracks at large angles**

$$50^\circ < \theta_p < 130^\circ$$

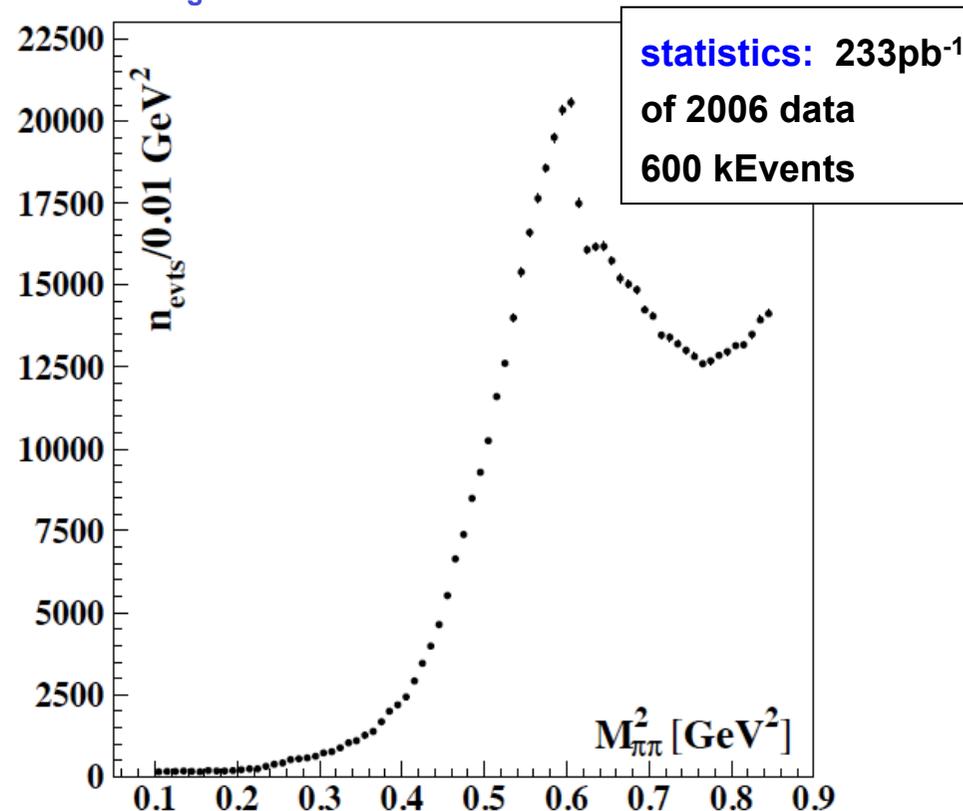
**Photons at large angles**

$$50^\circ < \theta_\gamma < 130^\circ$$

- ✓ independent complementary analysis
- ✓ threshold region  $(2m_\pi)^2$  accessible
- ✓  $\gamma_{\text{ISR}}$  photon detected  
(4-momentum constraints)
- ✓ lower signal statistics
- ✓ larger contribution from FSR events
- ✓ larger  $\phi \rightarrow \pi^+\pi^-\pi^0$  background contamination
- ✓ irreducible background from  $\phi$  decays ( $\phi \rightarrow f_0 \gamma \rightarrow \pi\pi \gamma$ )



**At least 1 photon with  $50^\circ < \theta_g < 130^\circ$   
and  $E_g > 20$  MeV  $\rightarrow$  photon detected**



Use data sample taken at  $\sqrt{s} \approx 1000$  MeV,  
20 MeV below the f<sub>0</sub>-peak

# Impact of DAFNE-2 on $(g-2)_\mu$

arXiv:1007.521

$$a_\mu^{\text{exp}} - a_\mu^{\text{theo,SM}} = (27.7 \pm 8.4) 10^{-10} \quad (3.3\sigma) \quad [\text{Eidelman, TAU08}]$$

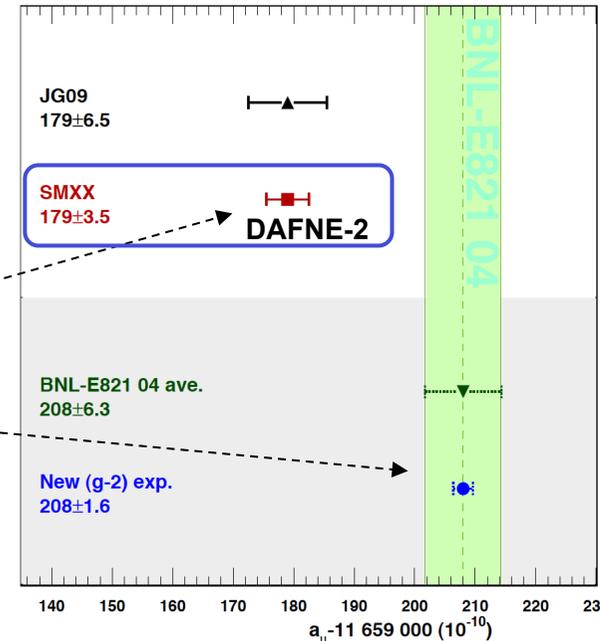
$$8.4 = \sim 5_{\text{HLO}} \oplus \sim 3_{\text{HLbL}} \oplus 6_{\text{BNL}}$$

$$4 \quad \quad 2.6_{\text{DAFNE-2}} \quad 2.5 \quad 1.6_{\text{NEW G-2}}$$

**7-8 $\sigma$**   
(if 27.7 will remain the same)

$$\delta a_\mu^{\text{HLO}} = 5.3 = 3.3(\sqrt{s} < 1\text{GeV}) \oplus 3.9(1 < \sqrt{s} < 2\text{GeV}) \oplus 1.2(\sqrt{s} > 2\text{GeV})$$

$$\delta a_\mu^{\text{HLO}} \rightarrow 2.6 = 1.9(\sqrt{s} < 1\text{GeV}) \oplus 1.3(\sqrt{s} < 1\text{GeV}) \oplus 1.2(\sqrt{s} > 2\text{GeV})$$



This means:

$\delta\sigma_{\text{HAD}} \sim 0.4\%$   $\sqrt{s} < 1\text{GeV}$  (instead of 0.7% as now) *With ISR at 1 GeV*  
 $\delta\sigma_{\text{HAD}} \sim 2\%$   $1 < \sqrt{s} < 2\text{GeV}$  (instead of 6% as now) *With Energy Scan 1-2 GeV*

*Possible at DAFNE-2!*

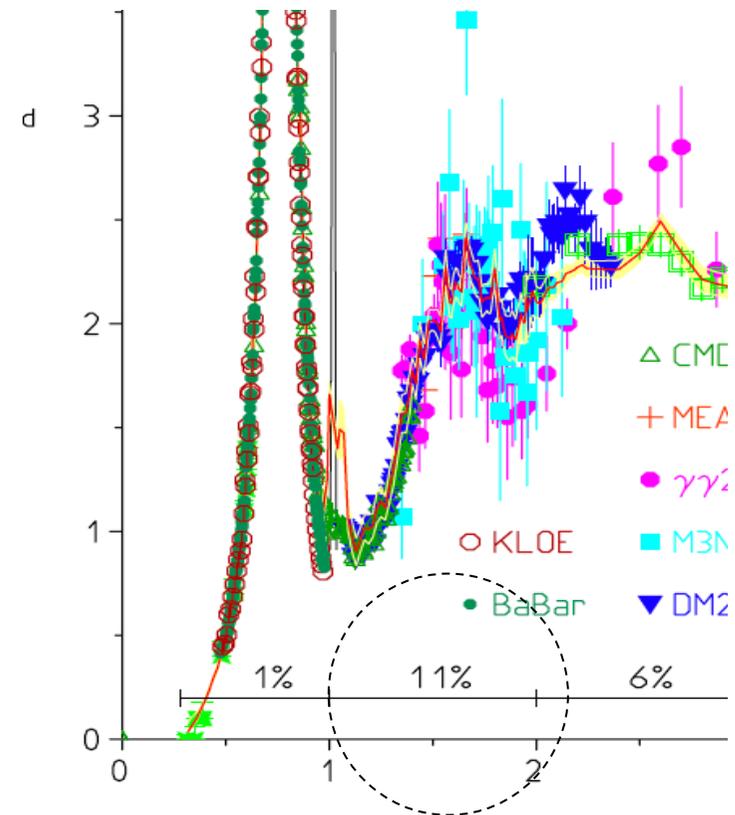
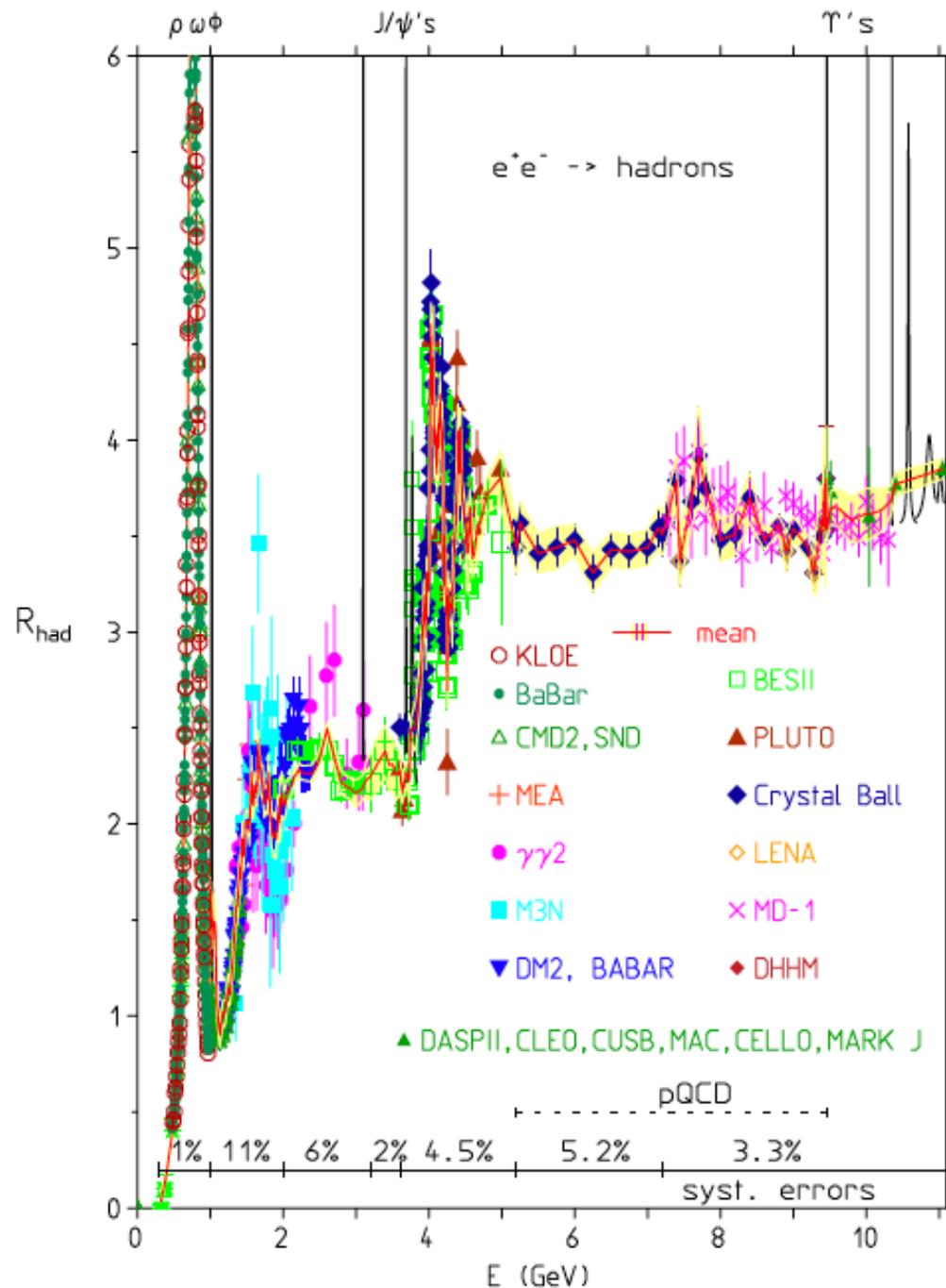
However the project is not yet approved...

Precise measurement of  $\sigma_{\text{HAD}}$  at low energies very important also for  $\alpha_{\text{em}}(M_Z)$  (necessary for ILC) !!!

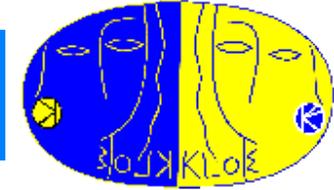
## Data at 2012 (F.J.)

Many improvements (mostly due to BaBar ISR).

However the region below 2.5 GeV is still poorly known ( $\delta R \sim 5-15\%$ )



# Radiative Corrections



## Radiator-Function $H(s, s_p)$ (ISR):

- ISR-Process calculated at NLO-level

**PHOKHARA** generator

(H.Czyż, A.Grzełińska, J.H.Kühn, G.Rodrigo, EPJC27,2003)

**Precision: 0.5%**

$$s \cdot \frac{d\sigma_{\pi\pi\gamma}}{ds_\pi} = \sigma_{\pi\pi}(s_\pi) \times H(s, s_\pi)$$

## Radiative Corrections:

### i) Bare Cross Section

divide by Vacuum Polarisation  $d(s) = (a(s)/a(0))^2$

→ from F. Jegerlehner

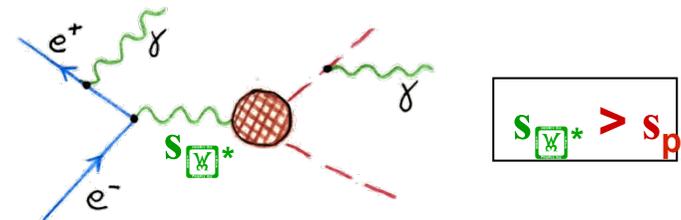
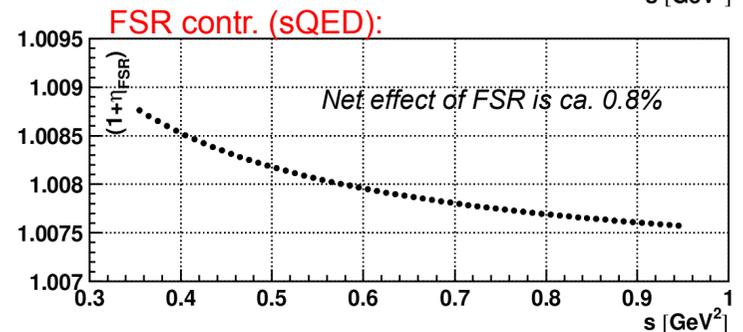
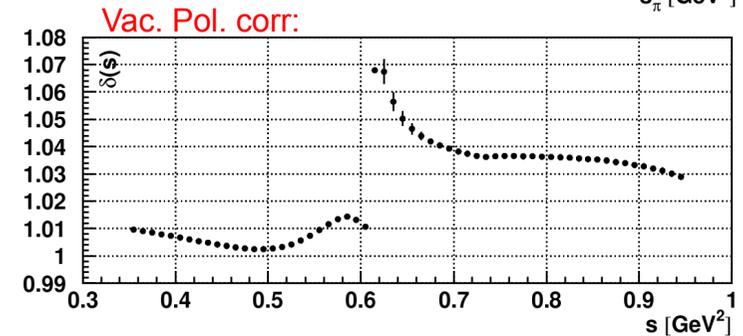
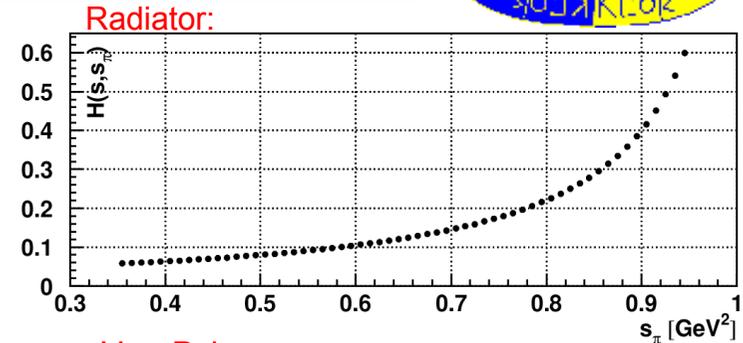
### ii) FSR

Cross section  $s_{pp}$  must be incl. for FSR  
for use in the dispersion integral of  $a_m$

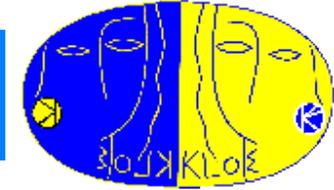


FSR corrections have to be taken into account  
in the efficiency eval. (Acceptance,  $M_{Trk}$ ) and in  
the mapping  $s_\pi \rightarrow s_{\gamma^*}$

(H.Czyż, A.Grzełińska, J.H.Kühn, G.Rodrigo, EPJC33,2004)



# SA Event Selection (KLOE08)



a) 2 tracks with  $50^\circ < \theta_{\text{track}} < 130^\circ$

b) small angle (not detected)  $\gamma$

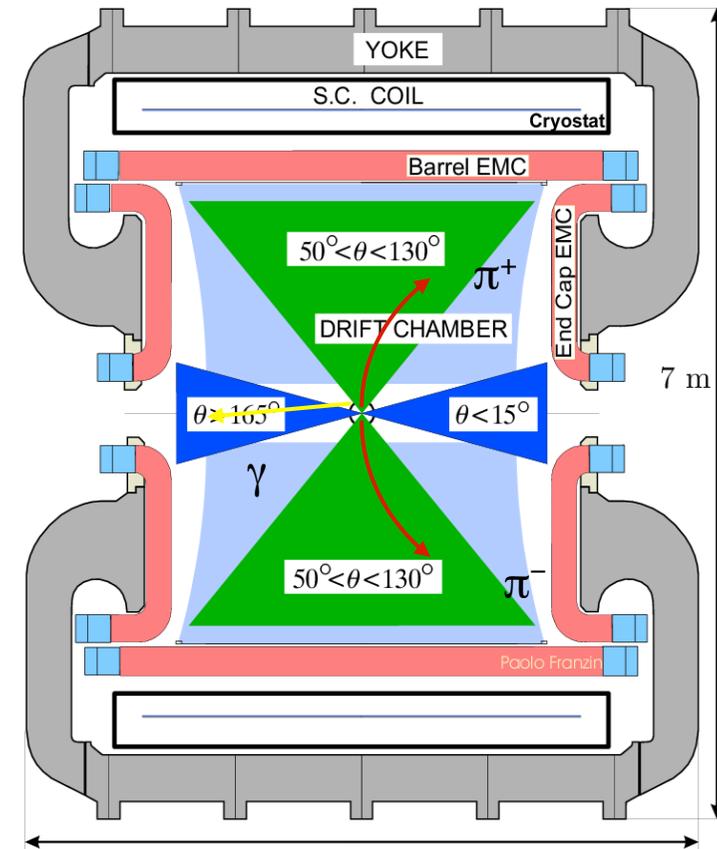
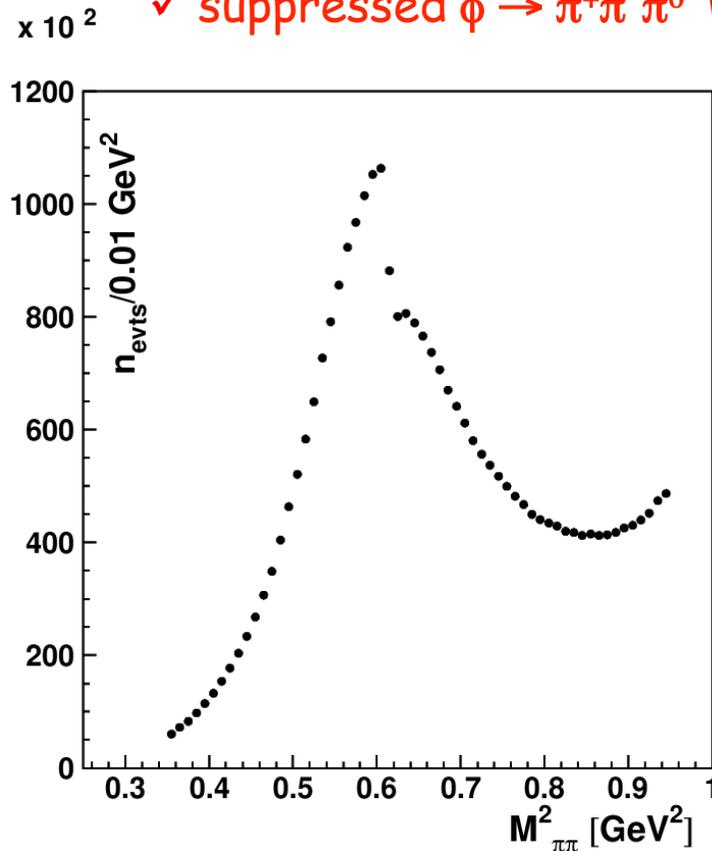
( $\theta_{\pi\pi} < 15^\circ$  or  $> 165^\circ$ )

✓ high statistics for ISR

✓ low relative FSR contribution

✓ suppressed  $\phi \rightarrow \pi^+\pi^-\pi^0$  wrt the signal

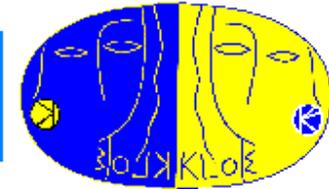
kinematics:  $\vec{p}_\gamma = \vec{p}_{\text{miss}} = -(\vec{p}_+ + \vec{p}_-)$



**statistics:** 240pb<sup>-1</sup> of 2002 data

**3.1 Mill. Events between 0.35 and 0.95 GeV<sup>2</sup>**

# Luminosity:



KLOE measures  $L$  with Bhabha scattering

F. Ambrosino et al. (KLOE Coll.)  
**Eur.Phys.J.C47:589-596,2006**

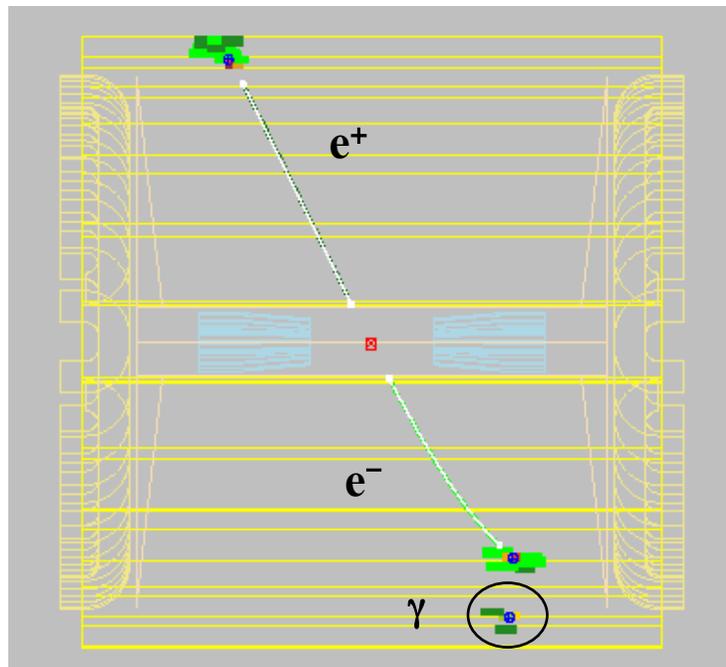
$55^\circ < \theta < 125^\circ$   
 acollinearity  $< 9^\circ$   
 $p \geq 400$  MeV

$$\int \mathcal{L} dt = \frac{N_{obs} - N_{bkg}}{\sigma_{eff}}$$

generator used for  $\sigma_{eff}$

**BABAYAGA (Pavia group):**

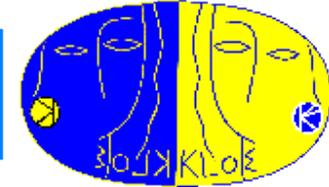
*C. M.C. Calame et al., NPB758 (2006) 22*



new version (**BABAYAGA@NLO**) gives  
 0.7% decrease in cross section,  
 and better accuracy: 0.1%

Systematics on Luminosity	
Theory	0.1 %
Experiment	0.3 %
TOTAL 0.1 % th $\oplus$ 0.3% exp = 0.3%	

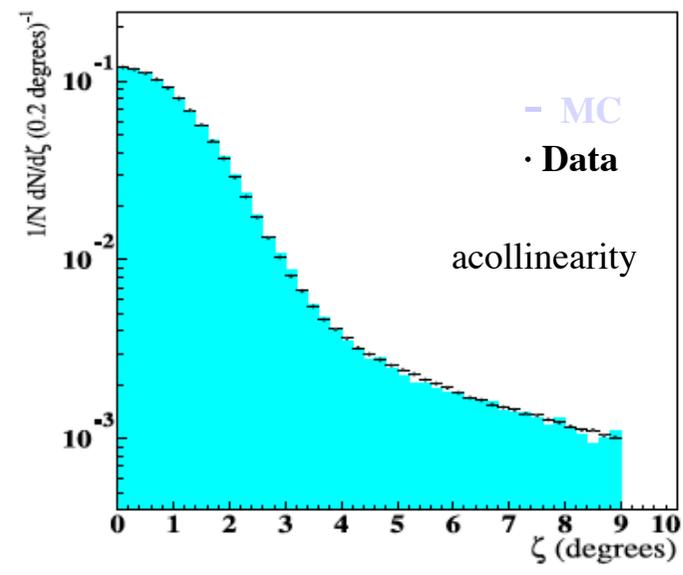
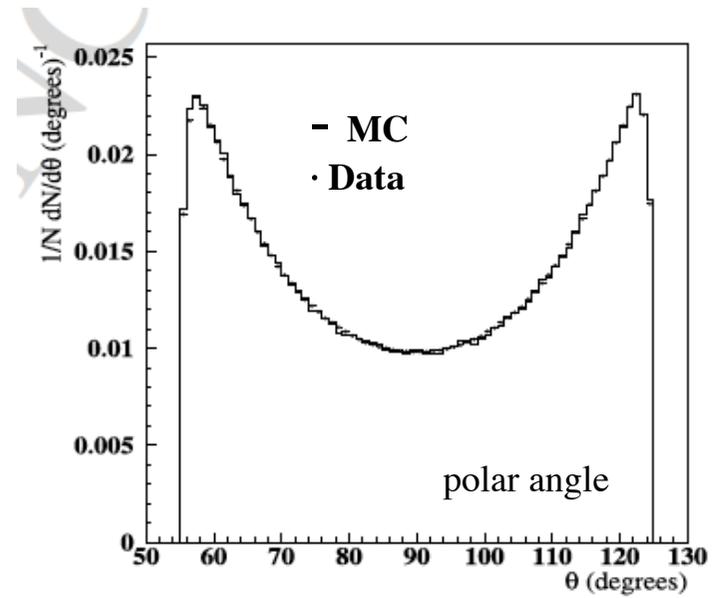
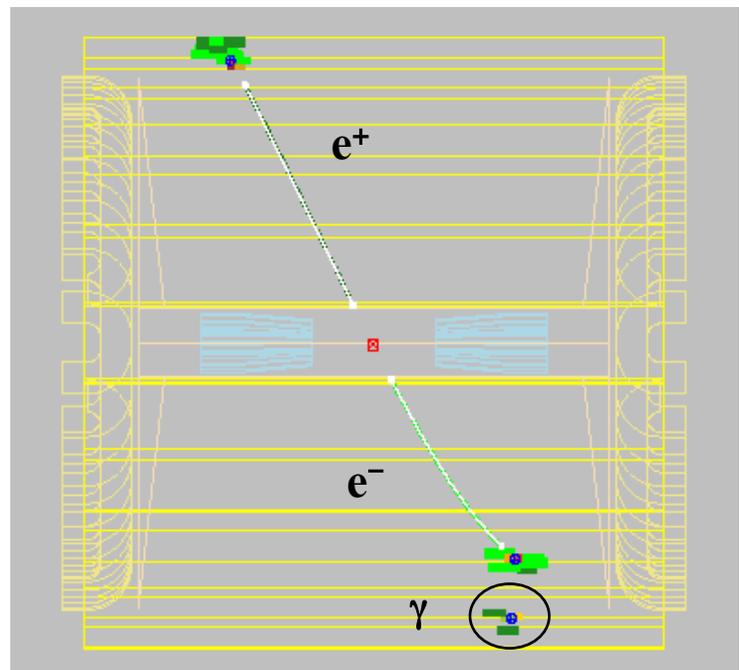
# Luminosity:



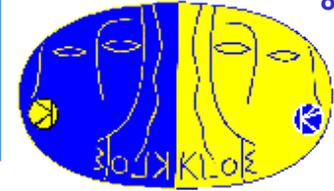
KLOE measures  $L$  with Bhabha scattering

$55^\circ < \theta < 125^\circ$   
acollinearity  $< 9^\circ$   
 $p \geq 400$  MeV

$$\int \mathcal{L} dt = \frac{N_{obs} - N_{bkg}}{\sigma_{eff}}$$



# LA Event Selection (KLOE10)

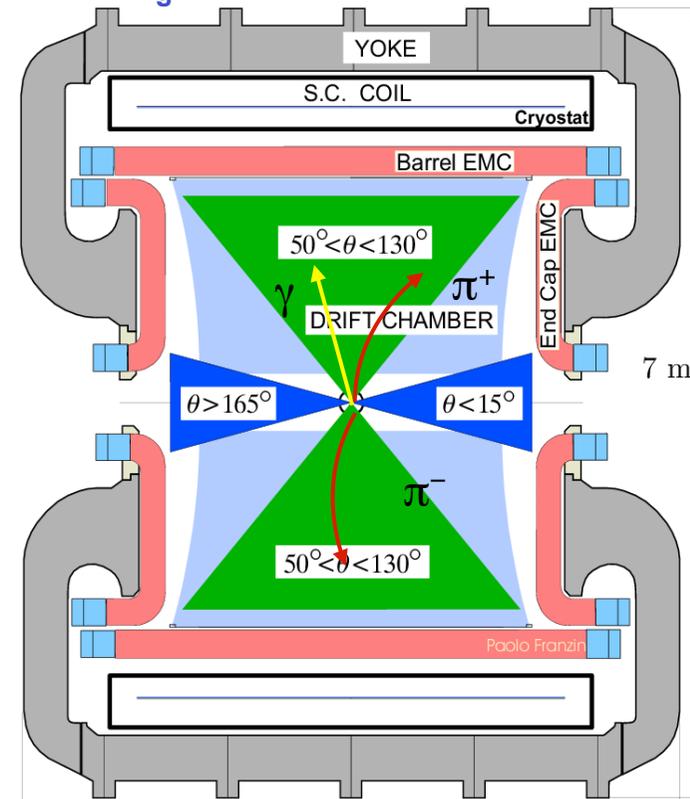


**2 pion tracks at large angles**  
 $50^\circ < \theta_p < 130^\circ$

**Photons at large angles**  
 $50^\circ < \theta_\gamma < 130^\circ$

- ✓ independent complementary analysis
- ✓ threshold region  $(2m_\pi)^2$  accessible
- ✓  $\gamma_{\text{ISR}}$  photon detected  
(4-momentum constraints)
- ✓ lower signal statistics
- ✓ larger contribution from FSR events
- ✓ larger  $\phi \rightarrow \pi^+\pi^-\pi^0$  background contamination
- ✓ irreducible background from  $\phi$  decays ( $\phi \rightarrow f_0 \gamma \rightarrow \pi\pi \gamma$ )

**At least 1 photon with  $50^\circ < \theta_\gamma < 130^\circ$   
 and  $E_\gamma > 20$  MeV  $\rightarrow$  photon detected**



**Threshold region non-trivial**  
 due to irreducible FSR-effects, which  
 have to be estimated from MC using  
 phenomenological models  
 (interference effects unknown)

